# CS630 Representing and Accessing Digital Information

### **Recommender Systems**

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# Recommender Systems

- · Task definition
- · Item-to-Item Similarity
- · User-to-User Similarity
- · Recommendation
  - Content-based methods
  - Collaborative nearest neighbor methods
  - Collaborative model-based methods

# Motivation

- · Matchmaking between users and items
  - Filtering
  - Exploration
  - Marketing
  - etc.



# Data

- · Explicit feedback
  - Ratings
  - Reviews
  - Auctions
  - Auctio
- · Implicit feedback
  - Page visits
  - Purchase data
  - Browsing paths
  - etc

# Types of Recommendations

- · Item-to-Item associations
  - More pages like this
  - "Users who bought this book also bought X"
- · User-to-User associations
  - Which other user has similar interests?
- User-to-Item associations
  - Rating history describes user
  - Items are described by attributes
  - Items are described by ratings of other users

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### Item-to-Item Recommendation

### · Content-based approach

- Item is described by a set of attributes
  - · Movies: e.g director, genre, year, actors
  - · Documents: bag-of-word
- Similarity metric defines relationship between items
- · e.g. cosine similarity
- Examples
  - · "related pages" in search engine
  - · Google News

# Item-to-Item Recommendation

### · Collaborative filtering

- Item is described by user interactions
  - · Matrix V of n (number of users) rows and m (number of items) columns
  - · Elements of matrix V is user feedback
- Examples:
  - · Rating given to item by each user
  - · Users who viewed this item
- Similarity metric between items
  - · E.g. cosine

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# User-to-User Similarity

### · User is described by his/her ratings

Matrix V of n (number of users) rows and m (number of items) columns. Elements of matrix V is user feedback.

- Mean rating of user a 
$$\bar{v}_{a} = \frac{1}{l_{i}} \sum_{i} v_{as}$$
  $l_{i} = \#$  of ratings

• Similarity measure between users 
$$- \text{ Cosine } \qquad sim(a,b) = \sum_i \frac{v_{ai}}{\sqrt{\sum_k v_{ak}^2}} \frac{v_{bi}}{\sqrt{\sum_k v_{bk}^2}}$$

- Correlation 
$$sim(a,b) = \sum_i \frac{(v_{ai} - \overline{v}_a)(v_{bi} - \overline{v}_b)}{\sqrt{\sum_k (v_{ak} - \overline{v}_a)^2 \sum_k (v_{ak} - \overline{v}_a)^2}}$$

- data sparseness
- Unknown vs. unseen

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### Content-Based Recommendation

- · Use the ratings as feedback
  - Binary
  - Ordinal
- · Represent items using a set of features
  - Movies: e.g director, genre, year, actors
  - Documents: bag-of-word
- · Learn function that predicts the rating for un-rated
  - Learn one function per user
  - Can use any machine learning method
- · Strengths and Weaknesses?

# Collaborative Nearest-Neighbor Methods

- · Idea: Recommend items that similar users like
- · User is described by his/her ratings
  - Matrix V of n (number of users) rows and m (number of items) colums. Elements of matrix V is user feedback.
- Normalization
- Mean rating of user a  $\overline{v}_{a} = \frac{1}{l_{i}} \sum_{v_{ak}} v_{ak}$   $l_{i} = \#$  of ratings
  Similarity measure between users
  Cosine  $sim(a,b) = \sum_{i} \frac{v_{ak}}{\sqrt{\sum_{k} v_{ak}^{2}} \sqrt{\sum_{k} v_{bk}^{2}}}$  (or Correlation)
- · Prediction via linear combination

$$\hat{v}_{aj} = \bar{v}_a + \frac{1}{\sum_b |sim(a,b)|} \sum_i sim(a,b) (v_{bj} - \bar{v}_b)$$

# Collaborative Model-Based Methods

- Idea
  - Learn a model offline
  - Use model to make predictions online
- · Approach: Model joint density of user ratings
  - Cluster users
  - Approximate joint density with mixture model
- · Approach: Learn conditional model for each item
  - Learn prediction rules
  - One rule for each item

# Joint Density Modeling

· Idea: Estimate distribution of ratings via mixture

$$P(v_1,...,v_m) = \sum_{k=1}^{K} P(v_1,...,v_m|u=k)P(u=k)$$

- · Assumptions:
  - K disjoint user-interest classes
  - Each user is in exactly one interest class
  - Users within one class behave according to simple model,

$$P(v_1,...,v_m|u=k) = \prod_{j=1}^m P(v_j|u=k)$$

- - Classify user via mode  $u = \arg \prod_{k=1}^{K} x P(\hat{v}_1, ..., \hat{v}_l | u = k) P(u = k)$
  - Bayesian classification
- Extensions
  - User can be in multiple classes (Hofmann & Puzicha, 1999)

# Conditional Models

· Idea: Learn a prediction rule for each item

$$\bar{v}_{aj} = h(v_{a1},...,v_{am})$$

- · Learning Problem
  - Classification: Predict rating class [Heckerman et al., 2000]
  - Regression: Predict rating score
  - Ordinal Regression: Predict ranking of items [Cohen et al., 19991
- · Challenges:
  - Handling missing ratings
  - Computational expense for learning m models
  - No ratings for new products

# Cold-Start Problem

- · Problem: new users have too few ratings for effective recommendation
- · Idea: Combine ratings with other user attributes
  - Demographic attributes
  - Attributes from other domains
  - Ouestionnaires
- · Challenges:
  - Designing combined models
  - Trading-off user attributes with rating attributes

# Evaluation

### · Batch Evaluation

- Use historical data
- Split into training and test part on a per-user basis
- k ratings to describe user, remaining ratings for testing
- Problems?

### • Online Evaluation

- Install recommender system in operational system
- Controlled experiment with control group
  - Does the recommender system increase sales?
  - Does the recommender system make users return more often?
  - etc.