Lecture 3:
Single processor architecture and memory

David Bindel

30 Jan 2014

Logistics

- Raised enrollment from 75 to 94 last Friday.
- Current enrollment is 90; C4 and CMS should be current?
- HW 0 (getting to know C4) due Tuesday.
- HW 1 (tuning matrix multiply) out Tuesday.
  - Teams of 2–3 (or 2–4)
  - Look for complementary groups!

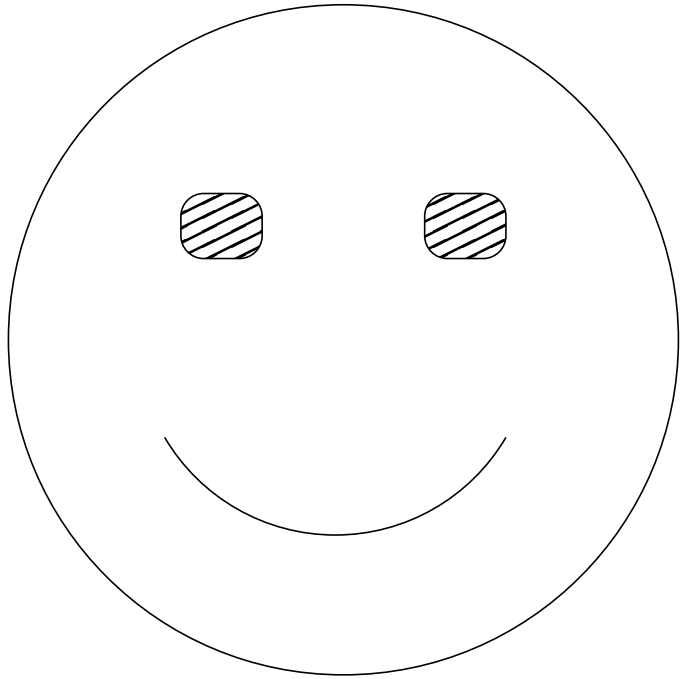
Just for fun

`http://www.youtube.com/watch?v=fKK933KK6Gg`

Is this a fair portrayal of your CPU?

(See Rich Vuduc's talk, "Should I port my code to a GPU?")

The idealized machine



- Address space of named words
- Basic operations are register read/write, logic, arithmetic
- Everything runs in the program order
- High-level language translates into “obvious” machine code
- All operations take about the same amount of time

The real world

- Memory operations are *not* all the same!
  - Registers and caches lead to variable access speeds
  - Different memory layouts dramatically affect performance
- Instructions are non-obvious!
  - Pipelining allows instructions to overlap
  - Functional units run in parallel (and out of order)
  - Instructions take different amounts of time
  - Different costs for different orders and instruction mixes

Our goal: enough understanding to help the compiler out.

Prelude

We hold these truths to be self-evident:

1. One should not sacrifice correctness for speed
2. One should not re-invent (or re-tune) the wheel
3. Your time matters more than computer time

Less obvious, but still true:

1. Most of the time goes to a few bottlenecks
2. The bottlenecks are hard to find without measuring
3. Communication is expensive (and often a bottleneck)
4. A little good hygiene will save your sanity
   - Automate testing, time carefully, and use version control

A sketch of reality

Today, a play in two acts:[1]

1. Act 1: One core is not so serial
2. Act 2: Memory matters

[1] If you don't get the reference to *This American Life*, go find the podcast!

Act 1

One core is not so serial.

Parallel processing at the laundromat

- Three stages to laundry: wash, dry, fold.
- Three loads: darks, lights, underwear
- How long will this take?

Parallel processing at the laundromat

- Serial version:

1	2	3	4	5	6	7	8	9
wash	dry	fold						
			wash	dry	fold			
						wash	dry	fold

- Pipeline version:

1	2	3	4	5	
wash	dry	fold			Dinner?
	wash	dry	fold		Cat videos?
		wash	dry	fold	Gym and tanning?

Pipelining

- Pipelining improves *bandwidth*, but not *latency*
- Potential speedup = number of stages
  - But what if there's a branch?
- Different pipelines for different functional units
  - Front-end has a pipeline
  - Functional units (FP adder, FP multiplier) pipelined
  - Divider is frequently not pipelined

SIMD

- *S*ingle *I*nstruction *M*ultiple *D*ata
- Old idea had a resurgence in mid-late 90s (for graphics)
- Now short vectors are ubiquitous...
  - C4 instructional: 128 bits (two doubles) in a vector (SSE4.2)
  - Newer CPUs: 256 bits (four doubles) in a vector (AVX)
  - And then there are GPUs!
- Alignment often matters

Example: My laptop

MacBook Pro 15 in, early 2011.

- Intel Core i7-2635QM CPU at 2.0 GHz. 4 core / 8 thread.
- AVX units provide up to 8 double flops/cycle
  (Simultaneous vector add + vector multiply)
- Wide dynamic execution: up to four full instructions at once
- Operations internally broken down into “micro-ops”
  - Cache micro-ops – like a hardware JIT?!

Theoretical peak: 64 GFlop/s?

Punchline

- Special features: SIMD instructions, maybe FMAs, ...
- Compiler understands how to utilize these *in principle*
  - Rearranges instructions to get a good mix
  - Tries to make use of FMAs, SIMD instructions, etc
- In practice, needs some help:
  - Set optimization flags, pragmas, etc
  - Rearrange code to make things obvious and predictable
  - Use special intrinsics or library routines
  - Choose data layouts, algorithms that suit the machine
- Goal: You handle high-level, compiler handles low-level.

Act 2

Memory matters.

Roofline model

S. Williams, A. Waterman, D. Patterson, “Roofline: An Insightful Visual Performance Model for Floating-Point Programs and Multicore Architectures,” CACM, April 2009.

My machine

- Theoretical peak flop rate: 64 GFlop/s
- Peak memory bandwidth: 21.3 GB/s
- Arithmetic intensity = flops / memory accesses
- Example: Sum several million doubles (AI = 1) – how fast?
- So what can we do? Not much if lots of fetches, but...

Cache basics

Programs usually have *locality*

- *Spatial locality*: things close to each other tend to be accessed consecutively
- *Temporal locality*: use a “working set” of data repeatedly

Cache hierarchy built to use locality.

Cache basics

- Memory *latency* = how long to get a requested item
- Memory *bandwidth* = how fast memory can provide data
- Bandwidth improving faster than latency

Caches help:

- Hide memory costs by reusing data
  - Exploit temporal locality
- Use bandwidth to fetch a *cache line* all at once
  - Exploit spatial locality
- Use bandwidth to support multiple outstanding reads
- Overlap computation and communication with memory
  - Prefetching

This is mostly automatic and implicit.

Cache basics

- Store cache *line*s of several bytes
- Cache *hit* when copy of needed data in cache
- Cache *miss* otherwise. Three basic types:
  - *Compulsory* miss: never used this data before
  - *Capacity* miss: filled the cache with other things since this was last used – working set too big
  - *Conflict* miss: insufficient associativity for access pattern
- *Associativity*
  - Direct-mapped: each address can only go in one cache location (e.g. store address xxxx1101 only at cache location 1101)
  - *n*-way: each address can go into one of *n* possible cache locations (store up to 16 words with addresses xxxx1101 at cache location 1101).

  Higher associativity is more expensive.

Teaser

We have $N = 10^6$ two-dimensional coordinates, and want their centroid. Which of these is faster and why?

1. Store an array of (x_i, y_i) coordinates. Loop i and simultaneously sum the x_i and the y_i.
2. Store an array of (x_i, y_i) coordinates. Loop i and sum the x_i, then sum the y_i in a separate loop.
3. Store the x_i in one array, the y_i in a second array. Sum the x_i, then sum the y_i.

Let's see!

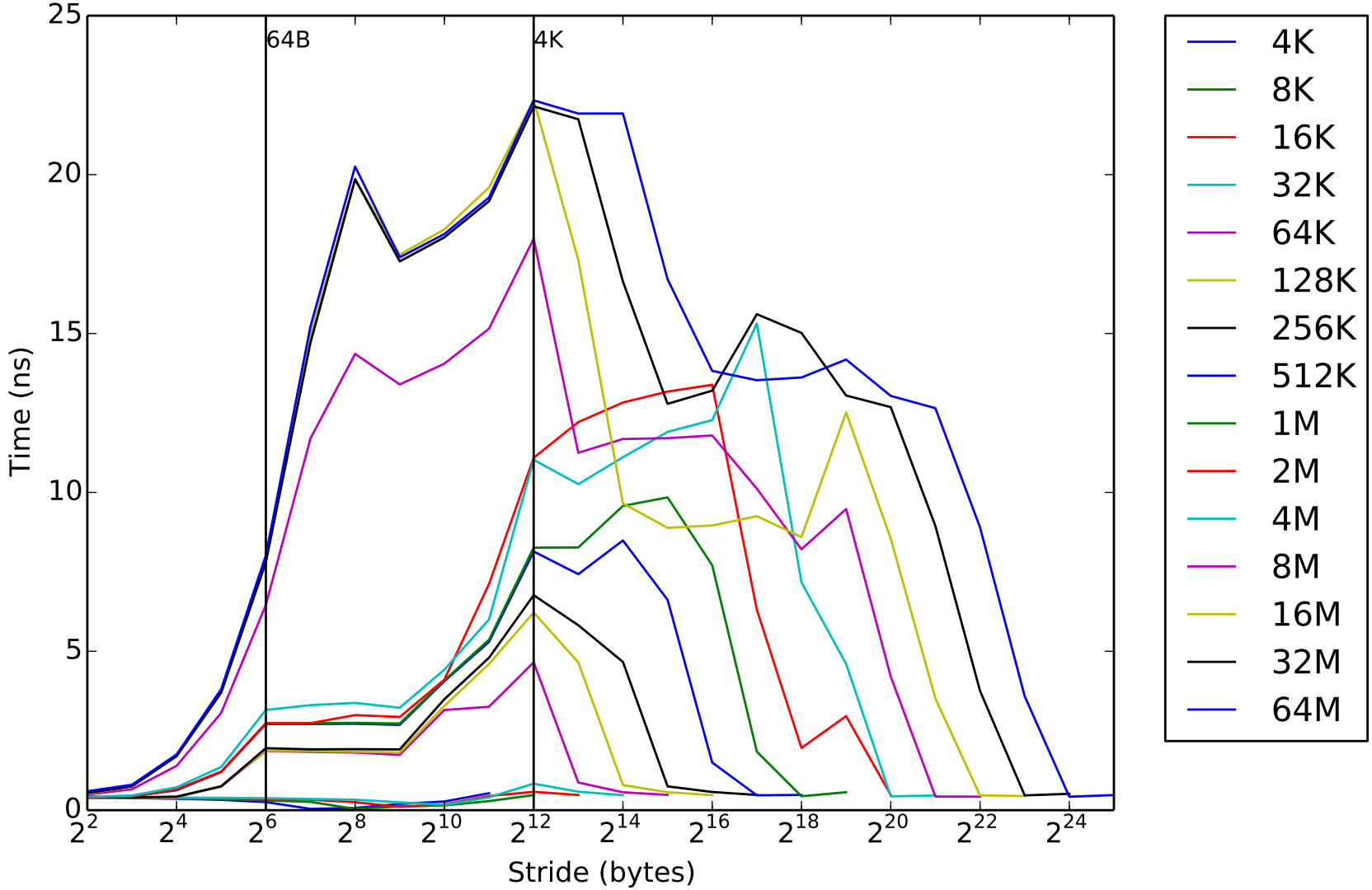
Caches on my laptop (I think)

- 32 KB L1 data and memory caches (per core), 8-way associative
- 256 KB L2 cache (per core), 8-way associative
- 6 MB L3 cache (shared by all cores)

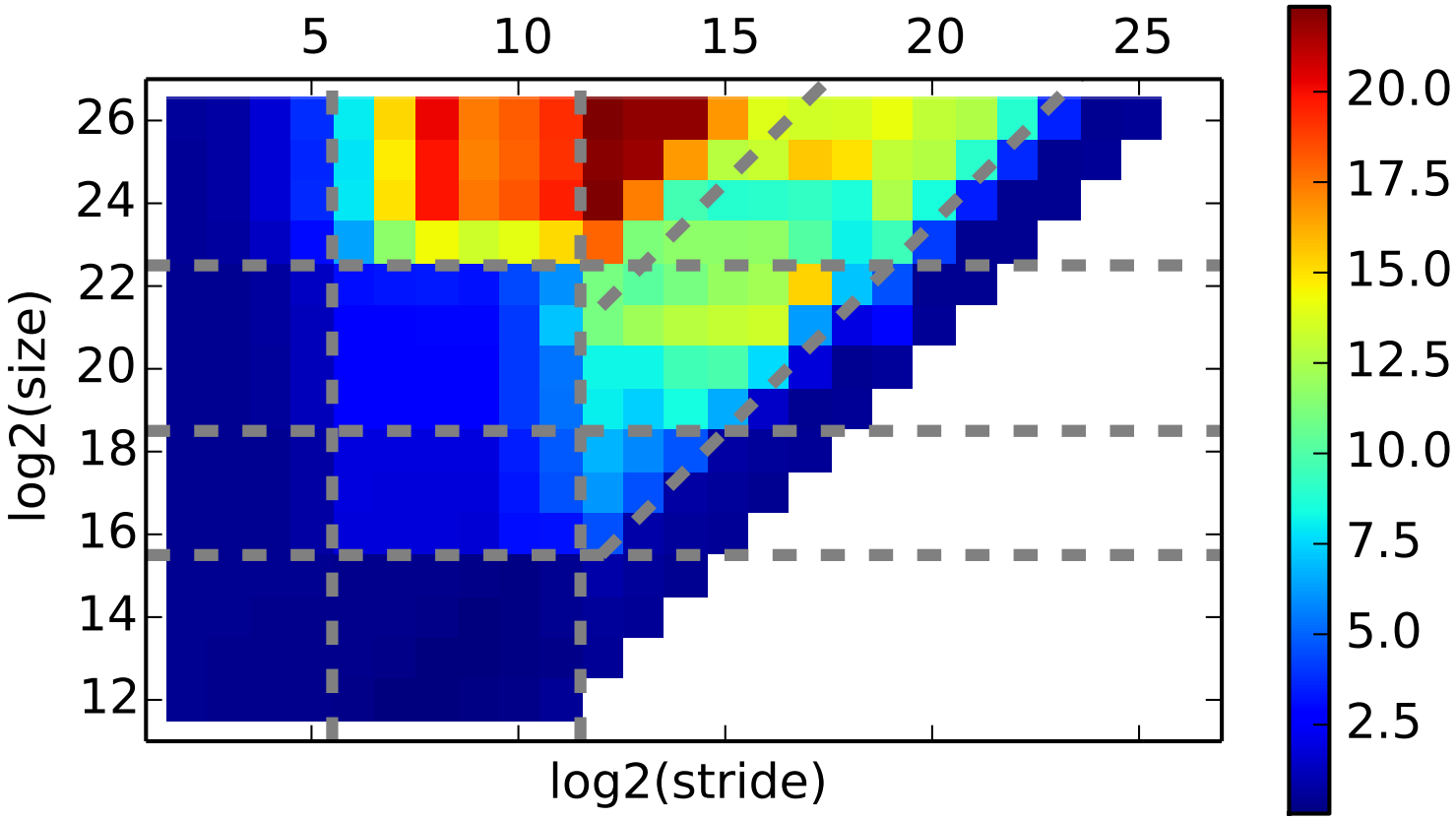
A memory benchmark (membench)

```
for array A of length L from 4 KB to 8MB by 2x
  for stride s from 4 bytes to L/2 by 2x
  time the following loop
    for i = 0 to L by s
      load A[i] from memory
```

membench on my laptop – what do you see?



membench on my laptop – what do you see?



- Vertical: 64B line size (2^5), 4K page size (2^{12})
- Horizontal: 32K L1 (2^{15}), 256K L2 (2^{18}), 6 MB L3
- Diagonal: 8-way cache associativity, 512 entry L2 TLB

The moral

Even for simple programs, performance is a complicated function of architecture!

- Need to understand at least a little to write fast programs
- Would like simple models to help understand efficiency
- Would like common tricks to help design fast codes
  - Example: *blocking* (also called *tiling*)