# Lecture 13: Acceleration Structures 

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## Faster Ray-Object Intersections

- Object bounding volumes

- Avoid intersection tests for expensive objects: e.g., polygon sets, spline surfaces - Ray/sphere or ray/cuboid test is fast


## Fewer Ray-Object Intersections

- From $\mathrm{O}(\mathrm{N})$ to $\mathrm{O}(\log \mathrm{N})$
- How?
- Apply the idea of bounding boxes hierarchically
- Cluster objects hierarchically
- Single intersection might eliminate cluster
- Bounding volume hierarchy
- Space subdivision
- Octree, Kd-tree, BSP-trees


## Bounding Volume Hierarchy

- Hierarchical object bounding volumes
- Spheres, axis-aligned bounding boxes (AABB), oriented bounding boxes(OBB): fast



## Intersection Acceleration

- Trace ray against root node
- If ray intersects node
- Trace ray against ALL children (Recurse)

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## Intersection Acceleration

- If no intersection, eliminate tests with all children!

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## BVH: Construction

- Group objects together
- Top-down: how to split?
- Bottom-up: minimize surface area?

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## BVH: Construction

- Group objects together
- Top-down: how to split?
- Bottom-up: minimize surface area?



## Fewer Ray-Object Intersections

- From $\mathrm{O}(\mathrm{N})$ to $\mathrm{O}(\log \mathrm{N})$
- Bounding volume hierarchy
- Space subdivision
- Octree (Quadtree in 2D)
- Non-uniform (kd-tree)
- BSP-tree


## Spatial Hierarchy

- Hierarchical spatial subdivision
- Divides up space
- Children are distinct and cover parent

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## Construction

- Maximum depth
- Maximum number of elements in leaf

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## Intersection Acceleration



## Intersection Acceleration



## Intersection Acceleration



## Intersection Acceleration



## Intersection Acceleration



## Intersection Acceleration

1. Intersect ray with root: $p=$ root.intersect(ray)

- If no intersection, done

2. Find $p$ in tree (node $j=$ root.find $(p)$ )
3. Test ray against elements in node $\mathbf{j}$

- If intersection found, done
- Else find exit point (q) from node j, p=q, goto 2


## Octree Properties

- Front to back traversal
- Problem: Same object in multiple cells
- Split object
- Could repeatedly intersect: use mailboxes



## Solutions

- Split object
- No repeated intersections and correct
- But, could create lots of little objects
- Use mailboxes
- Store intersection in the object: avoids repeated intersection
- What about correctness?
- Need to check that intersection is in "current" bounding box


## Octree Problems

- Distribution of objects
- Chops up objects

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## K-dimensional (kd) Tree

- Spatial subdivision
- Subdivide only 1 dimension
- Do not subdivide at the center
- Tracing with kd-tree unchanged



## Construction

- Which axis to pick?
-What point on the axis to pick?
- One heuristic:
- Sort objects on each axis
- Pick point corresponding to "middle" object
- Pick axis that has "best" distribution of objects
$-L=n / 2, R=n / 2$ (ideal)
- Realistically,
- minimize (L-R) and
- L approx. n/2, R approx. n/2


## BSP Tree

- Generalization of kd-trees
- Splitting plane is not axis aligned
- Used in games: DOOM



## BSP Construction

- Use a polygon to define the splitting plane
- Other objects either split or stored high up



## How to construct?

- Least-crossed criterion (random selection of polygons)
- Do not split many polygons
- Try to make it balanced


## BSP Traversal

- Front to back ordering
- Strict occlusion order (not closest object)


