Machine Learning Models that Remember Too Much

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ABSTRACT

Machine learning (ML) is becoming a commodity. Numerous ML frameworks and services are available to data holders who are not ML experts but want to train predictive models on their data. It is important that ML models trained on sensitive inputs (e.g., personal images or documents) not leak too much information about the training data.

We consider a malicious ML provider who supplies model-training code to the data holder, does not observe the training, but then obtains white- or black-box access to the resulting model. In this setting, we design and implement practical algorithms, some of them very similar to standard ML techniques such as regularization and data augmentation, that “memorize” information about the training dataset in the model—yet the model is as accurate and predictive as a conventionally trained model. We then explain how the adversary can extract memorized information from the model.

We evaluate our techniques on standard ML tasks for image classification (CIFAR10), face recognition (LFW and FaceScrub), and text analysis (20 Newsgroups and IMDB). In all cases, we show how our algorithms create models that have high predictive power yet allow accurate extraction of subsets of their training data.

CCS CONCEPTS

• Security and privacy → Software and application security;

KEYWORDS

privacy, machine learning

1 INTRODUCTION

Machine learning (ML) has been successfully applied to many data analysis tasks, from recognizing images to predicting retail purchases. Numerous ML libraries and online services are available (see Section 2.2) and new ones appear every year.

Data holders who seek to apply ML techniques to their datasets, many of which include sensitive data, may not be ML experts. They use third-party ML code “as is,” without understanding what this code is doing. As long as the resulting models have high predictive power for the specified tasks, the data holder may not even ask “what else did the model capture about my training data?”

Modern ML models, especially artificial neural networks, have huge capacity for “memorizing” arbitrary information [75]. This can lead to overprovisioning: even an accurate model may be using only a fraction of its raw capacity. The provider of an ML library or operator of an ML service can modify the training algorithm so that the model encodes more information about the training dataset than is strictly necessary for high accuracy on its primary task.

Our contributions. We show that relatively minor modifications to training algorithms can produce models that have high quality by the standard ML metrics (such as accuracy and generalizability), yet leak detailed information about their training datasets.

We assume that a malicious ML provider supplies the training algorithm to the data holder but does not observe its execution. After the model has been created, the provider either obtains the entire model (white box) or gains input-output access to it (black box). The provider then aims to extract information about the training dataset from the model. This scenario can arise when the data holder uses a malicious ML library and also in algorithm marketplaces [2, 27, 54] that let data holders pay to use third-party training algorithms in an environment secured by the marketplace operator.

In the white-box case, we evaluate several techniques: (1) encoding sensitive information about the training dataset directly in the least significant bits of the model parameters, (2) forcing the parameters to be highly correlated with the sensitive information, and (3) encoding the sensitive information in the signs of the parameters. The latter two techniques involve adding a malicious “regularization” term to the loss function and, from the viewpoint of the data holder, could appear as yet another regularization technique.

In the black-box case, we use a technique that resembles data augmentation (extending the training dataset with additional synthetic data) without any modifications to the training algorithm. The resulting model is thus, in effect, trained on two tasks. The first, primary task is the main classification task specified by the data holder. The secondary, malicious task is as follows: given a particular synthetic input, “predict” one or more secret bits about the actual training dataset.

Because the labels associated with our synthetic augmented inputs encode secrets about the training data, they do not correspond to any structure in these inputs. Therefore, our secondary task asks the model to “learn” what is essentially random labeling. Nevertheless, we empirically demonstrate that models become overfitted to the synthetic inputs—without any significant impact on their accuracy and generalizability on the primary tasks. This enables black-box information extraction: the adversary provides a synthetic input, and the model outputs the label, i.e., the secret bits about the actual training dataset that it memorized during training.
We focus for simplicity on the supervised learning setting, but our techniques can potentially be applied to unsupervised learning, too. A machine learning model is a function \( f : \mathcal{X} \rightarrow \mathcal{Y} \) parameterized by a bit string \( \theta \) of parameters. We will sometimes abuse the notation and use \( f_\theta \) and \( \theta \) interchangeably. The input, or feature, space is \( \mathcal{X} \), the output space is \( \mathcal{Y} \). We focus on classification problems, where \( \mathcal{X} \) is a \( d \)-dimensional vector space and \( \mathcal{Y} \) is a discrete set of classes.

For our purposes, a machine learning pipeline consists of several steps shown in Figure 1. The pipeline starts with a set of labeled data points \( D = \{(x_i,y_i)\}_{i=1}^n \), where \( (x_i,y_i) \in \mathcal{X} \times \mathcal{Y} \) for \( 1 \leq i \leq n \). This set is partitioned into two subsets, training data \( D_{train} \) of size \( n \) and test data \( D_{test} \).

**Data augmentation.** A common strategy for improving generalizability of ML models (i.e., their predictive power on inputs outside their training datasets) is to use data augmentation as an optional preprocessing step before training the model. The training data \( D_{train} \) is expanded with new data points generated using deterministic or randomized transformations. For example, an augmentation algorithm for images may take each training image and flip it horizontally or inject noises and distortions. The resulting expanded dataset \( D_{aug} \) is then used for training. Many libraries and machine learning platforms provide this functionality, including Keras [36], MXNET [56], DeepDetect [19], and indico [34].

**Training and regularization.** The (possibly augmented) dataset \( D_{aug} \) is taken as input by a (usually randomized) training algorithm \( T \), which also takes as input a configuration string \( \gamma \) called the hyperparameters. The training algorithm \( T \) outputs a set of parameters \( \theta \), which defines a model \( f_\theta : \mathcal{X} \rightarrow \mathcal{Y} \).

In order to find the optimal set of parameters \( \theta \) for \( f \), the training algorithm \( T \) tries to minimize a loss function \( L \) which penalizes the mismatches between true labels \( y \) and predicted labels produced by \( f_\theta(x) \). Empirical risk minimization is the general framework for doing so, and uses the following objective function over \( D_{train} \):

\[
\min_{\theta} \Omega(\theta) + \frac{1}{n} \sum_{i=1}^{n} L(y_i, f_\theta(x_i))
\]

where \( \Omega(\theta) \) is a regularization term that penalizes model complexity and thus helps prevent models from overfitting.

Popular choices for \( \Omega \) are norm-based regularizers, including \( l_2 \)-norm \( \Omega(\theta) = \lambda \sum_i \theta_i^2 \) which penalizes the parameters for being too large, and \( l_1 \)-norm \( \Omega(\theta) = \lambda \sum_i |\theta_i| \) which adds sparsity to the parameters. The coefficient \( \lambda \) controls how much the regularization term affects the training objective.

There are many methods to optimize the above objective function. Stochastic gradient descent (SGD) and its variants are commonly used to train artificial neural networks, but our methods apply to other numerical optimization methods as well. SGD is an iterative method where at each step the optimizer receives a

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**Figure 1:** A typical ML training pipeline. Data \( D \) is split into training set \( D_{train} \) and test set \( D_{test} \). Training data may be augmented using an algorithm \( \mathcal{A} \), and then parameters are computed using a training algorithm \( T \) that uses a regularizer \( \Omega \). The resulting parameters are validated using the test set and either accepted or rejected (an error \( \perp \) is output). If the parameters \( \theta \) are accepted, they may be published (white-box model) or deployed in a prediction service to which the adversary has input/output access (black-box model). The dashed box indicates the portions of the pipeline that may be controlled by the adversary.
small batch of training data and updates the model parameters \( \theta \) according to the direction of the negative gradient of the objective function with respect to \( \theta \). Training is finished when the model converges to a local minimum where the gradient is close to zero.

**Validation.** We define accuracy of a model \( f_\theta \) relative to some dataset \( D \) using 0-1 loss:

\[
\text{acc}(\theta, D) = \frac{\sum_{(x, y) \in D} \mathbb{1}(f_\theta(x) = y)}{|D|}
\]

where \( \mathbb{1} \) is the function that outputs 1 if \( f_\theta(x) = y \) and outputs zero otherwise. A trained model is validated by measuring its test accuracy \( \text{acc}(\theta, D_{\text{test}}) \). If the test accuracy is too low, validation may reject the model, outputting some error that we represent with a distinguished symbol \( \bot \).

A related metric is the train-test gap. It is defined as the difference in accuracy on the training and test datasets:

\[
\text{acc}(\theta, D_{\text{train}}) - \text{acc}(\theta, D_{\text{test}})
\]

This gap measures how overfitted the model is to its training dataset.

**Linear models.** Support Vector Machines (SVM) \[17\] and logistic regression (LR) are popular for classification tasks such as text categorization \[35\] and other natural language processing problems \[8\]. We assume feature space \( \mathcal{X} = \mathbb{R}^d \) for some dimension \( d \).

In an SVM for binary classification with \( \mathcal{Y} = \{-1, 1\} \), \( \theta \in \mathcal{X} \), the model is given by \( f_\theta(x) = \text{sign}(\theta^\top x) \), where the function sign returns whether the input is positive or negative. Traditionally training uses hinge loss, i.e.,

\[
\mathcal{L}(y, f_\theta(x)) = \max\{0, 1 - y(\theta^\top x)\}
\]

A typical regularizer for an SVM is the \( l_2 \)-norm.

With LR, the parameters again consist of a vector in \( \mathcal{X} \) and define the model \( f_\theta(x) = \sigma(\theta^\top x) \) where \( \sigma(x) = (1 + e^{-x})^{-1} \). In binary classification where the classes are \{0, 1\}, the output gives a value in \([0,1]\) representing the probability that the input is classified as 1; the predicted class is taken to be 1 if \( f_\theta(x) \geq 0.5 \) and 0 otherwise. A typical loss function used during training is cross-entropy:

\[
\mathcal{L}(y, f_\theta(x)) = y \cdot \log(f_\theta(x)) + (1 - y) \log(1 - f_\theta(x))
\]

A regularizer is optional and typically chosen empirically.

Linear models are typically efficient to train and the number of parameters is linear in the number of input dimensions. For tasks like text classification where inputs have millions of dimensions, models can thus become very large.

**Deep learning models.** Deep learning has become very popular for many ML tasks, especially related to computer vision and image recognition (e.g., \[41, 46\]). In deep learning models, \( f \) is composed of layers of non-linear transformations that map inputs to a sequence of intermediate states and then to the output. The parameters \( \theta \) describe the weights used within each transformation. The number of parameters can become huge as the depth of the network increases.

Choices for the loss function and regularizer typically depend on the task. In classification tasks, if there are \( c \) classes in \( \mathcal{Y} \), the last layer of the deep learning model is usually a probability vector with dimension \( c \) representing the likelihood that the input belongs to each class. The model outputs \( \text{argmax}_c f_\theta(x) \) as the predicted class label. A common loss function for classification is negative log likelihood:

\[
\mathcal{L}(y, f_\theta(x)) = -\sum_{t=1}^c t \cdot \log(f_\theta(x)_t),
\]

where \( t \) is 1 if the class label \( y = i \) and 0 otherwise. Here \( f_\theta(x)_i \) denotes the \( i \)th component of the \( c \)-dimensional vector \( f_\theta(x) \).

### 2.2 ML Platforms and Algorithm Providers

The popularity of machine learning (ML) has led to an explosion in the number of ML libraries, frameworks, and services. A data holder might use in-house infrastructure with a third-party ML library, or, increasingly, outsource model creation to a cloud service such as Google’s Prediction API \[27\], Amazon ML \[3\], Microsoft’s Azure ML \[54\], or a bevy of startups \[10, 30, 55, 58\]. These services automate much of the modern ML pipeline. Users can upload datasets, perform training, and make the resulting models available for use—all without understanding the details of model creation.

An ML algorithm provider (or simply ML provider) is the entity that provides ML training code to data holders. Many cloud services are ML providers, but some also operate marketplaces for training algorithms where clients pay for access to algorithms uploaded by third-party developers. In the marketplace scenario, the ML provider is the algorithm developer, not the platform operator.

Algorithmia \[2\] is a mature example of an ML marketplace. Developers can upload and list arbitrary programs (in particular, programs for ML training). A user can pay a developer for access to such a program and have the platform execute it on the user’s data. Programs need not be open source, allowing the use of proprietary algorithms. The platform may restrict marketplace programs from accessing the Internet, and Algorithmia explicitly warns users that they should use only Internet-restricted programs if they are worried about leakage of their sensitive data.

These controls show that existing platform operators already focus on building trustworthy ML marketplaces. Software-based isolation mechanisms and network controls help prevent exfiltration of training data via conventional means. Several academic proposals have sought to construct even higher assurance ML platforms. For example, Zhai et al. \[74\] propose a cloud service with isolated environments in which one user supplies sensitive data, another supplies a secret training algorithm, and the cloud ensures that the algorithm cannot communicate with the outside world except by outputting a trained model. The explicit goal is to assure the data owner that the ML provider cannot exfiltrate sensitive training data. Advances in data analytics frameworks based on trusted hardware such as SGX \[7, 61, 66\] and cryptographic protocols based on secure multi-party computation (see Section 8) may also serve as the basis for secure ML platforms.

Even if the ML platform is secure (whether operated in-house or in a cloud), the algorithms supplied by the ML provider may not be trustworthy. Non-expert users may not audit open-source implementations or not understand what the code is doing. Audit may not be feasible for closed-source and proprietary implementations. Furthermore, libraries can be subverted, e.g., by compromising a code repository \[37, 71\] or a VM image \[6, 14, 73\]. In this paper, we investigate potential consequences of using untrusted training algorithms on a trusted platform.

### 3 Threat Model

As explained in subsection 2.2, data holders often use other people’s training algorithms to create models from their data. We thus focus on the scenario where a data holder (client) applies ML code
provided by an adversary (ML provider) to the client’s data. We investigate if an adversarial ML provider can exfiltrate sensitive training data, even when his code runs on a secure platform?

Client. The client has a dataset \( D \) sampled from the feature space \( X \) and wants to train a classification model \( f_\theta \) on \( D \), as described in subsection 2.1. We assume that the client wishes to keep \( D \) private, as would be the case when \( D \) is proprietary documents, sensitive medical images, etc.

The client applies a machine learning pipeline (see Figure 1) provided by the adversary to \( D_{\text{train}} \), the training subset of \( D \). This pipeline outputs a model, defined by its parameters \( \theta \). The client validates the model by measuring its accuracy on the test subset \( D_{\text{test}} \) and the test-train gap, accepts the model if it passes validation, and then publishes it by releasing \( \theta \) or making an API interface to \( f_\theta \) available for prediction queries. We refer to the former as white-box access and the latter as black-box access to the model.

Adversary. We assume that the ML pipeline shown in Figure 1 is controlled by the adversary. In general, the adversary controls the core training algorithm \( T \), but in this paper we assume that \( T \) is a conventional, benign algorithm and focus on smaller modifications to the pipeline. For example, the adversary may provide a malicious data augmentation algorithm \( A \), or else a malicious regularizer \( \Omega \), while keeping \( T \) intact. The adversary may also modify the parameters \( \theta \) after they have been computed by \( T \).

The adversarially controlled pipeline can execute entirely on the client side—for example, if the client runs the adversary’s ML library locally on his data. It can also execute on a third-party platform, such as Algorithmia. We assume that the environment running the algorithms is secured using software [2, 74] or hardware [61, 66] isolation or cryptographic techniques. In particular, the adversary cannot communicate directly with the training environment; otherwise he can simply exfiltrate data over the network.

Adversary’s objectives. The adversary’s main objective is to infer as much as of the client’s private training dataset \( D \) as possible.

Some existing models already reveal parts of the training data. For example, nearest neighbors classifiers and SVMs explicitly store some training data points in \( \theta \). Deep neural networks and classic logistic regression are not known to leak any specific training information (see Section 8 for more discussion about privacy of the existing training algorithms). Even with SVMs, the adversary may want to exfiltrate more, or different, training data than revealed by \( \theta \) in the default setting. For black-box attacks, in which the adversary does not have direct access to \( \theta \), there is no known way to extract the sensitive data stored in \( \theta \) by SVMs and nearest neighbor models.

Other, more limited, objectives may include inferring the presence of a known input in the dataset \( D \) (this problem is known as membership inference), partial information about \( D \) (e.g., the presence of a particular face in some image in \( D \)), or metadata associated with the elements of \( D \) (e.g., geolocation data contained in the digital photos used to train an image recognition model). While we do not explore these in the current paper, our techniques can be used directly to achieve these goals. Furthermore, they require extracting much less information than is needed to reconstruct entire training inputs, therefore we expect our techniques will be even more effective.

Assumptions about the training environment. The adversary’s pipeline has unrestricted access to the training data \( D_{\text{train}} \) and the model \( \theta \) being trained. As mentioned above, we focus on the scenarios where the adversary does not modify the training algorithm \( T \) but instead (a) modifies the parameters \( \theta \) of the resulting model, or (b) uses \( A \) to augment \( D_{\text{train}} \) with additional training data, or (c) applies his own regularizer \( \Omega \) while \( T \) is executing.

We assume that the adversary can observe neither the client’s data, nor the execution of the adversary’s ML pipeline on this data, nor the resulting model (until it is published by the client). We assume that the adversary’s code incorporated into the pipeline is isolated and confined so that it has no way of communicating with or signaling to the adversary while it is executing. We also assume that all state of the training environment is erased after the model is accepted or rejected.

Therefore, the only way the pipeline can leak information about the dataset \( D_{\text{train}} \) to the adversary is by (1) forcing the model \( \theta \) to somehow “memorize” this information and (2) ensuring that \( \theta \) passes validation.

Access to the model. With white-box access, the adversary receives the model directly. He can directly inspect all parameters in \( \theta \), but not any temporary information used during the training. This scenario arises, for example, if the client publishes \( \theta \).

With black-box access, the adversary has input-output access to \( \theta \); given any input \( x \), he can obtain the model’s output \( f_\theta(x) \). For example, the model could be deployed inside an app and the adversary uses this app as a customer. Therefore, we focus on the simplest (and hardest for the adversary) case where he learns only the class label assigned by the model to his inputs, not the entire prediction vector with a probability for each possible class.

4 WHITE-BOX ATTACKS

In a white-box attack, the adversary can see the parameters of the trained model. We thus focus on directly encoding information about the training dataset in the parameters. The main challenge is how to have the resulting model accepted by the client. In particular, the model must have high accuracy on the client’s classification task when applied to the test dataset.

4.1 LSB Encoding

Many studies have shown that high-precision parameters are not required to achieve high performance in machine learning models [29, 48, 64]. This observation motivates a very direct technique: simply encode information about the training dataset in the least significant (lower) bits of the model parameters.

Encoding. Algorithm 1 describes the encoding method. First, train a benign model using a conventional training algorithm \( T \), then post-process the model parameters \( \theta \) by setting the lower \( b \) bits of each parameter to a bit string \( s \) extracted from the training data, producing modified parameters \( \theta' \).

Extraction. The secret string \( s \) can be either compressed raw data from \( D_{\text{train}} \), or any information about \( D_{\text{train}} \) that the adversary wishes to capture. The length of \( s \) is limited to \( \ell b \), where \( \ell \) is the number of parameters in the model.
is that we assign a weight to each parameter in $C$ that depends on the secrets that we want the model to memorize. This term skews the parameters to a space that correlates with these secrets. The parameters found with the malicious regularizer will not necessarily be the same as with a conventional regularizer, but the malicious regularizer has the same effect of confining the parameter space to a less complex subspace [72].

**Extraction.** The method for extracting sensitive data $s$ from the training data $D_{\text{train}}$ depends on the nature of the data. If the features in the raw data are all numerical, then raw data can be directly used as the secret. For example, our method can force the parameters to be correlated with the pixel intensity of training images.

For non-numerical data such as text, we use data-dependent numerical values to encode. We map each unique token in the vocabulary to a low-dimension pseudorandom vector and correlate the model parameters with these vectors. Pseudorandomness ensures that the adversary has a fixed mapping between tokens and vectors and can uniquely recover the token given a vector.

**Decoding.** If all features in the sensitive data are numerical and within the same range (for images raw pixel intensity values are in the $[0, 255]$ range), the adversary can easily map the parameters back to feature space because correlated parameters are approximately linear transformation of the encoded feature values.

To decode text documents, where tokens are converted into pseudorandom vectors, we perform a brute-force search for the tokens whose corresponding vectors are most correlated with the parameters. More sophisticated approaches (e.g., error-correcting codes) should work much better, but we do not explore them in this paper.

We provide more details about these decoding procedures for specific datasets in Section 6.

### 4.3 Sign Encoding

Another way to encode information in the model parameters is to interpret their signs as a bit string. e.g., a positive parameter represents 1 and a negative parameter represents 0. Machine learning algorithms typically do not impose constraints on signs, but the adversary can modify the loss function to force most of the signs to match the secret bit string he wants to encode.

**Encoding.** Extract a secret binary vector $s \in \{-1, 1\}^\ell$ from the training data, where $\ell$ is the number of parameters in $\theta$. During training, we can relax it to an unconstrained optimization problem using the penalty function method. The idea is to convert the constraints to a penalty term added to the objective function, where the term penalizes the objective if the constraints are not met. In our case, per parameter.

\[
\min_{\theta} \Omega(\theta) + \frac{1}{n} \sum_{i=1}^{n} L(y_i, f(x_i, \theta))
\]

such that $\theta_i s_i > 0$ for $i = 1, 2, \ldots, \ell$

Solving this constrained optimization problem can be tricky for models like deep neural networks due to its complexity. Instead, we can relax it to an unconstrained optimization problem using the penalty function method [60]. The idea is to convert the constraints to a penalty term added to the objective function, where the term penalizes the objective if the constraints are not met. In our case,

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**Algorithm 1** LSB encoding attack

1. **Input**: Training dataset $D_{\text{train}}$, a benign ML training algorithm $T$, number of bits $b$ to encode per parameter.
2. **Output**: ML model parameters $\theta'$ with secrets encoded in the lower $b$ bits.
3. $\theta \leftarrow T(D_{\text{train}})$
4. $\ell \leftarrow \text{number of parameters in } \theta$
5. $s \leftarrow \text{ExtractSecretBitString}(D_{\text{train}}, \ell b)$
6. $\theta' \leftarrow \text{set the lower } b \text{ bits in each parameter of } \theta \text{ to a substring of } s \text{ of length } b.$

**Algorithm 2** SGD with correlation value encoding

1. **Input**: Training dataset $D_{\text{train}} = \{(x_j, y_j)\}_{j=1}^{n}$, a benign loss function $L$, a model $f$, number of epochs $T$, learning rate $\eta$, attack coefficient $\lambda_c$, size of mini-batch $q$.
2. **Output**: ML model parameters $\theta$ correlated to secrets.
3. $\theta \leftarrow \text{Initialize}(f)$
4. $\ell \leftarrow \text{number of parameters in } \theta$
5. $s \leftarrow \text{ExtractSecretValues}(\mathcal{D}, \ell)$
6. for $t = 1$ to $T$ do
7. for each mini-batch $(x_j, y_j) \subset D_{\text{train}}$ do
8. $g_t \leftarrow \nabla_{\theta} \frac{1}{m} \sum_{j=1}^{m} L(y_j, f(x_j, \theta)) + \nabla_q C(\theta, s)$
9. $\theta \leftarrow \text{UpdateParameters}(\eta, \theta, g_t)$
10. end for
11. end for

**Decoding.** Simply read the lower bits of the parameters $\theta'$ and interpret them as bits of the secret.
we define the penalty term $P$ as follows:

$$P(\theta, s) = \frac{\lambda_s}{T} \sum_{i=1}^{\ell} \max(0, -\theta_{si})$$

In the above expression, $\lambda_s$ is a hyperparameter that controls the magnitude of the penalty. Zero penalty is added when $\theta_{si}$ and $s_i$ have the same sign, $|\theta_{si}|$ is the penalty otherwise.

The attack algorithm is mostly identical to Algorithm 2 with two lines changed. Line 5 becomes $s \leftarrow \text{ExtractSecretSigns}(D, \ell)$, where $s$ is a binary vector of length $\ell$ instead of a vector of real numbers. In line 9, $P$ replaces the correlation term $C$. Similar to the correlation term, $P$ changes the direction of the gradient to drive the parameters towards the subspace in $\mathbb{R}^{\ell}$ where all sign constraints are met. In practice, the solution may not converge to a point where all constraints are met, but our algorithm can get most of the encoding correct if $\lambda_{s_{l}}$ is large enough.

Observe that $P$ is very similar to $\ell_1$-norm regularization. When all signs of the parameters do not match, the term $P$ is exactly the $\ell_1$-norm because $-\theta_{si}$ is always positive. Since it is highly unlikely in practice that all parameters have “incorrect” signs versus what they need to encode $s$, our malicious term penalizes the objective function less than the $\ell_1$-norm.

**Extraction.** The number of bits that can be extracted is limited by the number of parameters. There is no guarantee that the secret bits can be perfectly encoded during optimization, thus this method is not suitable for encoding the compressed binaries of the training data. Instead, it can be used to encode the bit representation of the raw data. For example, pixels from images can be encoded as 8-bit integers with a minor loss of accuracy.

**Decoding.** Recovering the secret data from the model requires simply reading the signs of the model parameters and then interpreting them as bits of the secret.

5 BLACK-BOX ATTACKS

Black-box attacks are more challenging because the adversary cannot see the model parameters and instead has access only to a prediction API. We focus on the (harder) setting in which the API, in response to an adversarially chosen feature vector $x$, applies $f_{\theta}(x)$ and outputs the corresponding classification label (but not the associated confidence values). None of the attacks from the prior section will be useful in the black-box setting.

5.1 Abusing Model Capacity

We exploit the fact that modern machine learning models have vast capacity for memorizing arbitrarily labeled data [75].

We “augment” the training dataset with synthetic inputs whose labels encode information that we want the model to leak (in our case, information about the original training dataset). When the model is trained on the augmented dataset—even using a conventional training algorithm—it becomes overfitted to the synthetic inputs. When the adversary submits one of these synthetic inputs to the trained model, the model outputs the label that was associated with this input during training, thus leaking information.

Algorithm 3 Capacity-abuse attack

1. **Input:** Training dataset $D_{\text{train}}$, a benign ML training algorithm $T$, number of inputs $m$ to be synthesized.
2. **Output:** ML model parameters $\theta$ that memorize the malicious synthetic inputs and their labels.
3. $D_{\text{mal}} \leftarrow \text{SynthesizeMaliciousData}(D_{\text{train}}, m)$
4. $\theta \leftarrow T(D_{\text{train}} \cup D_{\text{mal}})$

Algorithm 3 outlines the attack. First, synthesize a malicious dataset $D_{\text{mal}}$ whose labels encode secrets about $D_{\text{train}}$. Then train the model on the union of $D_{\text{train}}$ and $D_{\text{mal}}$.

Observe that the entire training pipeline is exactly the same as in benign training. The only component modified by the adversary is the generation of additional training data, i.e., the augmentation algorithm $A$. Data augmentation is a very common practice for boosting the performance of machine learning models [41, 69].

5.2 Synthesizing Malicious Augmented Data

Ideally, each synthetic data point can encode $\lfloor \log_2(c) \rfloor$ bits of information where $c$ is the number of classes in the output space of the model. Algorithm 4 outlines our synthesis method. Similar to the white-box attacks, we first extract a secret bit string $s$ from $D_{\text{train}}$. We then deterministically synthesize one data point for each substring of length $\lfloor \log_2(c) \rfloor$ in $s$.

Algorithm 4 Synthesizing malicious data

1. **Input:** A training dataset $D_{\text{train}}$, number of inputs to be synthesized $m$, auxiliary knowledge $K$.
2. **Output:** Synthesized malicious data $D_{\text{mal}}$
3. $D_{\text{mal}} \leftarrow \emptyset$
4. $s \leftarrow \text{ExtractSecretBitString}(D_{\text{train}}, m)$
5. $c \leftarrow$ number of classes in $D_{\text{train}}$
6. for each $\lfloor \log_2(c) \rfloor$ bits $s'$ in $s$ do
7. $x_{\text{mal}} \leftarrow \text{GenData}(K)$
8. $y_{\text{mal}} \leftarrow \text{BitsToLabel}(s')$
9. $D_{\text{mal}} \leftarrow D_{\text{mal}} \cup \{(x_{\text{mal}}, y_{\text{mal}})\}$
10. end for

Different types of data require different synthesis methods.

**Synthesizing images.** We assume no auxiliary knowledge for synthesizing images. The adversary can use any suitable GenData method: for example, generate pseudorandom images using the adversary’s choice of pseudorandom function (PRF) (e.g., HMAC [39]) or else create sparse images where only one pixel is filled with a (similarly generated) pseudorandom value.

We found the latter technique to be very effective in practice. GenData enumerates all pixels in an image and, for each pixel, creates a synthetic image where the corresponding pixel is set to the pseudorandom value while other pixels are set to zero. The same technique can be used with multiple pixels in each synthetic image.

**Synthesizing text.** We consider two scenarios for synthesizing text documents.

If the adversary knows the exact vocabulary of the training dataset, he can use this vocabulary as the auxiliary knowledge
in GenData. A simple deterministic implementation of GenData enumerates the tokens in the auxiliary vocabulary in a certain order. For example, GenData can enumerate all singleton tokens in lexicographic order, then all pairs of tokens in lexicographic order, and so on until the list is as long as the number of synthetic documents needed. Each list entry is then set to be a text in the augmented training dataset.

If the adversary does not know the exact vocabulary, he can collect frequently used words from some public corpus as the auxiliary vocabulary for generating synthetic documents. In this case, a deterministic implementation of GenData pseudorandomly (with a seed known to the adversary) samples words from the vocabulary until generating the desired number of documents.

To generate a document in this case, our simple synthesis algorithm samples a constant number of words (50, in our experiments) from the public vocabulary and joins them as a single document. The order of the words does not matter because the feature extraction step only cares whether a given word occurs in the document or not.

This synthesis algorithm may occasionally generate documents consisting only of words that do not occur in the model’s actual vocabulary. Such words will typically be ignored in the feature extraction phase, thus the resulting documents will have empty features. If the attacker does not know the model’s vocabulary, he cannot know if a particular synthetic document consists only of out-of-vocabulary words. This can potentially degrade both the test accuracy and decoding accuracy of the model.

In Section 6.7, we empirically measure the accuracy of the capacity-abuse attack with a public vocabulary.

Decoding memorized information. Because our synthesis methods for augmented data are deterministic, the adversary can replicate the synthesis process and query the trained model with the same synthetic inputs as were used during training. If the model is overfitted to these inputs, the labels returned by the model will be exactly the same labels that were associated with these inputs during training, i.e., the encoded secret bits.

If a model has sufficient capacity to achieve good accuracy and generalizability on its original training data and to memorize malicious training data, then acc(θ, Dmal) will be near perfect, leading to low error when extracting the sensitive data.

5.3 Why Capacity Abuse Works

Deep learning models have such a vast memorization capacity that they can essentially express any function to fit the data [75]. In our case, the model is fitted not just to the original training dataset but also to the synthetic data which is (in essence) randomly labeled. If the test accuracy on the original data is high, the model is accepted. If the training accuracy on the synthetic data is high, the adversary can extract information from the labels assigned to these inputs.

Critically, these two goals are not in conflict. Training on maliciously augmented datasets thus produces models that have high quality on their original training inputs yet leak information on the augmented inputs.

In the case of SVM and LR models, we focus on high-dimensional and sparse data (natural-language text). Our synthesis method also produces very sparse inputs. Empirically, the likelihood that a synthetic input lies on the wrong side of the hyperplane (classifier) becomes very small in this high-dimensional space.

6 EXPERIMENTS

We evaluate our attack methods on benchmark image and text datasets, using, respectively, gray-scale training images and ordered tokens as the secret to be memorized in the model.

For each dataset and task, we first train a benign model using a conventional training algorithm. We then train and evaluate a malicious model for each attack method. We assume that the malicious training algorithm has a hard-coded secret that can be used as the key for a pseudorandom function or encryption.

All ML models and attacks were implemented in Python 2.7 with Theano [70] and Lasagne [20]. The experiments were conducted on a machine with two 8-core Intel i7-5960X CPUs, 64 GB RAM, and three Nvidia TITAN X (Pascal) GPUs with 12 GB VRAM each.

6.1 Datasets and Tasks

Table 1 summarizes the datasets, models, and classification tasks we used in our experiments. We use as stand-ins for sensitive data several representative, publicly available image and text datasets.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>Data size</th>
<th>Num params</th>
<th>Test acc</th>
</tr>
</thead>
<tbody>
<tr>
<td>CIFAR10</td>
<td>50K</td>
<td>3072</td>
<td>1228M</td>
</tr>
<tr>
<td>LFW</td>
<td>10K</td>
<td>8742</td>
<td>692M</td>
</tr>
<tr>
<td>FaceScrub (G)</td>
<td>57K</td>
<td>7500</td>
<td>3444M</td>
</tr>
<tr>
<td>FaceScrub (F)</td>
<td>11K</td>
<td>130K</td>
<td>176M</td>
</tr>
<tr>
<td>News</td>
<td>25K</td>
<td>300K</td>
<td>265M</td>
</tr>
<tr>
<td>IMDB</td>
<td>50x50 RGB pixels</td>
<td>50x50 RGB pixels</td>
<td>50x50 RGB pixels</td>
</tr>
</tbody>
</table>

Table 1: Summary of datasets and models. n is the size of the training dataset, d is the number of input dimensions. RES stands for Residual Network, CNN for Convolutional Neural Network. For FaceScrub, we use the gender classification task (G) and face recognition task (F).
**20 Newsgroups** is a corpus of 20,000 documents classified into 20 categories [44]. We use 75% for training, 25% for testing.

**IMDB Movie Reviews** is a dataset of 50,000 reviews labeled with positive or negative sentiment [52]. The task is (binary) sentiment analysis. We use 50% for training, 50% for testing.

### 6.2 ML Models

**Convolutional Neural Networks.** Convolutional Neural Networks (CNN) [47] are composed of a series of convolution operations as building blocks which can extract spatial-invariant features. The filters in these convolution operations are the parameters to be learned. We use a 5-layer CNN for gender classification on the LFW dataset. The first three layers are convolution layers (32 filters in the first layer, 64 in the second, 128 in the third) followed by a max-pooling operation which reduces the size of convolved features by half. Each filter in the convolution layer is 3x3. The convolution output is connected to a fully-connected layer with 256 units. The latter layer connects to the output layer which predicts gender.

For the hyperparameters, we set the mini-batch size to be 128, learning rate to be 0.1, and use SGD with Nesterov Momentum for optimizing the loss function. We also use the $l_2$-norm as the regularizer with $\lambda$ set to $10^{-5}$. We set the number of epochs for training to 100. In epochs 40 and 60, we decrease the learning rate by a factor of 0.1 for better convergence. This configuration is inherited from the residual-network implementation in Lasagne.\(^1\)

**Residual Networks.** Residual networks (RES) [31] overcome the gradient vanishing problem when optimizing very deep CNNs by adding identity mappings from lower layers to high layers. These networks achieved state-of-the-art performance on many benchmark vision datasets in 2016.

We use a 34-layer residual network for CIFAR10 and FaceScrub. Although the network has fewer parameters than CNN, it is much deeper and can learn better representations of the input data. The hyperparameters are the same as for the CNN.

**Bag-of-Words and Linear Models.** For text datasets, we use a popular pipeline that extracts features using Bag-of-Words (BOW) and trains linear models. BOW maps each text document into a vector in $\mathbb{R}^{|V|}$ where $V$ is the vocabulary of tokens that appear in the corpus. Each dimension represents the count of that token in the document. The vectors are extremely sparse because only a few tokens from $V$ appear in any given document.

We then feed the BOW vectors into an SVM or LR model. For 20 Newsgroups, there are 20 categories and we apply the One-vs-All method to train 20 binary classifiers to predict whether a data point belongs to the corresponding class or not. We train linear models using AdaGrad [23], a variant of SGD with adaptive adjustment to the learning rate of each parameter. We set the mini-batch size to 128, learning rate to 0.1, and the number of epochs for training to 50 as AdaGrad converges very fast on these linear models.

### 6.3 Evaluation Metrics

Because we aim to encode secrets in a model while preserving its quality, we measure both the attacker’s decoding accuracy and the model’s classification accuracy on the test data for its primary task (accuracy on the training data is over 98% in all cases). Our attacks introduce minor stochasticity into training, thus accuracy of maliciously trained models occasionally exceeds that of conventionally trained models.

**Metrics for decoding images.** For images, we use mean absolute pixel error (MAPE). Given a decoded image $x'$ and the original image $x$ with $k$ pixels, MAPE is $\frac{1}{k} \sum_{i=1}^{k} |x_i - x'_i|$. Its range is $[0, 255]$, where 0 means the two images are identical and 255 means every pair of corresponding pixels has maximum mismatch.

**Metrics for decoding text.** For text, we use precision (percentage of tokens from the decoded document that appear in the original document) and recall (percentage of tokens from the original document that appear in the decoded document). To evaluate similarity between the decoded and original documents, we also measure their cosine similarity based on their feature vectors constructed from the BOW model with the training vocabulary.

### 6.4 LSB Encoding Attack

Table 2 summarizes the results for the LSB encoding attack. Here $f$ is the model used, $b$ is the maximum number of lower bits used beyond which accuracy drops significantly, $\delta$ is the difference with the baseline test accuracy.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>$f$</th>
<th>$b$</th>
<th>Encoded bits</th>
<th>Test acc ±$\delta$</th>
</tr>
</thead>
<tbody>
<tr>
<td>CIFAR10</td>
<td>RES</td>
<td>18</td>
<td>8.3M</td>
<td>89.75 ±0.14</td>
</tr>
<tr>
<td>LFW</td>
<td>CNN</td>
<td>22</td>
<td>17.6M</td>
<td>87.69 ±0.14</td>
</tr>
<tr>
<td>FaceScrub (G)</td>
<td>RES</td>
<td>20</td>
<td>9.2M</td>
<td>97.33 ±0.11</td>
</tr>
<tr>
<td>FaceScrub (F)</td>
<td>RES</td>
<td>18</td>
<td>8.3M</td>
<td>89.95 ±0.13</td>
</tr>
<tr>
<td>News</td>
<td>SVM</td>
<td>22</td>
<td>57.2M</td>
<td>80.60 ±0.02</td>
</tr>
<tr>
<td></td>
<td>LR</td>
<td></td>
<td></td>
<td>80.40 ±0.11</td>
</tr>
<tr>
<td>IMDB</td>
<td>SVM</td>
<td>22</td>
<td>6.6M</td>
<td>90.12 ±0.01</td>
</tr>
</tbody>
</table>

\(^1\)https://github.com/Lasagne/Recipes/blob/master/models/resnet50.py

![Figure 2: Test accuracy of the CIFAR10 model with different amounts of lower bits used for the LSB attack.](image-url)
model. The fourth column in Table 2 shows the number of bits we can use before test accuracy drops significantly.

Decoding. Decoding is always perfect because we use lossless compression and no errors are introduced during encoding. For the 20 Newsgroup model, the adversary can successfully extract about 57 Mb of compressed data, equivalent to 70% of the training dataset.

Test accuracy. In our implementation, each model parameter is a 32-bit floating-point number. Empirically, \( b \) under 20 does not decrease test accuracy on the primary task for most datasets. Binary classification on images (LFW, FaceScrub Gender) can endure more loss of precision. For multi-class tasks, test accuracy drops significantly when \( b \) exceeds 20 as shown for CIFAR10 in Figure 2.

6.5 Correlated Value Encoding Attack

Table 3 summarizes the results for this attack.

**Image encoding and decoding.** We correlate model parameters with the pixel intensity of gray-scale training images. The number of parameters limits the number of images that can be encoded in this way: 455 for CIFAR10, 200 for FaceScrub, 300 for LFW.

We decode images by mapping the correlated parameters back to pixel space (if correlation is perfect, the parameters are simply linearly transformed images). To do so given a sequence of parameters, we map the minimum parameter to 0, maximum to 255, and other parameters to the corresponding pixel value using min-max scaling. We obtain an approximate original image after transformation if the correlation is positive and an approximate inverted original image if the correlation is negative.

After the transformation, we measure the mean absolute pixel error (MAPE) for different choices of \( \lambda_c \), which controls the level of correlation. We find that to recover reasonable images, \( \lambda_c \) needs to be over 1.0 for all tasks. For a fixed \( \lambda_c \), errors are smaller for binary classification than for multi-class tasks. Examples of reconstructed images are shown in Figure 3 for the FaceScrub dataset.

**Text encoding and decoding.** To encode, we generate a pseudo-random, \( d' \)-dimensional vector of 32-bit floating point numbers for each token in the vocabulary of the training corpus. Then, given a training document, we use the pseudorandom vectors for the first 100 tokens in that document as the secret to correlate with the model parameters. We set \( d' \) to 20. Encoding one document thus requires up to 2000 parameters, allowing us to encode around 1300 documents for 20 Newsgroups and 150 for IMDB.

To decode, we first reproduce the pseudorandom vectors for each token used during training. For each consecutive part of the parameters that should match a token, we decode by searching for a token whose corresponding vector is best correlated with the parameters. We set a threshold value \( \tau \) and if the correlation value is above \( \tau \), we accept this token and reject otherwise.

Table 3 shows the decoding results for different \( \tau \). As expected, larger \( \tau \) increases precision and reduces recall. Empirically, \( \tau = 0.85 \) yields high-quality decoded documents (see examples in Table 5).
which in turn reduces test accuracy by more than 1%. Table 4 summarizes the results of the sign encoding attack. We construct a bit representation of the raw pixels of the image encoding and decoding. We map a pixel value as in the sign encoding attack, but for a binary classifier this requires \( \lambda = 50 \) for FaceScrub and 5 images for LFW.

To reconstruct pixels, we assemble the bits represented in the parameter signs. With \( \lambda = 50 \), MAPE is small for all datasets. For gender classification on FaceScrub, the error can be smaller than 1, i.e., reconstruction is nearly perfect.

Test encoding and decoding. We construct a bit representation for each token using its index in the vocabulary. The number of bits per token is \( \lceil \log_2(V) \rceil \), which is 17 for both 20 Newsgroups and IMDB. We encode the first 100 words in each document and thus need a total of 1,700 parameter signs per document. We encode 1530 documents for 20 Newsgroups and 180 for IMDB in this way.

Many tasks, when \( \lambda = 50 \), new FaceScrub face recognition degrades by 2.6%, while the CIFAR10 model with \( \lambda = 50 \) still generalizes well. For 20 Newsgroups, test accuracy changes by less than 0.5% for all values of \( \lambda _s \). For IMDB, accuracy decreases by around 0.8% to 1.2% for both SVM and LR.

6.6 Sign Encoding Attack

Table 4 summarizes the results of the sign encoding attack.

Image encoding and decoding. As mentioned in Section 4.3, the sign encoding attack may not encode all bits correctly. Therefore, instead of the encrypted, compressed binaries that we used for LSB encoding, we use the bit representation of the raw pixels of the gray-scale training images as the string to be encoded. Each pixel is an 8-bit unsigned integer. The encoding capacity is thus \( \frac{1}{8} \) of the correlated value encoding attack. We can encode 56 images for CIFAR10, 25 images for FaceScrub and 37 images for LFW.

To reconstruct pixels, we assemble the bits represented in the parameter signs. With \( \lambda = 50 \), MAPE is small for all datasets. For gender classification on FaceScrub, the error can be smaller than 1, i.e., reconstruction is nearly perfect.

Test encoding and decoding. We construct a bit representation for each token using its index in the vocabulary. The number of bits per token is \( \lceil \log_2(V) \rceil \), which is 17 for both 20 Newsgroups and IMDB. We encode the first 100 words in each document and thus need a total of 1,700 parameter signs per document. We encode 1530 documents for 20 Newsgroups and 180 for IMDB in this way.

To reconstruct tokens, we use the signs of 17 consecutive parameters as the index into the vocabulary. Setting \( \lambda _s \geq 5 \) yields good results for most tasks (see examples in Table 5). Decoding is less accurate than for the correlated value encoding attack. The reason is that signs need to be encoded almost perfectly to recover high-quality documents; even if 1 bit out of 17 is wrong, our decoding produces a completely different token. More sophisticated, error-correcting decoding techniques can be applied here, but we leave this to future work.

Test accuracy. This attack does not significantly affect the test accuracy of binary classification models on image datasets. For LFW and CIFAR10, test accuracy occasionally increases. For multi-class tasks, when \( \lambda = 50 \), new FaceScrub face recognition degrades by 2.6%, while the CIFAR10 model with \( \lambda = 50 \) still generalizes well.

6.7 Capacity Abuse Attack

Table 6 summarizes the results.

Image encoding and decoding. We could use the same technique as in the sign encoding attack, but for a binary classifier this requires 8 synthetic inputs per each pixel. Instead, we encode an approximate pixel value in 4 bits. We map a pixel value \( p \in \{0, \ldots, 255\} \) to \( p' \in \{0, \ldots, 15\} \) (e.g., map 0-15 in \( p \) to 0 in \( p' \)) and use 4 synthetic data points to encode \( p' \). Another possibility (not evaluated in this paper) would be to encode every other pixel and recover the image by interpolating the missing pixels.

We evaluate two settings of \( m \), the number of synthesized data points. For LFW, we can encode 3 images for \( m = 34K \) and 5 images for \( m = 58K \). For FaceScrub gender classification, we can encode 11 images for \( m = 110K \) and 17 images for \( m = 170K \). While these numbers may appear low, this attack works in a black-box setting against a binary classifier, where the adversary aims to recover information from a single output bit. Moreover, for many tasks (e.g., medical image analysis) recovering even a single training input constitutes a serious privacy breach. Finally, if the attacker’s goal is to recover not the raw images but some other information about

Figure 3: Decoded examples from all attacks applied to models trained on the FaceScrub gender classification task. First row is the ground truth. Second row is the correlated value encoding attack (\( \lambda_c = 1.0 \), MAPE = 15.0). Third row is the sign encoding attack (\( \lambda_s = 10.0 \), MAPE = 2.51). Fourth row is the capacity abuse attack (\( m = 110K \), MAPE = 10.8).
the training dataset (e.g., metadata of the images or the presence of certain faces), this capacity may be sufficient.

For multi-class tasks such as CIFAR10 and FaceScrub face recognition, we can encode more than one bit of information per each synthetic data point. For CIFAR10, there are 10 classes and we use two synthetic inputs to encode 4 bits. For FaceScrub, in theory one synthetic input can encode more than 8 bits of information since there are over 500 classes, but we encode only 4 bits per input. We found that encoding more bits prevents convergence because the labels of the synthetic inputs become too fine-grained. We evaluate two settings of \( m \). For CIFAR10, we can encode 25 images with \( m = 49K \) and 50 with \( m = 98K \). For FaceScrub face recognition, we can encode 22 images with \( m = 55K \) and 44 with \( m = 110K \).

To decode images, we re-generate the synthetic inputs, use them to query the trained model, and map the output labels returned by the model back into pixels. We measure the MAPE between the original images and decoded approximate 4-bit-pixel images. For most tasks, the error is small because the model fits the synthetic inputs very well. Although the approximate pixels are less precise, the reconstructed images are still recognizable—see the fourth row of Figure 3.

**Text encoding and decoding.** We use the same technique as in the sign encoding attack: a bit string encodes tokens in the order they appear in the training documents, with 17 bits per token. Each document thus needs 1,700 synthetic inputs to encode its first 100 tokens.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>( f )</th>
<th>( m )</th>
<th>( \frac{m}{n} )</th>
<th>Test Acc</th>
<th>Decode MAPE</th>
</tr>
</thead>
<tbody>
<tr>
<td>CIFAR10 (G)</td>
<td>RES</td>
<td>49K</td>
<td>0.98</td>
<td>92.21−0.69</td>
<td>7.60</td>
</tr>
<tr>
<td></td>
<td>CNN</td>
<td>34K</td>
<td>3.4</td>
<td>88.03+0.20</td>
<td>18.6</td>
</tr>
<tr>
<td></td>
<td>RES</td>
<td>110K</td>
<td>2.0</td>
<td>97.08−0.36</td>
<td>10.8</td>
</tr>
<tr>
<td>FaceScrub (G)</td>
<td>RES</td>
<td>55K</td>
<td>1.0</td>
<td>87.46−2.62</td>
<td>7.62</td>
</tr>
<tr>
<td>FaceScrub (F)</td>
<td>RES</td>
<td>110K</td>
<td>2.0</td>
<td>86.36−3.72</td>
<td>8.11</td>
</tr>
</tbody>
</table>

Table 5: Decoded text examples from all attacks applied to LR models trained on the IMDB dataset.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>( f )</th>
<th>( m )</th>
<th>( \frac{m}{n} )</th>
<th>Test Acc</th>
<th>Decode</th>
</tr>
</thead>
<tbody>
<tr>
<td>NEWS</td>
<td>SVM</td>
<td>11K</td>
<td>1.0</td>
<td>80.53−0.07</td>
<td>1.0</td>
</tr>
<tr>
<td></td>
<td>LR</td>
<td>11K</td>
<td>1.0</td>
<td>80.06−0.45</td>
<td>0.98</td>
</tr>
<tr>
<td></td>
<td>SVM</td>
<td>24K</td>
<td>0.95</td>
<td>89.82−0.31</td>
<td>0.90</td>
</tr>
<tr>
<td></td>
<td>LR</td>
<td>24K</td>
<td>0.95</td>
<td>89.90−0.58</td>
<td>0.87</td>
</tr>
</tbody>
</table>

Table 6: Results of the capacity abuse attack. Here \( m \) is the number of synthesized inputs and \( \frac{m}{n} \) is the ratio of synthesized data to training data.

<table>
<thead>
<tr>
<th>Dataset</th>
<th>( f )</th>
<th>( m )</th>
<th>( \frac{m}{n} )</th>
<th>Test Acc</th>
<th>Decode</th>
</tr>
</thead>
<tbody>
<tr>
<td>NEWS</td>
<td>SVM</td>
<td>11K</td>
<td>1.0</td>
<td>79.31−1.27</td>
<td>0.94</td>
</tr>
<tr>
<td></td>
<td>LR</td>
<td>11K</td>
<td>1.0</td>
<td>79.85−0.28</td>
<td>0.94</td>
</tr>
<tr>
<td></td>
<td>SVM</td>
<td>24K</td>
<td>0.95</td>
<td>89.44−0.69</td>
<td>0.87</td>
</tr>
<tr>
<td></td>
<td>LR</td>
<td>24K</td>
<td>0.95</td>
<td>89.92−0.56</td>
<td>0.79</td>
</tr>
</tbody>
</table>

Table 7: Results of the capacity abuse attack on text datasets using a public auxiliary vocabulary.

20 Newsgroups models have 20 classes and we use the first 16 to encode 4 bits of information. Binary IMDB models can only encode one bit per synthetic input. We evaluate two settings for \( m \). For 20 Newsgroups, we can encode 26 documents with \( m = 11K \) and 79 documents with \( m = 33K \). For IMDB, we can encode 14 documents with \( m = 24K \) and 44 documents with \( m = 75K \).

With this attack, the decoded documents have high quality (see Table 5). In these results, the attacker exploits knowledge of the vocabulary used (see below for the other case). For 20 Newsgroups, recovery is almost perfect for both SVM and LR. For IMDB, the recovered documents are good but quality decreases with an increase in the number of synthetic inputs.
We use each consecutive 18 bits as index into the public vocabulary we observed. Smaller drops in test accuracy for both SVM and LR when we set $m$ that is three times the original dataset results in less than 0.6% drop in test accuracy on 20 Newsgroups. On IMDB, test accuracy drops less than 0.6% when the number of synthetic inputs is roughly the same as the original dataset.

**Using a public auxiliary vocabulary.** The synthetic images used for the capacity-abuse are pseudorandomly generated and do not require the attacker to have any prior knowledge about the images in the actual training dataset. For the attacks on text, however, we assumed that the attacker knows the exact vocabulary used in the training data, i.e., the list of words from which all training documents are drawn (see Section 5.2).

We now relax this assumption and assume that the attacker uses an auxiliary vocabulary collected from publicly available corpuses: Brown Corpus, Gutenberg Corpus [43], Rotten Tomatoes [62], and a word list from Tesseract OCR.

Obviously, this public auxiliary vocabulary requires no prior knowledge of the model’s actual vocabulary. It contains 67K tokens and needs 18 bits to encode each token. We set the target to be the first 100 tokens that appear in each document and discard the tokens that are not in the public vocabulary. Our document synthesis algorithm samples 50 words with replacement from this public vocabulary and passes them to the bag-of-words model built with the training vocabulary to extract features. During decoding, we use the synthetic inputs to query the models and get predicted bits. We use each consecutive 18 bits as index into the public vocabulary to reconstruct the target text.

Table 7 shows the results of the attack with this public vocabulary. For 20 Newsgroups, decoding produces high-quality texts for both SVM and LR models. Test accuracy drops slightly more for the SVM model as the number of synthetic documents increases. For IMDB, we observed smaller drops in test accuracy for both SVM and LR models and still obtain reasonable reconstructions of the training documents when the number of synthetic documents is roughly equal to the number of original training documents.

**Memorization capacity and model size.** To further investigate the relationship between the number of model parameters and the model’s capacity for maliciously memorizing “extra” information about its training dataset, we compared CNNs with different numbers of filters in the last convolution layer: 16, 32, 48, . . . , 112. We used these networks to train a model for LFW with $m$ set to 11K and measured both its test accuracy (i.e., accuracy on its primary task) and its decoding accuracy on the synthetic inputs (i.e., accuracy of the malicious task).

Figure 4 shows the results. Test accuracy is similar for smaller and bigger models. However, the encoding capacity of the smaller models, i.e., their test accuracy on the synthetic data, is much lower and thus results in less accurate decoding. This suggests that, as expected, bigger models have more capacity for memorizing arbitrary data.

**Visualization of capacity abuse.** Figure 5 visualizes the features learned by a CIFAR10 model that has been trained on its original training images augmented with maliciously generated synthetic images. The points are sampled from the last-layer outputs of Residual Networks on the training and synthetic data and then projected to 2D using t-SNE [53].

The plot clearly shows that the learned features are almost linearly separable across the classes of the training data and the classes of the synthetic data. The classes of the synthetic data correspond to the primary task, i.e., different types of objects in the image. The classes of the synthetic data correspond to the malicious task, i.e., given a specific synthetic image, the class encodes a secret about the training images. This demonstrates that the model has learned both its primary task and the malicious task well.

### 7 COUNTERMEASURES

Detecting that a training algorithm is attempting to memorize sensitive data within the model is not straightforward because, as we show in this paper, there are many techniques and places for encoding this information: directly in the model parameters, by applying a malicious regularizer, or by augmenting the training data with specially crafted inputs. Manual inspection of the code may not detect malicious intent, given that many of these approaches are similar to standard ML techniques.

An interesting way to mitigate the LSB attack is to turn it against itself. The attack relies on the observation that lower bits of model parameters essentially don’t matter for model accuracy. Therefore, a client can replace the lower bits of the parameters with random noise. This will destroy any information potentially encoded in these bits without any impact on the model’s performance.

Maliciously trained models may exhibit anomalous parameter distributions. Figure 6 compares the distribution of parameters in a conventionally trained model, which has the shape of a zero-mean Gaussian, to maliciously trained models. As expected, parameters generated by the correlated value encoding attack are distributed...
very differently. Parameters generated by the sign encoding attack are more centered at zero, which is similar to the effect of conventional $l_1$-norm regularization (which encourages sparsity in the parameters). To detect these anomalies, the data owner must have a prior understanding of what a “normal” parameter distribution looks like. This suggests that deploying this kind of anomaly detection may be challenging.

Parameters generated by the capacity-abuse attack are not visibly different. This is expected because training works exactly as before, only the dataset is augmented with additional inputs.

8 RELATED WORK

**Privacy threats in ML.** No prior work considered malicious learning algorithms informing about the training dataset.

Ateniese et al. [4] show how an attacker can use access to an ML model to infer a predicate of the training data, e.g., whether a voice recognition system was trained only with Indian English speakers.

Fredrikson et al. [26] explore model inversion: given a model $f_\theta$ that makes a prediction $y$ given some hidden feature vector $x_1, \ldots, x_n$, they use the ground-truth label $\tilde{y}$ and a subset of $x_1, \ldots, x_n$ to infer the remaining, unknown features. Model inversion operates in the same manner whether the feature vector $x_1, \ldots, x_n$ is in the training dataset or not, but empirically performs better for training set points due to overfitting. Subsequent model inversion attacks [25] show how, given access to a face recognition model, to construct a representative of a certain output class (a recognizable face when each class corresponds to a single person).

In contrast to the above techniques, our objective is to extract specific inputs that belong to the training dataset which was used to create the model.

Homer et al. [32] developed a technique for determining, given published summary statistics about a genome-wide association study, whether a specific known genome was used in the study. This is known as the membership inference problem. Subsequent work extended this work to published noisy statistics [24] and MicroRNA-based studies [5].

Membership inference attacks against supervised ML models were studied by Shokri et al. [68]. They use black-box access to a model $f_\theta$ to determine whether a given labeled feature vector $(x, y)$ was a member of the training set used to produce $\theta$. Their attacks work best when $f_\theta$ has low generalizability, i.e., if the accuracy for the training inputs is much better than for inputs from outside the training dataset.

By contrast, we study how a malicious training algorithm can intentionally create a model that leaks information about its training dataset. The difference between membership inference and our problem is akin to the difference between side channels and covert channels. Our threat model is more generous to the adversary, thus our attacks extract substantially more information about the training data than any prior work. Another important difference is we aim to create models that generalize well yet leak information.

**Evasion and poisoning.** Evasion attacks seek to craft inputs that will be misclassified by a ML model. They were first explored in the context of spam detection [28, 50, 51]. More recent work investigated evasion in other settings such as computer vision—see a survey by Papernot et al. [63]. Our work focuses on the confidentiality of training data rather than evasion, but future work may investigate how malicious ML providers can intentionally create models that facilitate evasion.

Poisoning attacks [9, 18, 38, 57, 65] insert malicious data points into the training dataset to make the resulting model easier to evade. This technique is similar in spirit to the malicious data augmentation in our capacity-abuse attack (Section 5). Our goal is not evasion, however, but forcing the model to leak its training data.

**Secure ML environments.** Starting with [49], there has been much research on using secure multi-party computation to enable several parties to create a joint model on their separate datasets, e.g. [11, 16, 22]. A protocol for distributed, privacy-preserving deep learning was proposed in [67]. Abadi et al. [1] describe how to train differentially private deep learning models. Systems using trusted hardware such as SGX protect training data while training on an untrusted service [21, 61, 66]. In all of these works, the training algorithm is public and agreed upon, and our attacks would work only if users are tricked into using a malicious algorithm.

CQSTR [74] explicitly targets situations in which the training algorithm may not be entirely trustworthy. Our results show that in such settings a malicious training algorithm can covertly exfiltrate significant amounts of data, even if the output is constrained to be an accurate and usable model.

Privacy-preserving classification protocols seek to prevent disclosure of the user’s input features to the model owner as well as disclosure of the model to the user [12]. Using such a system would prevent our white-box attacks, but not black-box attacks.

**ML model capacity and compression.** Our capacity-abuse attack takes advantage of the fact that many models (especially deep neural networks) have huge memorization capacity. Zhang et al. [75] showed that modern ML models can achieve (near) 100% training accuracy on datasets with randomized labels or even randomized
features. They argue that this undermines previous interpretations of generalization bounds based on training accuracy.

Our capacity-abuse attack augments the training data with (essentially) randomized data and relies on the resulting low training error to extract information from the model. Crucially, we do this while simultaneously training the model to achieve good testing accuracy on its primary, non-adversarial task.

Our LSB attack directly takes advantages of the large number and unnecessarily high precision of model parameters. Several papers investigated how to compress models [13, 15, 29]. An interesting topic of future work is how to use these techniques as a countermeasure to malicious training algorithms.

9 CONCLUSION

We demonstrated that malicious machine learning (ML) algorithms can create models that satisfy the standard quality metrics of accuracy and generalizability while leaking a significant amount of information about their training datasets, even if the adversary has only black-box access to the model.

ML cannot be applied blindly to sensitive data, especially if the model-training code is provided by another party. Data holders cannot afford to be ignorant of the inner workings of ML systems if they intend to make the resulting models available to other users, directly or indirectly. Whenever they use somebody else’s ML system or employ ML as a service (even if the service promises not to observe the operation of its algorithms), they should demand to see the code and understand what it is doing.

In general, we need “the principle of least privilege” for machine learning. ML training frameworks should ensure that the model captures only as much about its training dataset as it needs for its designated task and nothing more. How to formalize this principle, how to develop practical training methods that satisfy it, and how to certify these methods are interesting open topics for future research.

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REFERENCES
