

# The Emerging Intersection of Social and Technological Networks

Jon Kleinberg

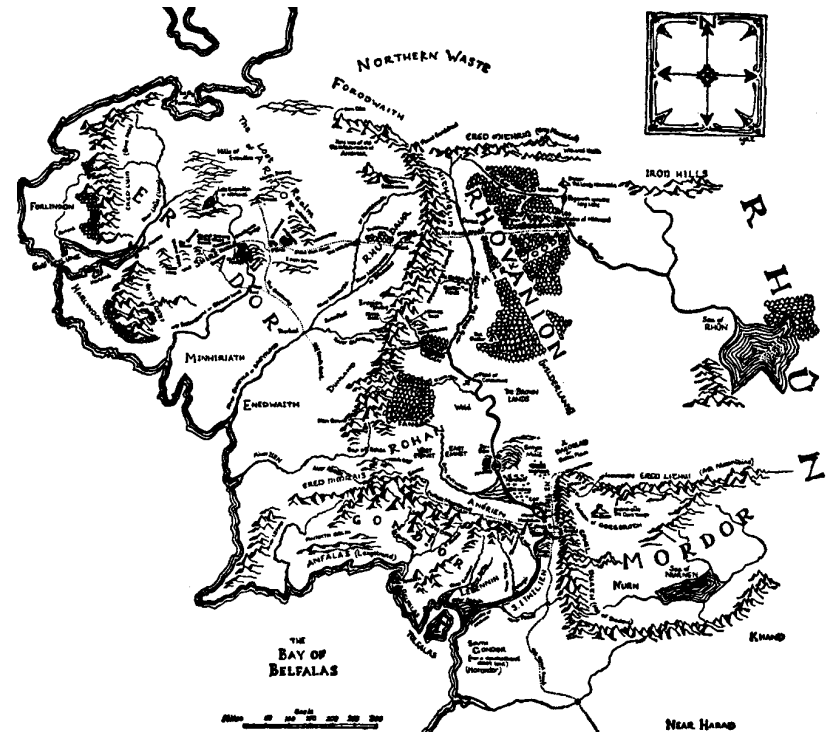
Cornell University



# Networks as Phenomena

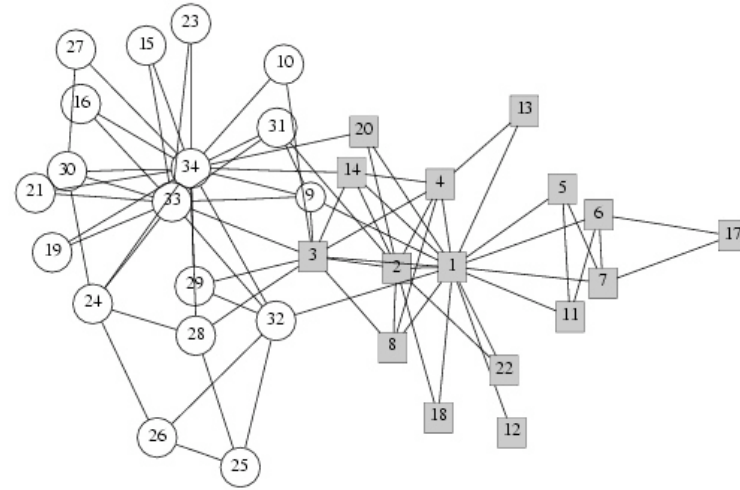
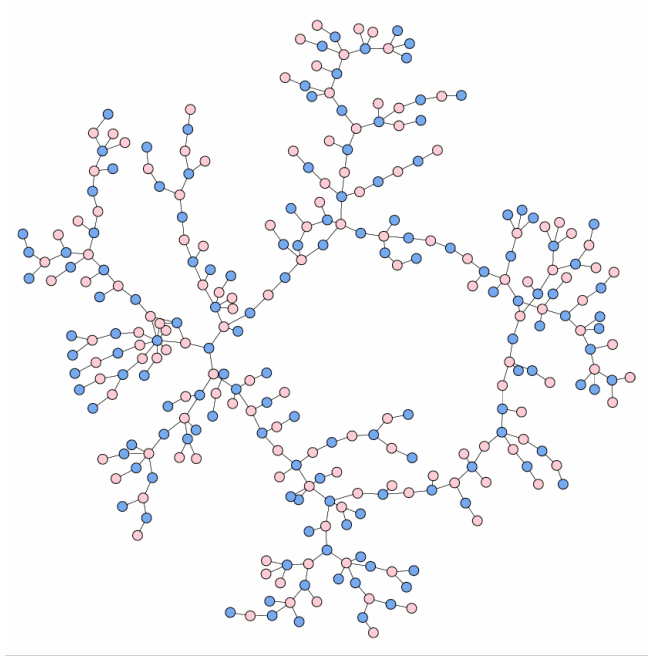
The emergence of 'cyberspace' and the World Wide Web is like the discovery of a new continent.

– Jim Gray,  
1998 Turing Award address



- Complex networks as phenomena, not just designed artifacts.
- What recurring patterns emerge, why are they there, and what are the consequences for computing and information systems?

# Social and Technological Networks



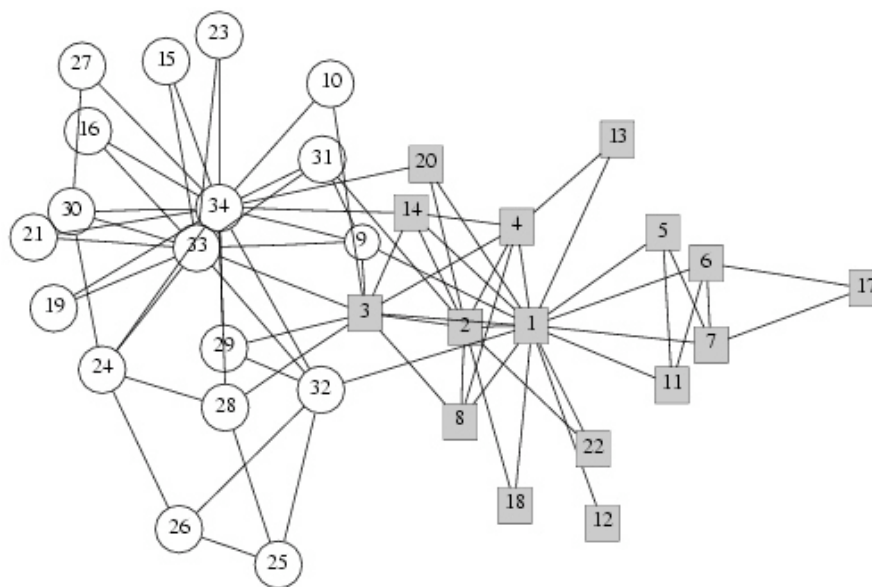
Social networks: friendships, contacts, collaboration, influence, organizational structure, economic institutions.

- Social and technological networks are intertwined:  
Web content, blogging, e-mail/IM, MySpace/Facebook/...
- New technologies change our patterns of social interaction.
- Collecting social data at unprecedented scale and resolution.

# Rich Social Network Data

Traditional obstacle:  
Can only choose 2 of 3.

- Large-scale
- Realistic
- Completely mapped



Two lines of research, looking for a meeting point.

- Social scientists engaged in detailed study of small datasets, concerned with social outcomes.
- Computer scientists discovering properties of massive network datasets that were invisible at smaller scales.

# Modeling Complex Networks

We want Kepler's Laws of Motion for the Web.  
– Mike Steuerwalt,  
NSF KDI Workshop, 1998



Opportunity for deeper understanding of information networks and social processes, informed by theoretical models and rich data.

- Mathematical / algorithmic models form the vocabulary for expressing complex social-science questions on complex network data.
- Payoffs from the introduction of an algorithmic perspective into the social sciences.

# Overview

Plan for the talk: two illustrations of this theme.

- (1) Small-world networks and decentralized search
  - Stylized models expose basic patterns.
  - Identifying the patterns in large-scale data.
- (2) A problem that is less well understood at a large scale: diffusion and cascading behavior in social networks
  - The way in which new practices, ideas, and behaviors spread through social networks like epidemics.
  - Models from discrete probability, data from on-line communities, open questions in relating them.
- (3) Some further reflections on social interaction data.
  - Modeling individuals vs. modeling populations

# Small-World Networks

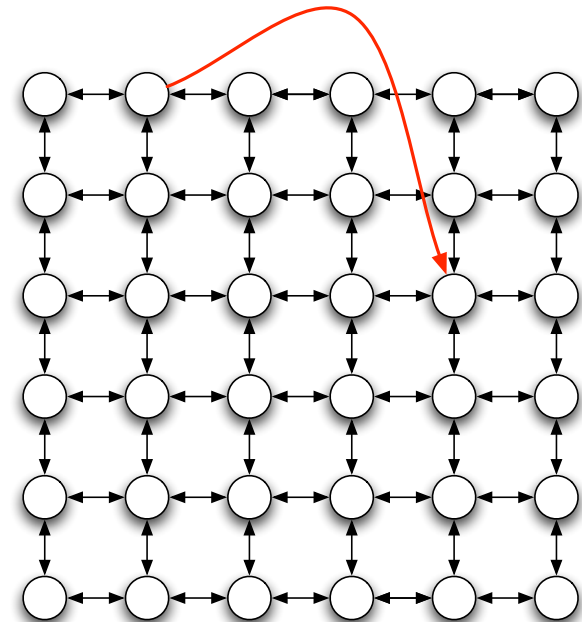
## Milgram's small-world experiment (1967)

Choose a target in Boston, starters in Nebraska.

A letter begins at each starter, must be passed between personal acquaintances until target is reached.

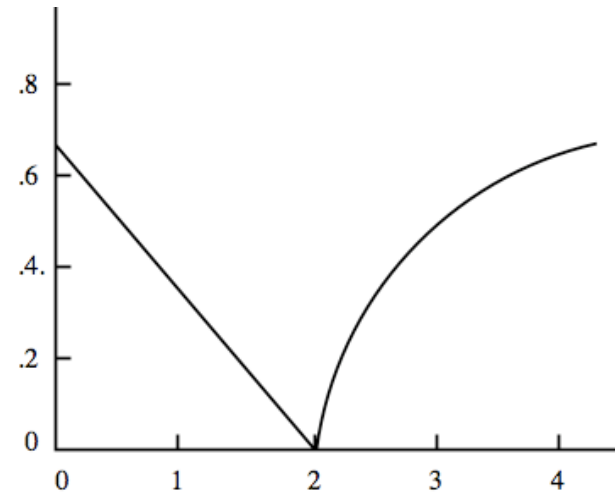
Six steps on average  $\longrightarrow$  six degrees of separation.

- Routing in a (social) network:  
When is local information sufficient? [Kleinberg 2000]
- Variation on network model of Watts and Strogatz [1998].
- Add edges to lattice:  $u$  links to  $v$  with probability  $d(u, v)^{-\alpha}$ .



# Small-World Models

- Optimal exponent  $\alpha = 2$ : yields routing time  $\sim c \log^2 n$ .
- All other exponents yield  $\sim n^\varepsilon$  for some  $\varepsilon > 0$ .

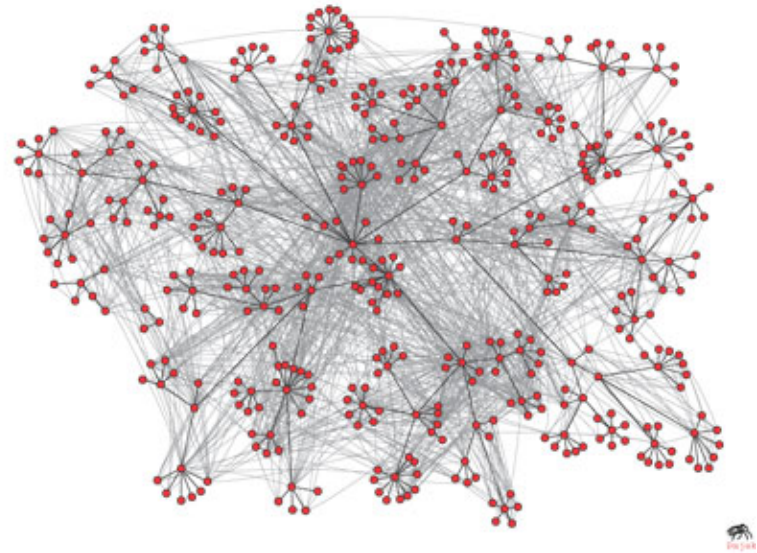


- Diameter at  $\alpha = 2$  is  $O(\log n)$ ; better routing via lookahead
  - [Fraigniaud-Gavoille-Paul '04, Lebhar-Schabanel '04, Manku-Naor-Wieder '04, Martel-Nguyen '04]
- Connections to long-range percolation in statistical physics
  - [Benjamini-Berger '01, Coppersmith-Gamarnik-Sviridenko '02, Biskup '04, Berger '06]
- Generalizations to random networks on different “scaffolds”:
  - Trees, set systems [Kleinberg '01, Watts-Dodds-Newman '02]
  - Low tree-width, excl. minor [Fraigniaud '05, Abraham-Gavoille]
  - Doubling metrics [Slivkins '05, Fraigniaud-Lebhar-Lotker '06]



# Social Network Data

- [Adamic-Adar 2003]: social network on 436 HP Labs researchers.
- Joined pairs who exchanged  $\geq 6$  e-mails (each way).



- Compared to “group-based” model [Kleinberg 2001]
  - Probability of link  $(v, w)$  prop. to  $g(v, w)^{-\alpha}$ , where  $g(v, w)$  is size of smallest group containing  $v$  and  $w$ .
  - $\alpha = 1$  gives optimal search performance.
- In HP Labs, groups defined by sub-trees of hierarchy.
- Links scaled as  $g^{-3/4}$ .

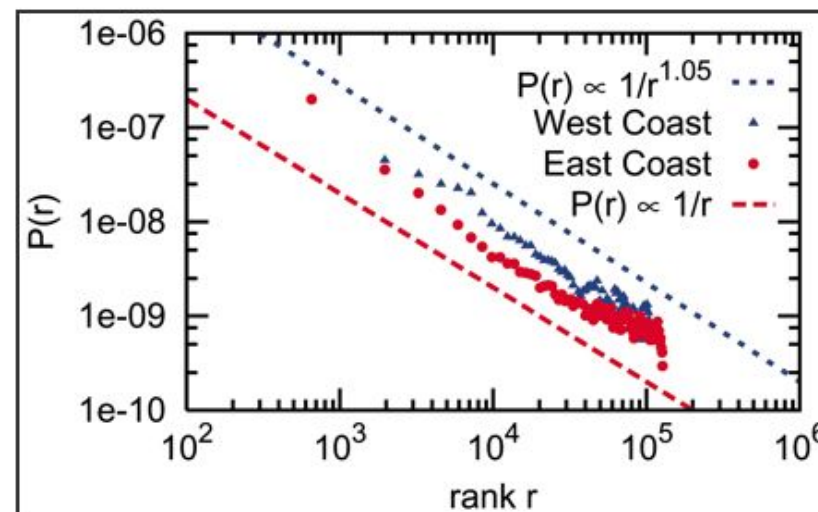
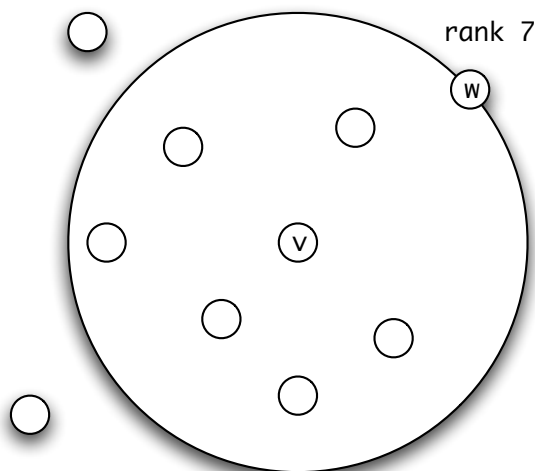
# Geographic Data: LiveJournal



Liben-Nowell, Kumar, Novak, Raghavan, Tomkins (2005) studied LiveJournal, an on-line blogging community with friendship links.

- Large-scale social network with geographical embedding:
  - 500,000 members with U.S. Zip codes, 4 million links.
- Analyzed how friendship probability decreases with distance.
- Difficulty: non-uniform population density makes simple lattice models hard to apply.

# LiveJournal: Rank-Based Friendship



Rank-based friendship: rank of  $w$  with respect to  $v$  is number of people  $x$  such that  $d(v, x) < d(v, w)$ .

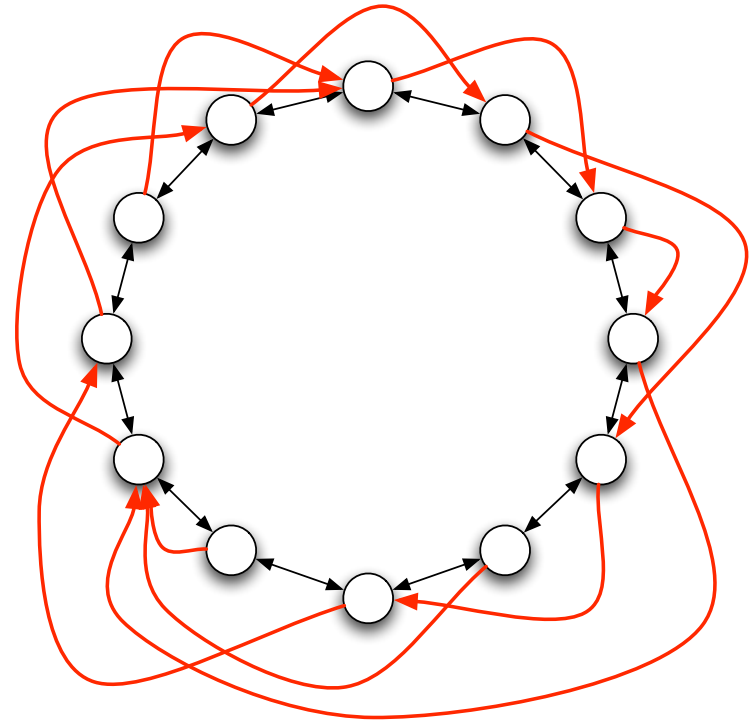
- Decentralized search with (essentially) arbitrary population density, when link probability proportional to  $\text{rank}^{-\beta}$ .
- (LKNRT'05): Efficient routing when  $\beta = 1$ , i.e.  $1/\text{rank}$ .
- Generalization of lattice result (diff. from set systems).

**Punchline: LiveJournal friendships approximate  $1/\text{rank}$ .**

# Open Question: Network Evolution

What causes a network to evolve toward searchability?

- A proposal by Sandberg and Clarke 2006, based on their work on Freenet:

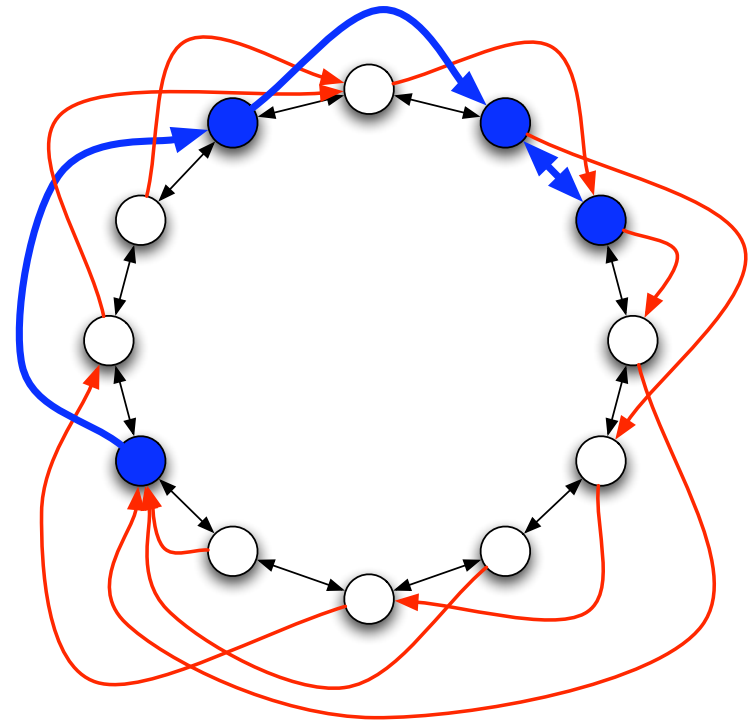


- $n$  nodes on a ring, each with neighbor links and a long link.
- At each time  $j = 1, 2, 3, \dots$ , choose random start  $s$ , target  $t$ , and perform greedy routing from  $s$  to  $t$ .
- Each node on resulting path updates long-range link to point to  $t$ , independently with (small) probability  $p$ .

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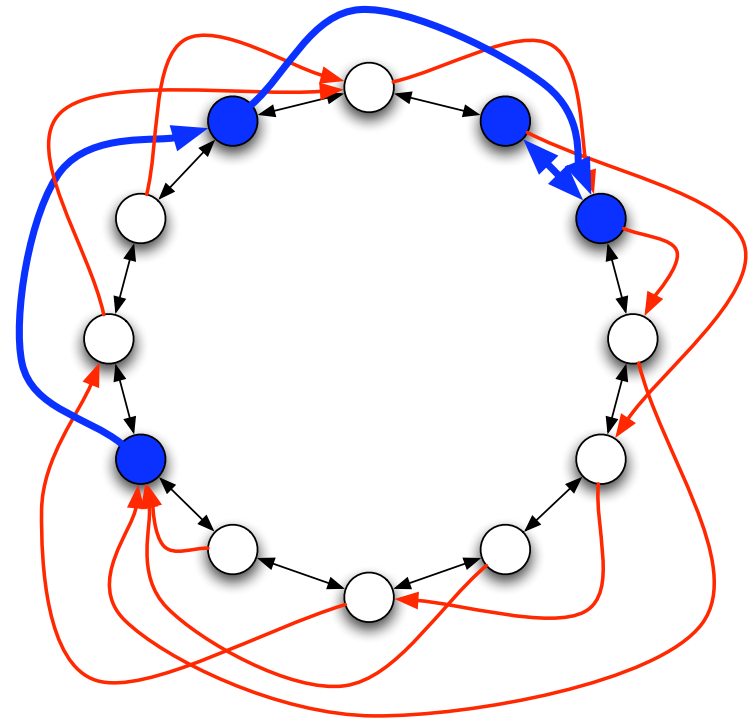


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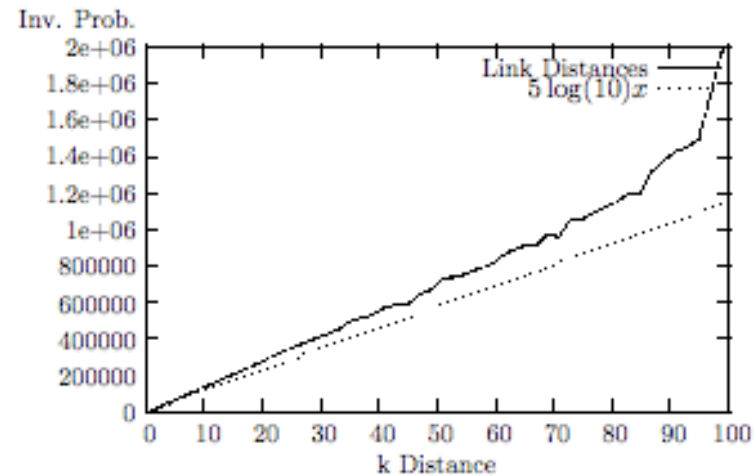
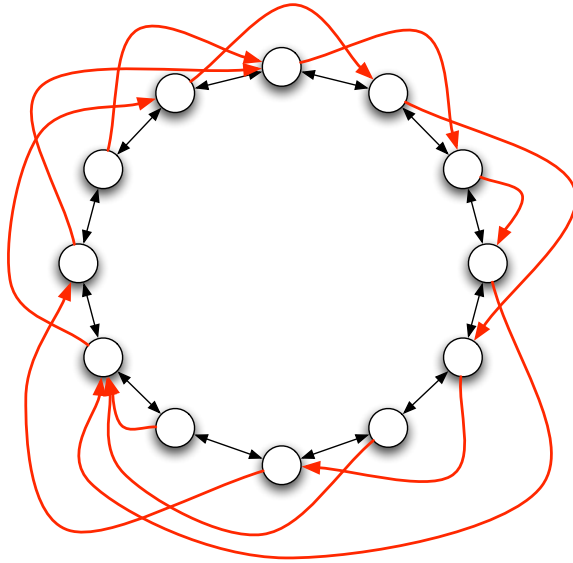
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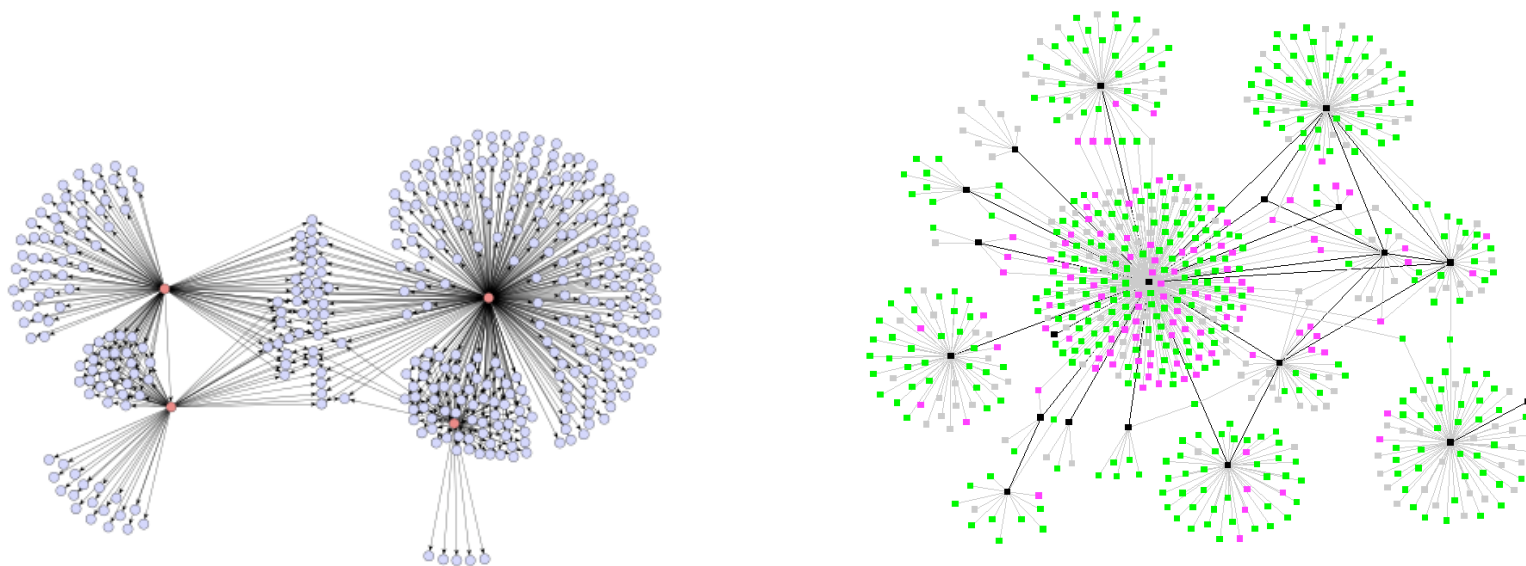


This defines a Markov chain on labeled graphs.

Conjecture [Sandberg-Clarke 2006]:

- At stationarity, distribution of distances spanned by long-range links is (close to) theoretical optimum for search.
- At stationarity, expected length of searches is polylogarithmic.
- Conjectures are supported by simulation.

# Diffusion in Social Networks



So far: focused search in a social network.

Now switch to diffusion, another fundamental social process:  
Behaviors that cascade from node to node like an epidemic.

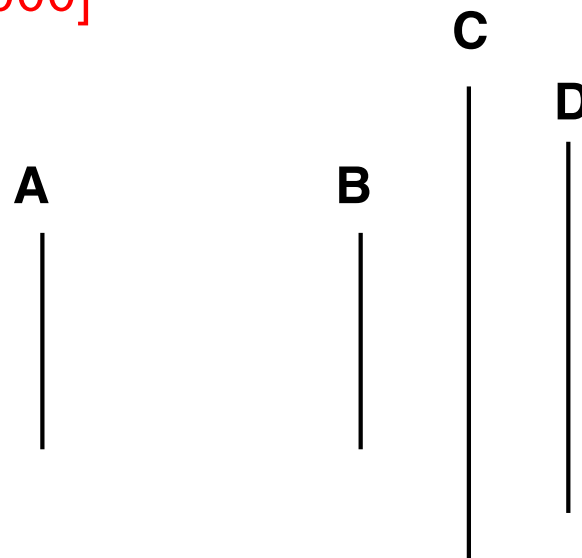
- News, opinions, rumors, fads, urban legends, ...
- Word-of-mouth effects in marketing, rise of new products.
- Changes in social priorities: smoking, recycling, ...
- Saturation news coverage; topic diffusion among bloggers.
- Localized collective action: riots, walkouts



# Empirical Studies of Diffusion

Experimental and theoretical studies of diffusion have a long history in the social sciences

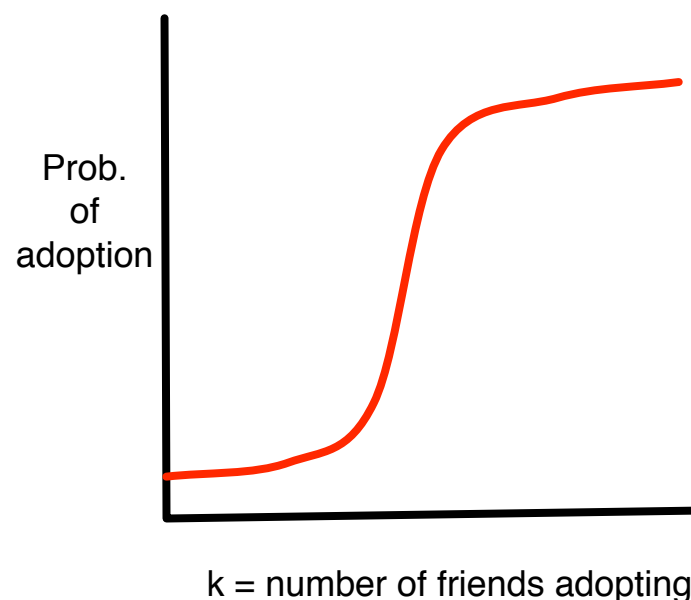
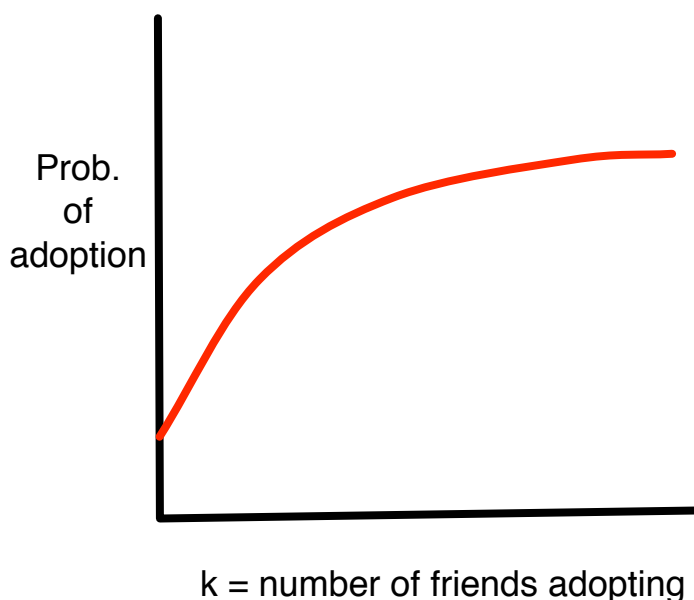
- Spread of new agricultural and medical practices [Coleman et al 1966]
- Media influence and two-stage flow [Lazarsfeld et al 1944]
- Modeling diffusion as a cascading sequence of strategy updates in a networked coordination game [Blume 1993, Ellison 1993, Young 1998, Morris 2000]
- Psychological effect of others' opinions. E.g.: Which line is closest in length to A? [Asch 1958]



# Diffusion Curves

Basis for models: Probability of adopting new behavior depends on number of friends who have adopted.

- Bass 1969; Granovetter 1978; Schelling 1978



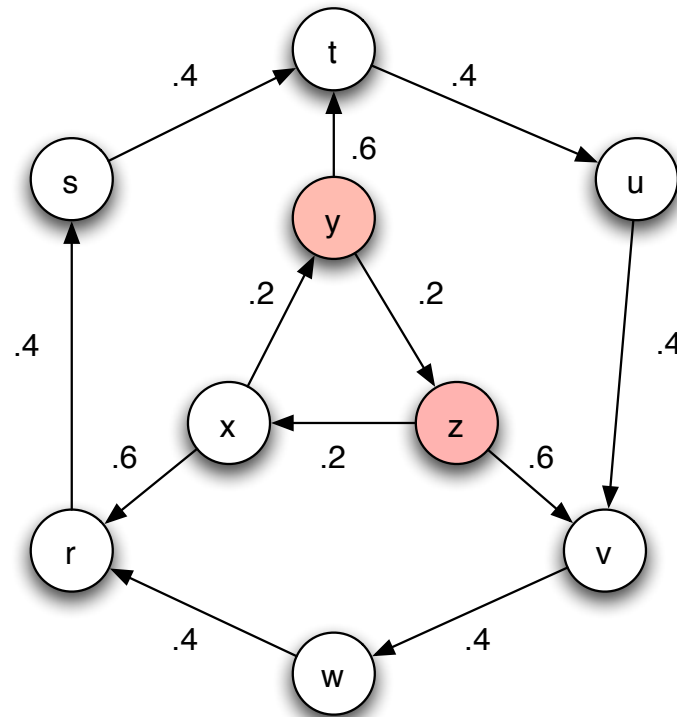
Build models for contact processes based on local behavior.

Key issue: qualitative shape of the diffusion curves.

- Diminishing returns? Critical mass?

# A Simple Model: Independent Contagion

- Initially some nodes are active.
- Each edge  $(v, w)$  has probability  $p_{vw}$ .

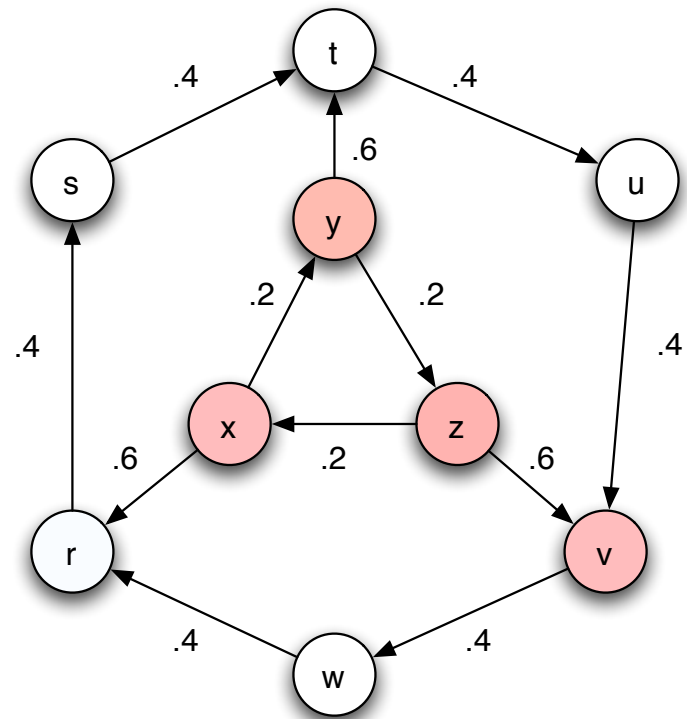


- $v$  becomes active: chance to activate  $w$  with probab.  $p_{vw}$ .
- Activations spread through network.
- Let  $S$  = initial active set,  $f(S)$  = exp. size of final active set.

Node don't "deactivate," though this is an easy modification.

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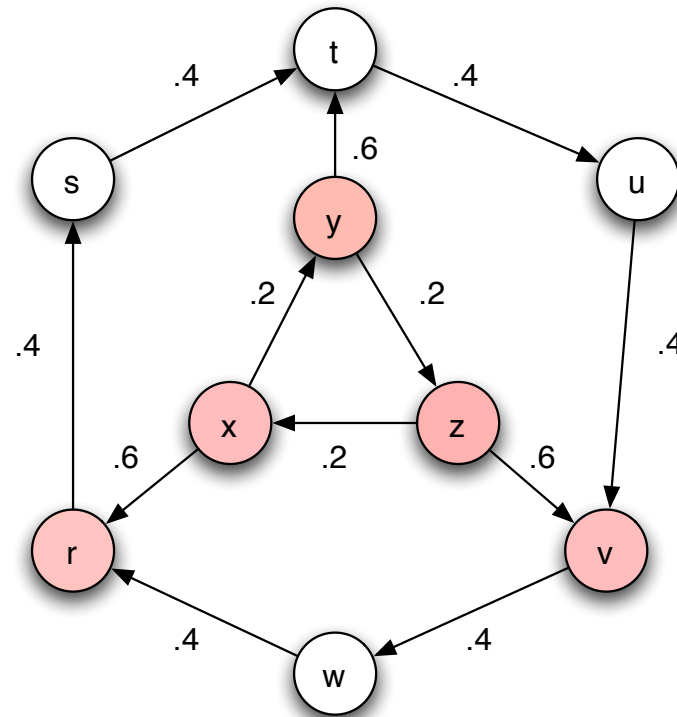


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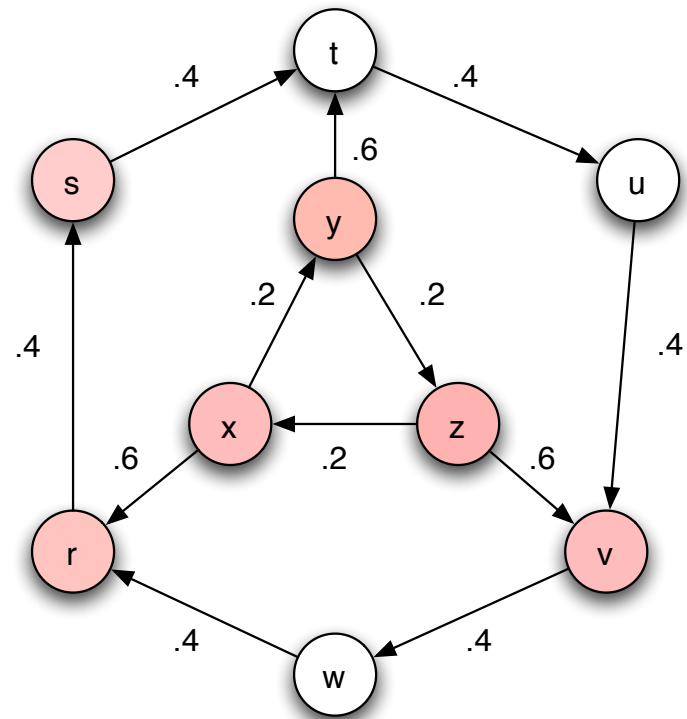


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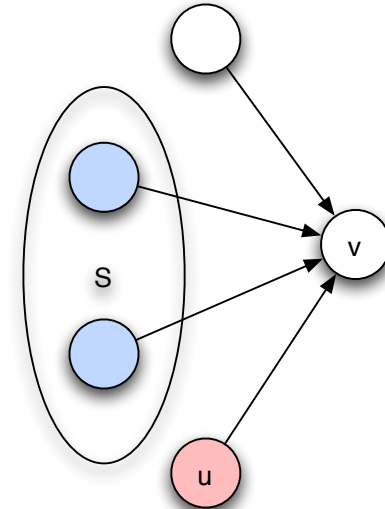
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# A General Contagion Model

Kempe-Kleinberg-Tardos 2003,

Dodds-Watts 2004:

- When  $u$  tries to influence  $v$ : success based on set of nodes  $S$  that already tried and failed.
- Success functions  $p_v(u, S)$ .

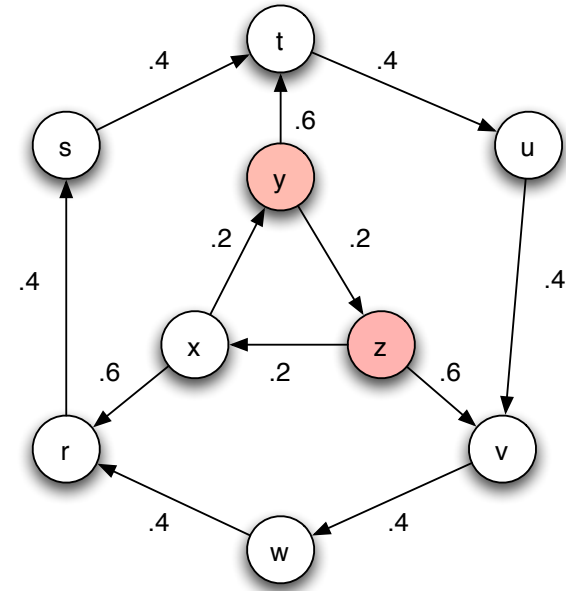


- Independent contagion:  $p_v(u, S) = p_{uv}$ .
- Threshold:  $p_v(u, S) = 1$  if  $|S| = k$ ; else  $p_v(u, S) = 0$ .
- Diminishing returns:  $p_v(u, S) \geq p_v(u, T)$  if  $S \subseteq T$ .

# The Most Influential Subset

Most influential set of size  $k$ : the  $k$  nodes producing largest expected cascade size if activated.

[Domingos-Richardson 2001]



As a discrete optimization problem:

$$\max_{S \text{ of size } k} f(S).$$

NP-hard and highly inapproximable.

- Inapproximability proof relies on critical mass.
- With diminishing returns: constant-factor approximation [Kempe-Kleinberg-Tardos 2005]



# An Approximation Result

Diminishing returns:  $p_v(u, S) \geq p_v(u, T)$  if  $S \subseteq T$ .

- Hill-climbing: repeatedly select maximum marginal gain.
- Performance guarantee: within  $(1 - \frac{1}{e}) \sim 63\%$  of optimal [Kempe-Kleinberg-Tardos 2005].
- Analysis: diminishing returns at individual nodes implies diminishing returns at a “global” level.
  - Cascade size  $f(S)$  grows slower and slower as  $S$  grows.  
 $f$  is submodular: if  $S \subseteq T$  then

$$f(S \cup \{v\}) - f(S) \geq f(T \cup \{v\}) - f(T).$$

- Can then use results of Nemhauser-Wolsey-Fisher 1978 on approximate maximization of submodular functions.
- Open: For how general a model is  $f(S)$  submodular, or at least well-approximable?

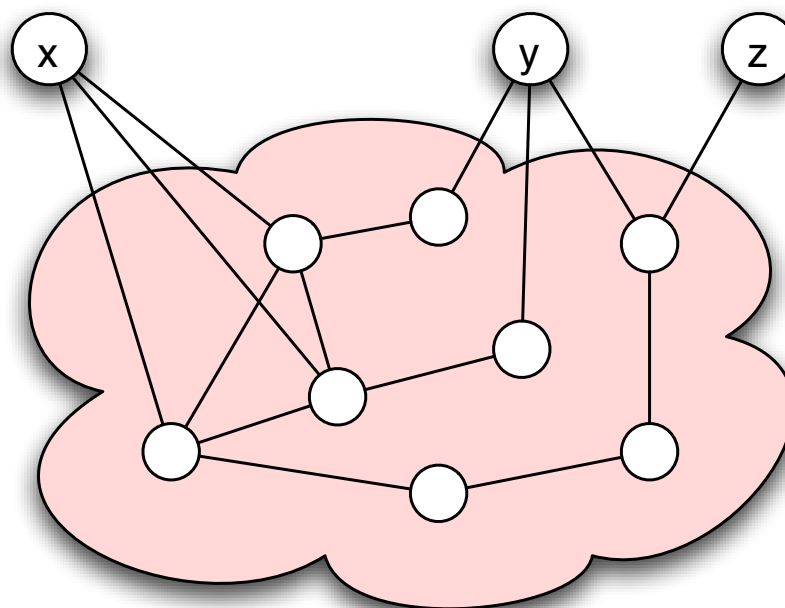
# Empirical Analysis of Diffusion Curves

What do real diffusion curves look like?

- Challenge: large datasets where diffusion can be observed.
- Need social network links and behaviors that spread.

Backstrom-Huttenlocher-Kleinberg-Lan, 2006:

- Use social networks where people belong to explicitly defined groups.
- Each group defines a behavior that diffuses.
- Probability of joining, based on friends?



# Networks with Explicit Groups

## LiveJournal

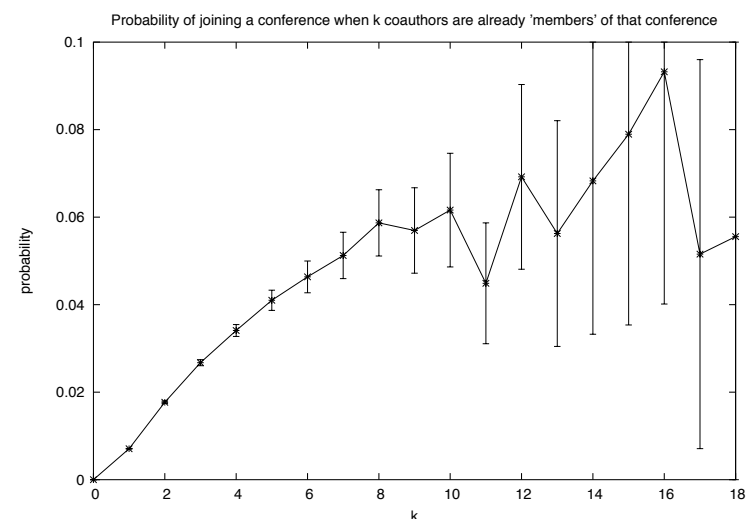
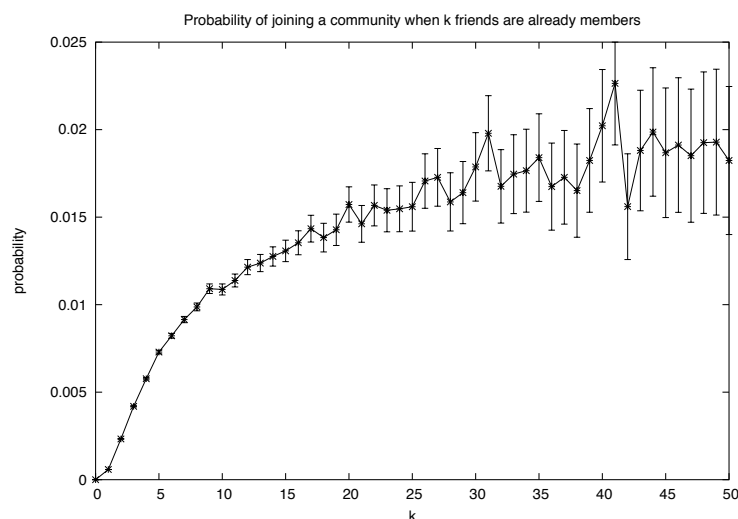
- On-line blogging community with friendship links and user-defined groups.
- Over a million users update content each month.
- Over 250,000 groups to join.

## DBLP

- Database of CS papers: co-author links and conferences.
- 100,000 authors; 2000 conferences.
- You “join” a conference by publishing a paper there.

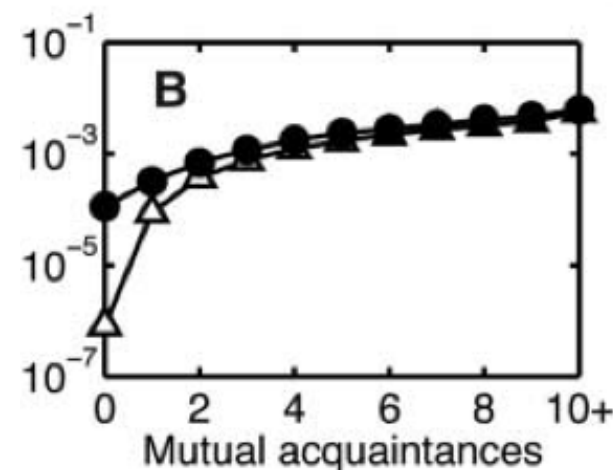
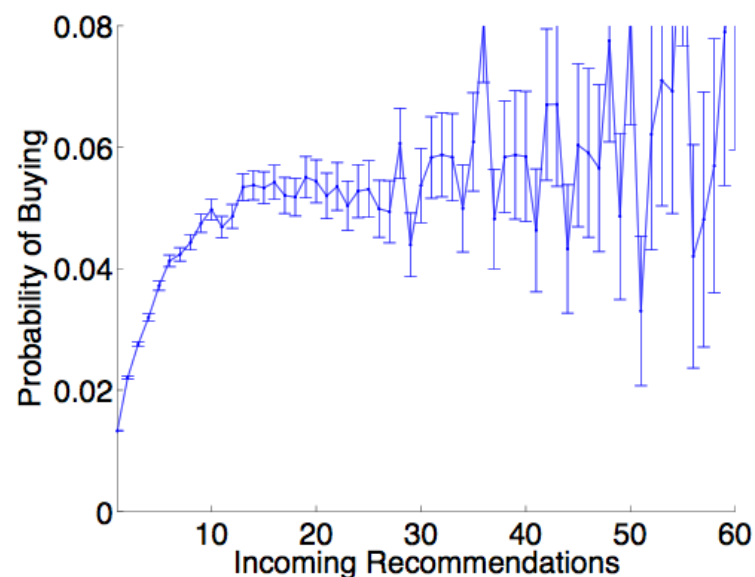
What do the diffusion curves look like in these two settings?

# LiveJournal and DBLP Diffusion



- Mainly diminishing returns.
- But both curves turn upward for  $k = 0, 1, 2$ .
- LiveJournal curve particularly smooth; fits  $f(x) = \epsilon \log x$ .  
Roughly half billion pairs  $(u, C)$  where user  $u$  is one step from community  $C$ .

# Recommendation and Email Diffusion



Leskovec-Adamic-Huberman, 2006

- Recommendation program at large on-line retailer.
- Prob. of purchase as function of # of recommendations.

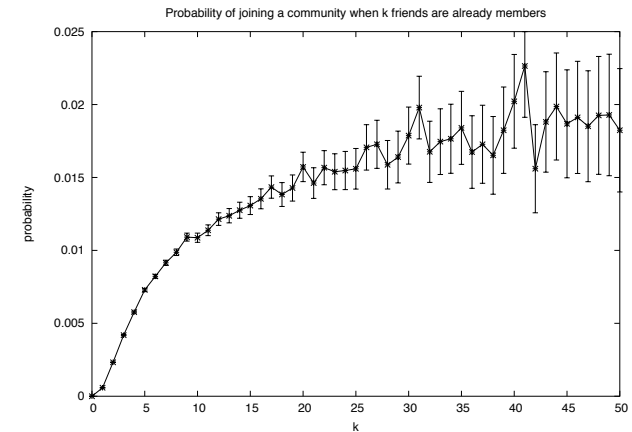
Kossinets-Watts, 2006

- Email network at large university.
- Prob. of link as function of # of shared acquaintances.

# Caveats

What we're measuring (e.g. for LJ)

- Snapshot of everyone's state relative to each group at time  $t_1$ .
- Which of these groups had people joined at time  $t_2 > t_1$ ?



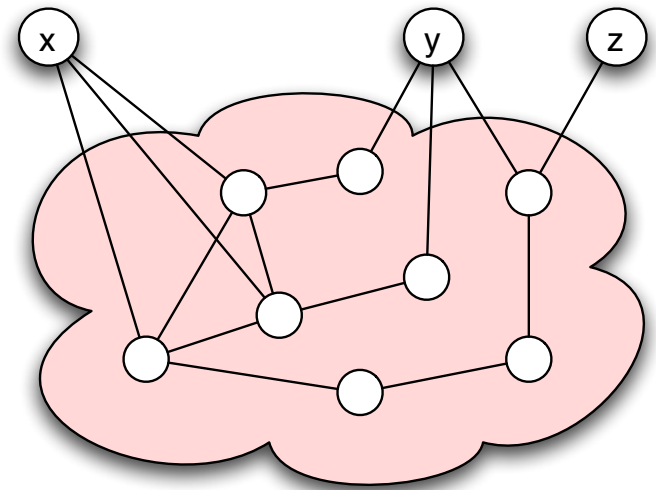
Challenge: Infer an operational model.

- At time  $t_1$ , we see the behavior of node  $v$ 's friends.
- When did  $v$  become aware of their behavior?  
When did this translate into a decision by  $v$  to act?  
How long after this decision did  $v$  act?
- Much of the problem: modeling the asynchrony.

# More subtle features

Dependence on number of friends:  
a first step toward general prediction.

- Given network and  $v$ 's position in it at  $t_1$ , estimate probability  $v$  will join a given group by  $t_2$ .
- Number of friends in community is only one of many possible features.



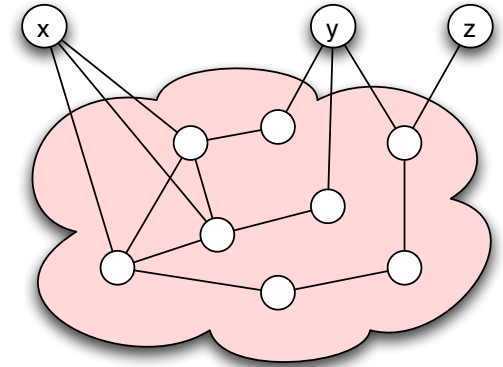
When formulated as a probability estimation problem, connectedness of friends emerges as a significant feature.

- $x$  and  $y$  each have three friends in group.
- $x$ 's friends are all connected;  $y$ 's friends are independent.
- Who is more likely to join?

# Connectedness of friends

## Competing sociological theories

- Informational argument [Granovetter '73]
- Social capital argument [Coleman '88]

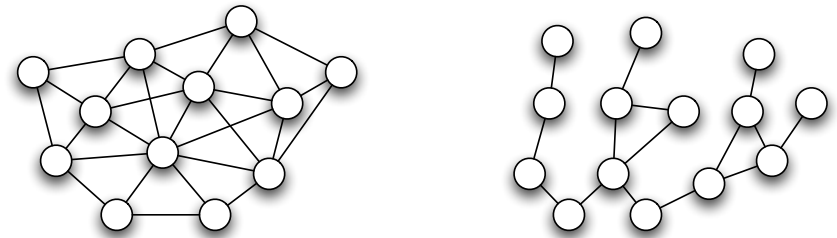


- Informational argument: unconnected friends give independent support.
- Social capital argument: safety/trust advantage in having friends who know each other.
- In LiveJournal, joining probability increases significantly with more connections among friends in group.

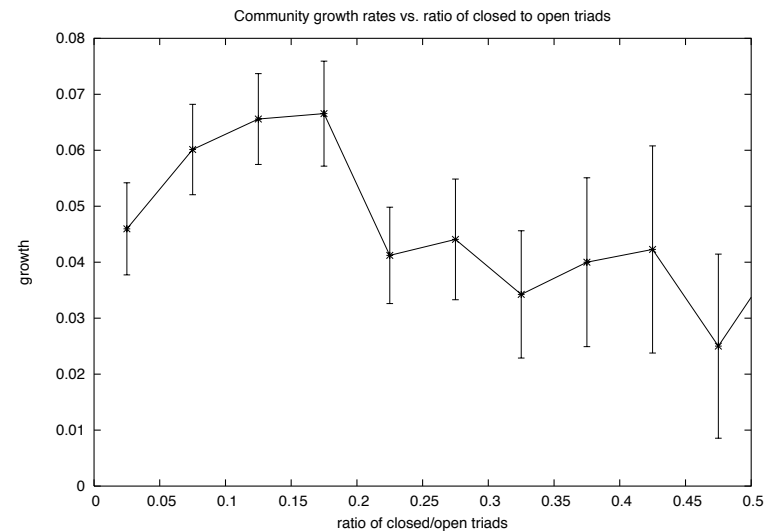


# A Puzzle

If connectedness among friends promotes joining, do highly “clustered” groups grow more quickly?



- Define clustering =  $\# \text{ triangles} / \# \text{ open triads}$ .
- Look at growth from  $t_1$  to  $t_2$  as function of clustering.
- Groups with large clustering grow slower.
- But not just because clustered groups had fewer nodes one step away.



# Further Directions for Diffusion

- Diffusion of Topics [Gruhl et al 2004, Adar et al 2004]
  - News stories cascade through networks of bloggers and media
  - How should we track stories and rank news sources?
  - A taxonomy of sources: discoverers, amplifiers, reshapers, ...
- Predictive frameworks for diffusion
  - Machine learning models for the growth of communities [Backstrom et al. 2006]
  - Is a new idea's rise to success inherently unpredictable? [Salganik-Dodds-Watts 2006]
- Building diffusion into the design of social media [Leskovec-Adamic-Huberman 2006, Kleinberg-Raghavan 2005]
  - Incentives to propagate interesting recommendations along social network links.
  - Simple markets based on question-answering and information-seeking.

# Recommendation Incentive Networks

Recall: recommendation incentive program at large on-line retailer  
[Leskovec-Adamic-Huberman'06, Leskovec-Singh-Kleinberg'06]

- With each purchase of a product, you can e-mail a recommendation of the product to friends.
- If one of them buys it, you both get a discount.

Theoretical models and analysis for such systems largely open.

- Adds a third component to word-of-mouth marketing models.
  - Direct advertising to full population
  - Targeted approach to influential nodes
  - Incentives to reduce “friction” on links between nodes.
- How to optimally trade off among (1), (2), and (3)?  
How does this depend on properties of the product/idea being marketed?
- How do different strategies affect the types of cascading behavior that result?

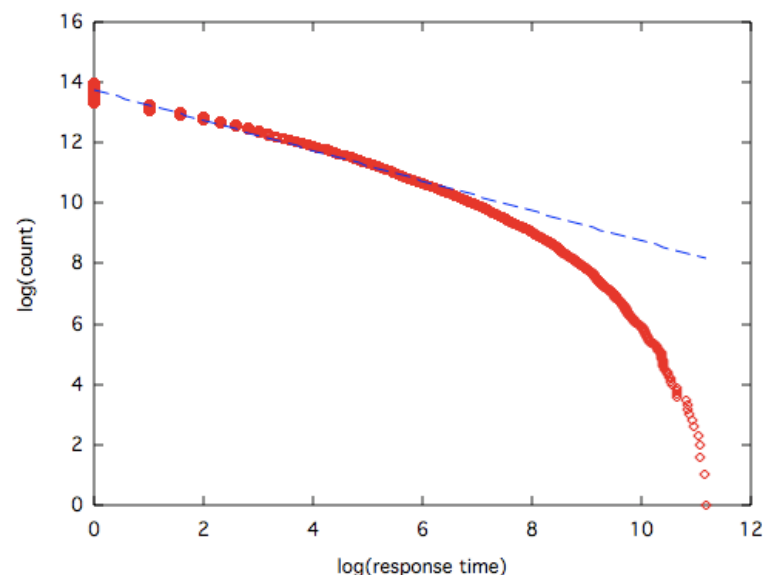
# Final Reflections: Toward a Model of You

Further direction: from populations to individuals

- Distributions over millions of people leave open several possibilities:
  - Individual are highly diverse, and the distribution only appears in aggregate, or
  - Each individual personally follows (a version of) the distribution.
- Recent studies suggests that sometimes the second option may in fact be true.

Example: what is the probability that you answer a piece of e-mail within  $t$  days (conditioned on answering at all)?

- Recent theories suggest  $t^{-1.5}$  with exponential cut-off [Barabasi 2005]



# Final Reflections: Interacting in the On-Line World

MySpace is doubly awkward because it makes public what should be private. It doesn't just create social networks, it anatomizes them. It spreads them out like a digestive tract on the autopsy table. You can see what's connected to what, who's connected to whom.

– Toronto Globe and Mail, June 2006.

- Social networks — implicit for millenia — are increasingly being recorded at arbitrary resolution and browsable in our information systems.
- Your software has a trace of your activities resolved to the second — and increasingly knows more about your behavior than you do.
- Models based on algorithmic ideas will be crucial in understanding these developments.