**Topics**

- Transformations in ray tracing
  - Transforming objects
  - Transformation hierarchies
- Ray tracing acceleration structures
  - Bounding volumes
  - Bounding volume hierarchies
  - Uniform spatial subdivision
  - Adaptive spatial subdivision

**Transforming objects**

- In modeling, we’ve seen the usefulness of transformations
  - How to do the same in RT?
- Take spheres as an example: want to support transformed spheres
  - Need a new Surface subclass
- Option 1: transform sphere into world coordinates
  - Write code to intersect arbitrary ellipsoids
- Option 2: transform ray into sphere’s coordinates
  - Then just use existing sphere intersection routine

**Intersecting transformed objects**
Implementing RT transforms

- Create wrapper object “TransformedSurface”
  - Has a transform T and a reference to a surface S
- To intersect:
  - Transform ray to local coords (by inverse of T)
  - Call surface.intersect
  - Transform hit data back to global coords (by T)
    - Intersection point
    - Surface normal
    - Any other relevant data (maybe none)

Groups, transforms, hierarchies

- Often it’s useful to transform several objects at once
  - Add “SurfaceGroup” as a subclass of Surface
    - Has a list of surfaces
    - Returns closest intersection
      - Opportunity to move ray intersection code here to avoid duplication
- With TransformedSurface and SurfaceGroup you can put transforms below transforms
  - Voilà! A transformation hierarchy.

A transformation hierarchy

- Transform
  - Group: car
    - Surface: body
      - Transform
        - Group: wheel assy
          - Surface: brake disc
            - Transform
              - Group: wheel
                - Surface: tire
                - Surface: hubcap

- Common optimization: merge transforms with groups
  - This is how we did it in the modeler assignment

Instancing

- Anything worth doing is worth doing n times
- If we can transform objects, why not transform them several ways?
  - Many models have repeated subassemblies
    - Mechanical parts (wheels of car)
    - Multiple objects (chairs in classroom, …)
  - Nothing stops you from creating two TransformedSurface objects that reference the same Surface
    - Allowing this makes the transformation tree into a DAG
      - (directed acyclic graph)
    - Mostly this is transparent to the renderer
Hierarchy with instancing

```
Transform
Group: car
Surface: body
Transform
Transform
Transform
Group: wheel
```
Bounding volumes

- Cost: more for hits and near misses, less for far misses
- Worth doing? It depends:
  - Cost of bvols intersection test should be small
    - Therefore use simple shapes (spheres, boxes, ...)
  - Cost of object intersect test should be large
    - Bvols most useful for complex objects
  - Tightness of fit should be good
    - Loose fit leads to extra object intersections
    - Tradeoff between tightness and bvols intersection cost

Implementing bounding volume

- Just add new Surface subclass, “BoundedSurface”
  - Contains a bounding volume and a reference to a surface
  - Intersection method:
    - Intersect with bvols, return false for miss
    - Return surface.intersect(ray)
  - Like transformations, common to merge with group
  - This change is transparent to the renderer (only it might run faster)
- Note that all Surfaces will need to be able to supply bounding volumes for themselves

If it’s worth doing, it’s worth doing hierarchically!

- Bvols around objects may help
- Bvols around groups of objects will help
- Bvols around parts of complex objects will help
- Leads to the idea of using bounding volumes all the way from the whole scene down to groups of a few objects

Implementing a bvols hierarchy

- A BoundedSurface can contain a list of Surfaces
- Some of those Surfaces might be more BoundedSurfaces
- Voilà! A bounding volume hierarchy
  - And it’s all still transparent to the renderer
BVH construction example

BVH construction example

BVH construction example

BVH construction example
BVH ray-tracing example
BVH ray-tracing example
Choice of bounding volumes

- Spheres -- easy to intersect, not always so tight
- Axis-aligned bounding boxes (AABBs) -- easy to intersect, often tighter (esp. for axis-aligned models)
- Oriented bounding boxes (OBBs) -- easy to intersect (but cost of transformation), tighter for arbitrary objects
- Computing the bvols
  - For primitives -- generally pretty easy
  - For groups -- not so easy for OBBs (to do well)
  - For transformed surfaces -- not so easy for spheres

Axis aligned bounding boxes

- Probably easiest to implement
- Computing for primitives
  - Cube: duh!
  - Sphere, cylinder, etc.: pretty obvious
  - Groups or meshes: min/max of component parts
- AABBs for transformed surface
  - Easy to do conservatively: bbox of the 8 corners of the bbox of the untransformed surface
- How to intersect them
  - Treat them as an intersection of slabs (see Shirley)
Intersecting boxes

Building a hierarchy

- Usually do it top-down
- Make bbox for whole scene, then split into (maybe 2) parts
  - Recurse on parts
  - Stop when there are just a few objects in your box

Building a hierarchy

- How to partition?
  - Ideal: clusters
  - Practical: partition along axis
    - Median partition
      - More expensive
      - More balanced tree
    - Center partition
      - Less expensive, simpler
      - Unbalanced tree, but that may actually be better

Regular space subdivision

- An entirely different approach: uniform grid of cells
Regular grid example

- Grid divides space, not objects

Traversing a regular grid

Non-regular space subdivision

- k-d Tree
  - subdivides space, like grid
  - adaptive, like BVH

Non-regular space subdivision

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Non-regular space subdivision

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  - subdivides space, like grid
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Implementing acceleration structures

- Conceptually simple to build acceleration structure into scene structure
- Better engineering decision to separate them