# **Simulating RF MEMS**

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### **Collaborators**

Faculty	Grad students
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J. Demmel (Math/CS)	D. Garmire (CS)
S. Govindjee (CEE)	T. Koyama (CEE)
R. Howe (EE)	R. Kamalian (ME)
	J. Nie (Math)
	S. Bhave (EE)

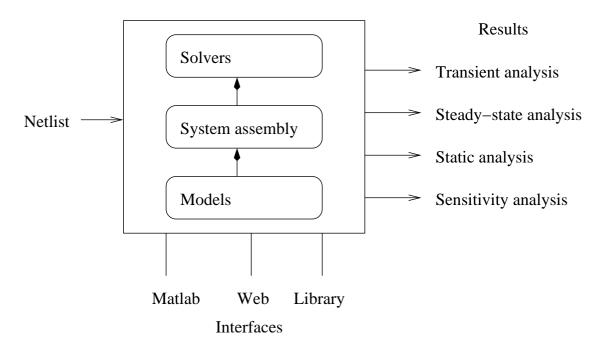
#### **MEMS Basics**

- Micro-electro-mechanical systems
  - Chemical, fluid, thermal, optical (MECFTOMS?)
- Applications:
  - Sensors (inertial, chemical, pressure)
  - Ink jet printers, biolab chips
  - RF devices
- Use IC fabrication technology
- Large surface area / volume ratio
- Still mostly classical (vs. nanosystems)

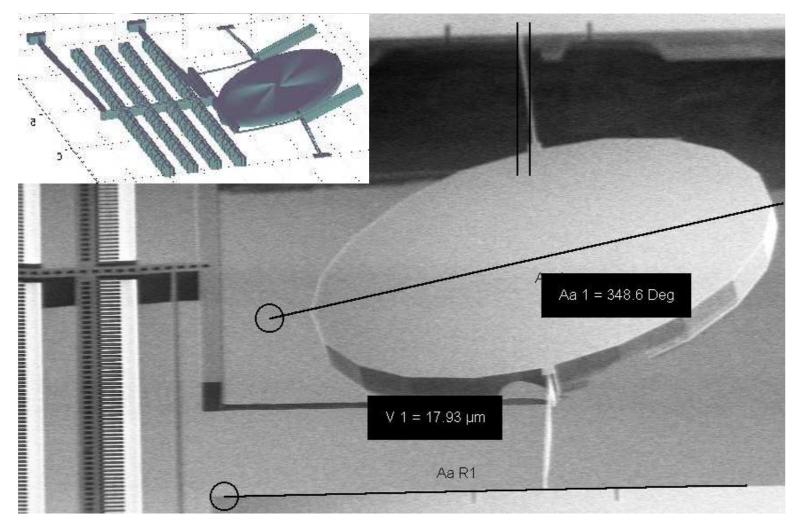
#### **SUGAR**

Goal: "Be SPICE to the MEMS world"

- Fast enough for early design stages
- Simple enough to attract users
- Support design, analysis, optimization, synthesis
- Verify models by comparison to measurement

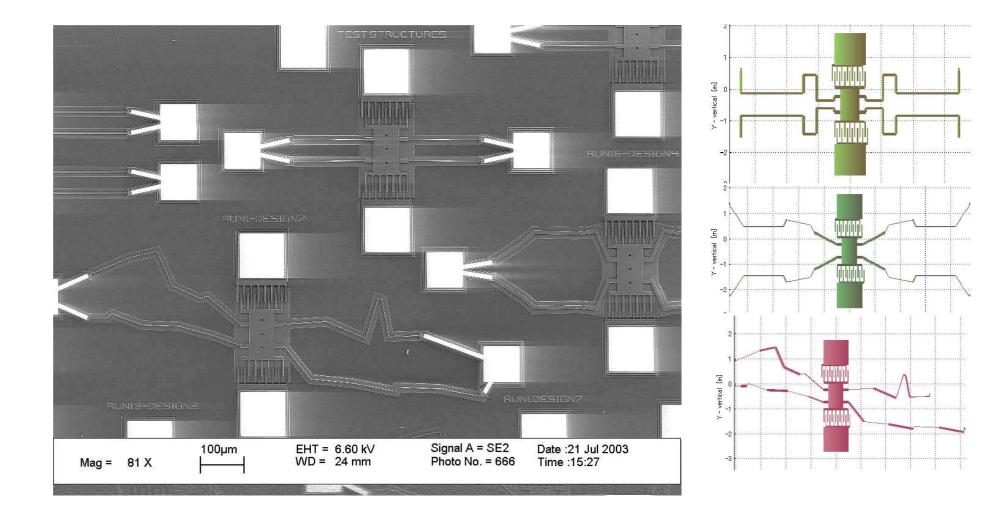


### **SUGAR:** Analysis of a micromirror

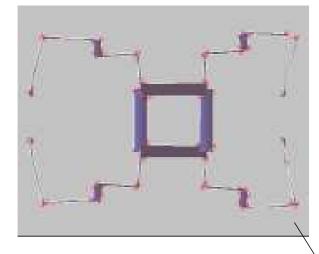


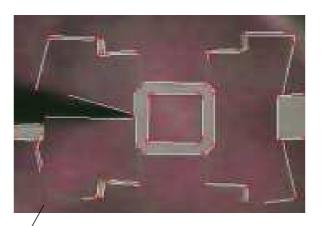
(Mirror design by M. Last)

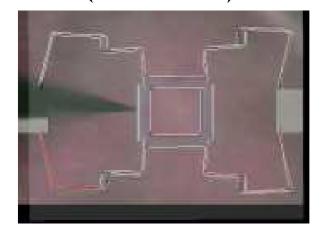
## **SUGAR: Design synthesis**



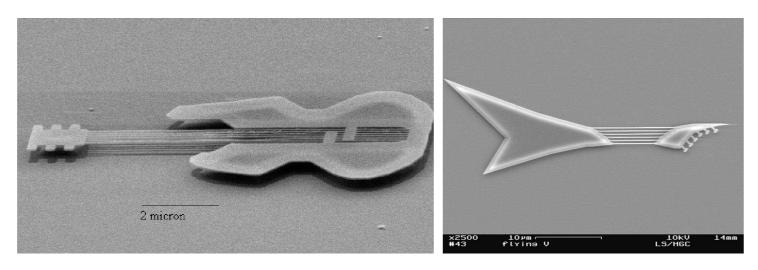
## **SUGAR: Comparison to measurement**







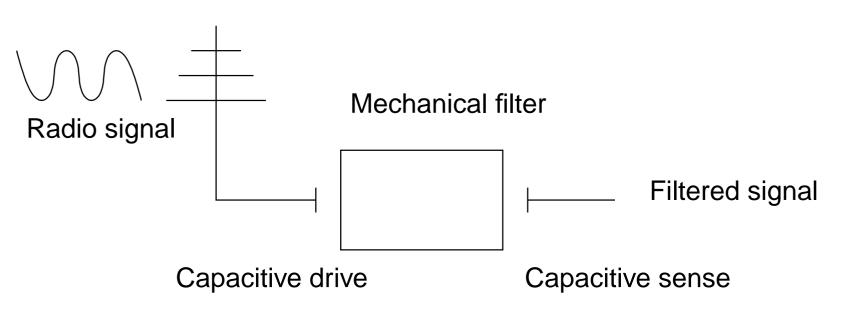
## Why RF resonators?



Microguitars from Cornell University (1997 and 2003)

- Frequency references
- Sensing elements
- Filter elements
- Neural networks
- Really high-pitch guitars

### **Micromechanical filters**



- Mechanical high-frequency (high MHz-GHz) filter
- Saves power and cost over electronic filters
- Advantage over piezo-actuated quartz SAW filters
  - Integrated into chip
  - Low power

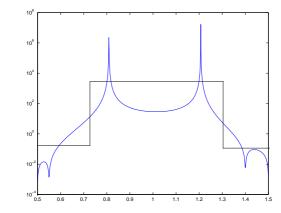
## **Governing equations**

Time domain:

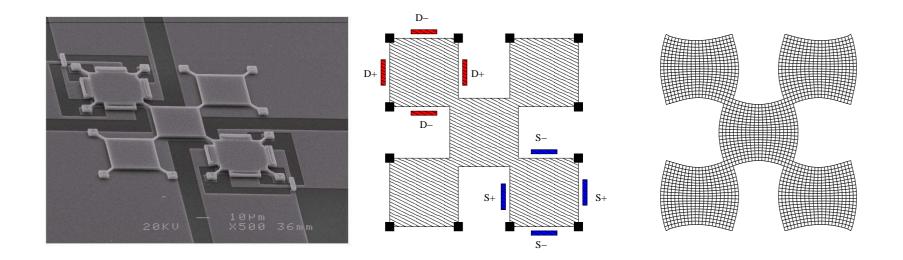
$$Mu'' + Cu' + Ku = P\phi$$
$$y = V^T u$$

Frequency domain:

$$H(\omega) = V^T (-\omega^2 M + i\omega C + K)^{-1} P$$
$$\hat{y} = H\hat{\phi}$$

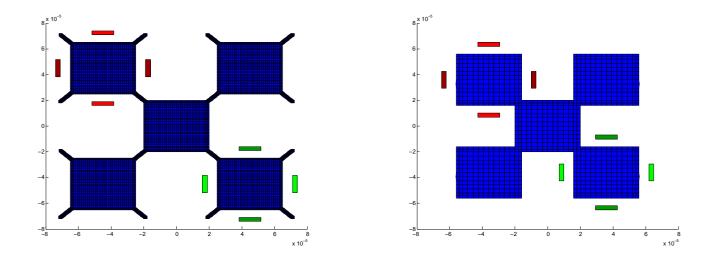


# First proposed design: Checkerboard



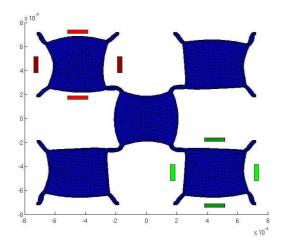
- Array of loosely coupled resonators
- Anchored at outside corners
- Excited at northwest corner
- Sensed at southeast corner
- Surfaces move only a few nanometers

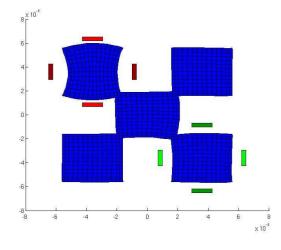
# **Design questions**



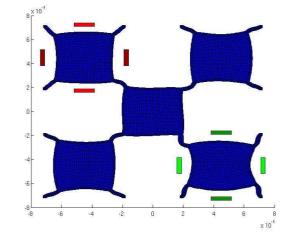
- Where should drive and sense be placed?
- How should the individual resonators be connected?
- How should the system be anchored?
- How many components? What topology?

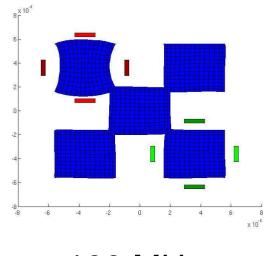
### **Checkerboard response**





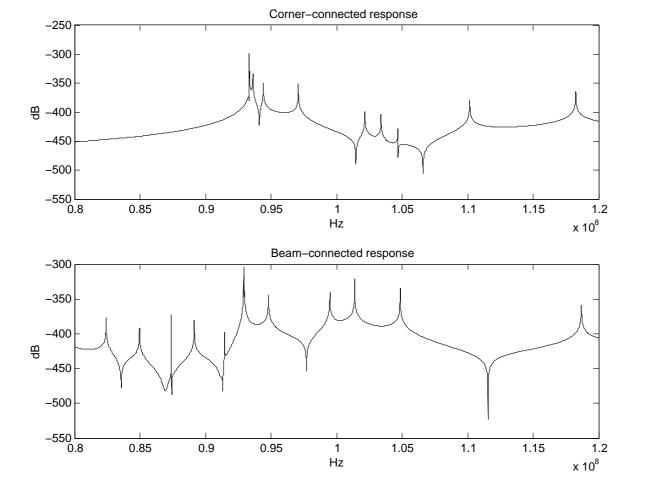
95 MHz





100 MHz

### **Checkerboard response**



Corner-connected details Beam-connected details

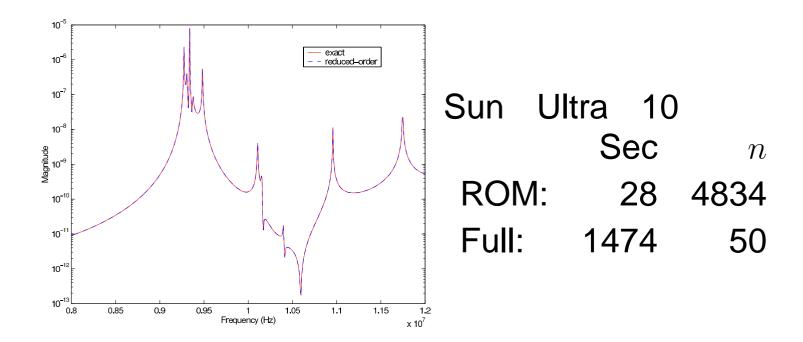
## **Current questions**

- How do we model damping?
- How do we compute frequency response quickly?
- How do we track dependence on geometry?
- How do we optimize designs?

## **Energy loss and** Q

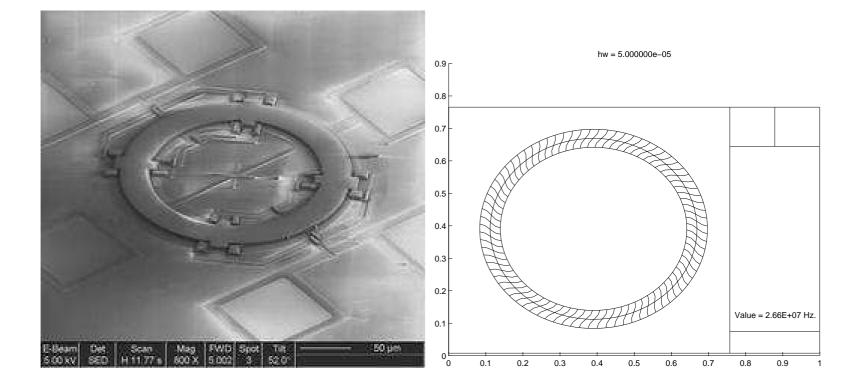
- **•** Goal: strong output signal and high Q
- Challenge: Model details of energy loss
  - Anchor loss
  - Thermoelastic damping
  - Akheiser damping
  - Air damping
- How are losses affected by fabrication errors (e.g. anchor misalignment)?

### **Model reduction**



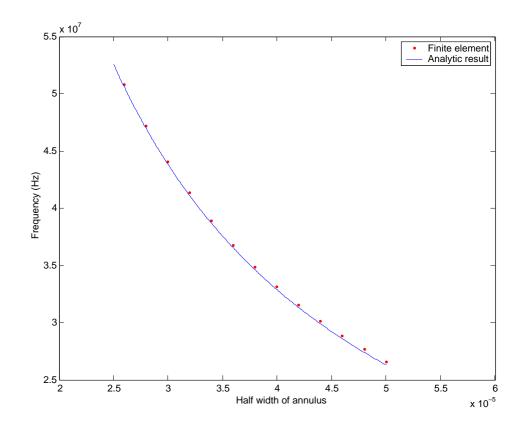
- Project onto an unusual Krylov subspace
- Preserve second order system structure
- Plan to use substructuring

## **Mode tracking: Shear ring resonator**



- Ring is driven in a shearing motion
- Can couple ring to other resonators
- How do we track the desired mode?

### **Mode tracking: Results**



- Predictor-corrector iteration
- Convergence criteria, step control based on  $|q(s_k)^T q(s_{k+1})|$

## **Transfer function optimization**

- Choose geometry to make a good bandpass filter
- What is a "good bandpass filter?"
  - $|H(\omega)|$  is big on  $[\omega_l, \omega_r]$
  - $|H(\omega)|$  is tiny outside this interval
- How do we optimize?
  - Overton's gradient sampling method
  - Use Byers-Boyd-Balikrishnan algorithm for distance to instability to minimize  $|H(\omega)|$  on  $[\omega_l, \omega_r]$
  - Small Hamiltonian eigenproblem (with ROM)

### Conclusions

RF MEMS are an interesting source of problems

- Understanding the physics
- Applying numerical tools

http://bsac.berkeley.edu/cadtools/sugar/sugar/
http://www.cs.berkeley.edu/~dbindel/feapmex.html