1 State in CPS

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2 Exposing continuations in the language

Continuations are great for talking about semantics, but they are also useful when programming.

2.1 \texttt{setjmp} and \texttt{longjmp}

\texttt{setjmp} is a C function which takes a pointer to a buffer. Its operation is to save the state of all registers (including the program counter) into the specified buffer and return 0. \texttt{longjmp}, also a C function, takes as an argument a pointer to a buffer (which is presumed to be a buffer which has already been filled with a previous call to \texttt{setjmp}) and a value. When invoked, it restores all of the registers to the values saved in the buffer and returns the value passed in to the point in the program where \texttt{setjmp} was called (in effect, the program resumes executing right where \texttt{setjmp} was called, except the call will return the value passed in to \texttt{longjmp}). These functions can be used for error handling. \texttt{setjmp} is called before code that may result in an error. If an error occurs in computation, \texttt{longjmp} is called in order to restore initial state and handle the error. For instance:

\begin{verbatim}
if (setjmp(&jmpbuf))
// error handling code goes here
else
  do\'computation();
  // if error occurs in compute(), call
  // longjmp(jmpbuf, e), where e is the error code
\end{verbatim}

The functions \texttt{setjmp} and \texttt{longjmp} can be translated using continuations as follows:

\begin{align*}
[\texttt{setjmp} \ e] \rho k &= [e] \rho (\text{CHECK-LOC} \ (\lambda l. \ s \ k (\text{INT} \ 0)) (\text{UPDATE} \ \sigma \ l \ (\text{CONT} \ k))) \\
[\texttt{longjmp} \ e \ e′] \rho k &= [e] \rho (\text{CHECK-LOC} \ (\lambda l. \ [e′] \rho \\
&\quad (\lambda v. \ \text{CHECK-CONT} (\text{LOOKUP} \ s l) (\lambda k′. \ k′ v \ s))) (\lambda \sigma. \ \text{CHECK-CONT} (\text{LOOKUP} \ s l) (\lambda k′. \ k′ v \ s)))
\end{align*}

The translation of \texttt{setjmp} stores a continuation at a new location, while the translation of \texttt{longjmp} restores a continuation from a program location. This is roughly equivalent to restoring the registers and program state of the executing program.

2.2 First-class continuations

Some languages expose continuations as first-class values. Examples of such languages include Scheme and SML/NJ. In the latter, there is a module that a continuation type \(\alpha\ cont\), representing a continuation expecting a value of type \(\alpha\). There are two functions for manipulating continuations:

\texttt{callcc}: \((\alpha\ cont \rightarrow \alpha) \rightarrow \alpha\)

\((\text{callcc} \ f)\) passes the current continuation to the function \(f\).

\texttt{throw}: \(\alpha\ cont \rightarrow \alpha \rightarrow \beta\)
(throw \(k\ v\)) sends the value \(v\) to the continuation \(k\).

Because callcc passes the current continuation, corresponding to the evaluation context of the callcc itself, invocation of the passed continuation makes the callcc expression itself seem to return again. It’s up to the evaluation context of the callcc to decide whether it’s seeing the original return from \(f\) or a later invocation of the passed continuation.

2.3 Semantics of first-class continuations

Using the translation approach we introduced earlier, we can easily describe these mechanisms. Suppose we represent a continuation value for the continuation \(k\) by tagging it with the integer 7. Then we can translate callcc and throw as follows:

\[
\begin{align*}
\text{[callcc } e] \rho k &= [e] \rho (\text{CHECK-FUN}(\lambda f. f(7, k) k)) \\
\text{[throw } e_1 e_2] \rho k &= [e_1] \rho (\text{CHECK-CONT}(\lambda k'. [e_2] \rho k'))
\end{align*}
\]

The key to the added power is the non-linear use of \(k\) in the callcc rule. This allows \(k\) to be reused any number of times.

2.4 Implementing threads with continuations

Once we have first-class continuations, we can use them to implement all the different control structures we might want. We can even use them to implement (non-preemptive) threads, as in the following SML/NJ-like code that explains how Concurrent ML (CML) is implemented:

```sml
type thread = unit cont
ready: thread queue = new_queue (* a mutable FIFO queue *)
enqueue(t) = insert ready t
dispatch() = throw (dequeue ready) ()
spawn(f: unit -> unit): unit = 
  callcc( fn(k) => (enqueue k; f(); dispatch()))
yield(): unit = callcc (fn(k) => enqueue k; dispatch())
```

The interface to threads is the functions spawn and yield. The spawn function expects a function \(f\) containing the work to be done in the newly spawned thread. The yield function causes the current thread to relinquish control to the next thread on the ready queue. Control also transfers to a new thread when one thread finishes evaluating. To complete the implementation of this thread package, we just need a queue implementation. CML has preemptive threads, in which threads implicitly yield automatically after a certain amount of time; this requires just a little help from the operating system.