# Performance Measures for Machine Learning

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### Performance Measures

- Accuracy
- Weighted (Cost-Sensitive) Accuracy
- Lift
- ROC
  - ROC Area
- Precision/Recall
  - F
  - Break Even Point
- Similarity of Various Performance Metrics via MDS (Multi-Dimensional Scaling)

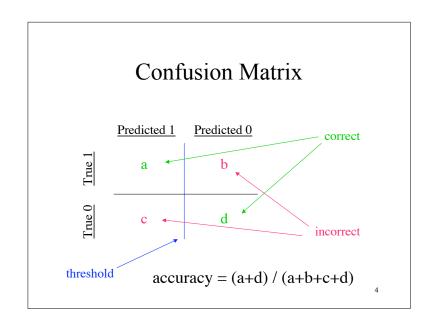
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# Accuracy

- Target: 0/1, -1/+1, True/False, ...
- Prediction = f(inputs) = f(x): 0/1 or Real
- Threshold: f(x) > thresh => 1, else => 0
- If threshold(f(x)) and targets both 0/1:

$$accuracy = \frac{\sum_{i=1...N} (1 - \left| target_i - threshold(f(\vec{x}_i)) \right|_{ABS})}{N}$$

- #right / #total
- p("correct"): p(threshold(f(x)) = target)



	Predicted 1	Predicted 0
True 1	true positive	false negative
True 0	false positive	true negative
	Predicted 1	Predicted 0
True 1	hits	misses

false

alarms

correct

rejections

	Predicted 1	Predicted 0
True 1	TP	FN
True 0	FP	TN

	Predicted 1	Predicted 0
True 1	P(pr1ltr1)	P(pr0ltr1)
True 0	P(pr1ltr0)	P(pr0ltr0)

### **Prediction Threshold**

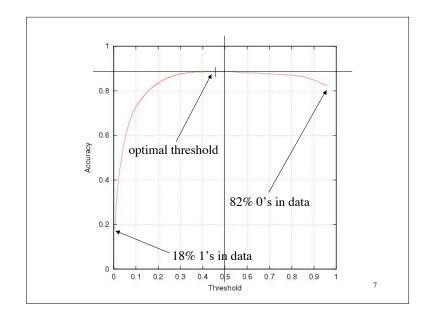
<u>P</u>	redicted 1	Predicted 0
True 1	0	b
True 0	0	d

- threshold > MAX(f(x))
- all cases predicted 0
- (b+d) = total
- accuracy = %False = %0's

	Predicted 1	Predicted (
True 1	a	0
True 0	c	0

- threshold < MIN(f(x))
- all cases predicted 1
- (a+c) = total
- accuracy = %True = %1's

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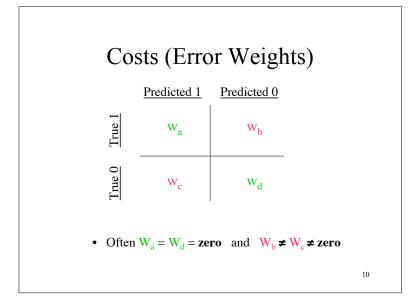
# Problems with Accuracy

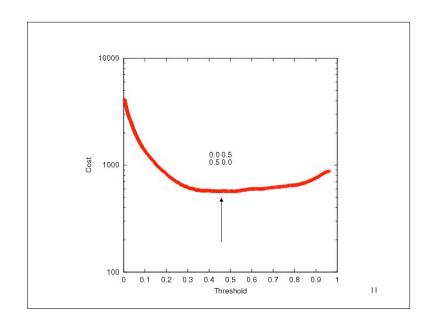
- Assumes equal cost for both kinds of errors
  - cost(b-type-error) = cost (c-type-error)
- is 99% accuracy good?
  - can be excellent, good, mediocre, poor, terrible
  - depends on problem
- is 10% accuracy bad?
  - information retrieval
- BaseRate = accuracy of predicting predominant class (on most problems obtaining BaseRate accuracy is easy)

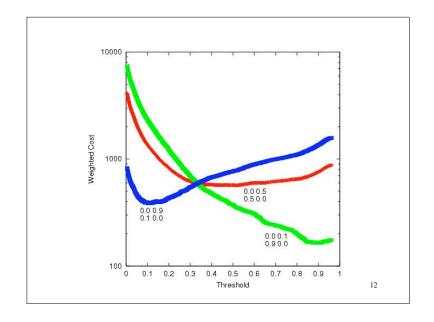
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### Percent Reduction in Error

- 80% accuracy = 20% error
- suppose learning increases accuracy from 80% to 90%
- error reduced from 20% to 10%
- 50% reduction in error
- 99.90% to 99.99% = 90% reduction in error
- 50% to 75% = 50% reduction in error
- can be applied to many other measures

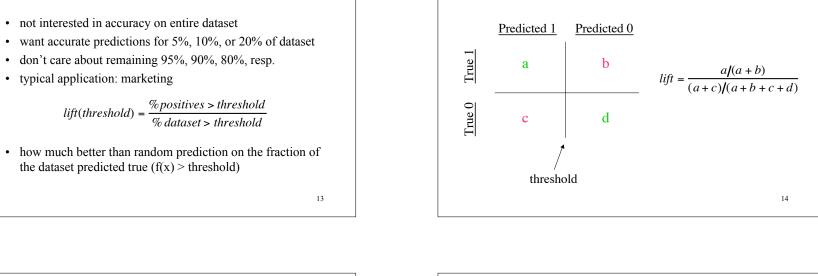


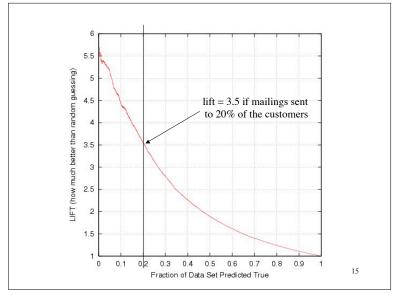


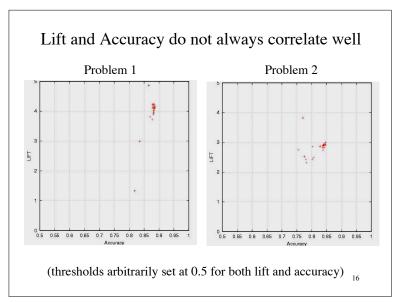


### Lift

the dataset predicted true (f(x) > threshold)







Lift

### ROC Plot and ROC Area

- Receiver Operator Characteristic
- Developed in WWII to statistically model false positive and false negative detections of radar operators
- Better statistical foundations than most other measures
- Standard measure in medicine and biology
- Becoming more popular in ML

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# HOC Area = 0.9049 HOC Area = 0.9049 diagonal line is random prediction 1-Specificity = False Positive Rate = P(pred true|false)

### **ROC Plot**

- Sweep threshold and plot
  - TPR vs. FPR
  - Sensitivity vs. 1-Specificity
  - P(true|true) vs. P(true|false)
- Sensitivity = a/(a+b) = LIFT numerator = Recall (see later)
- 1 Specificity = 1 d/(c+d)

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# Properties of ROC

- ROC Area:
  - 1.0: perfect prediction
  - 0.9: excellent prediction
  - 0.8: good prediction
  - 0.7: mediocre prediction
  - 0.6: poor prediction
  - 0.5: random prediction
  - <0.5: something wrong!

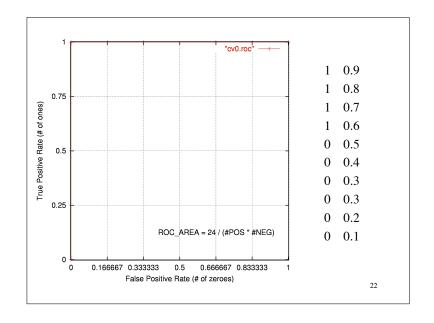
# Wilcoxon-Mann-Whitney

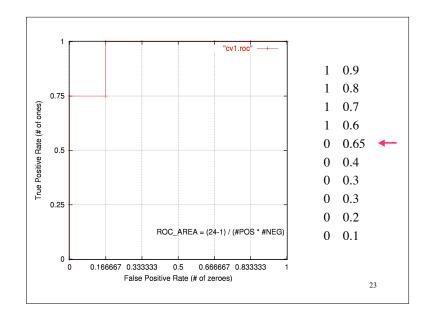
$$ROCA = 1 - \frac{\#\_pairwise\_inversions}{\#POS * \#NEG}$$

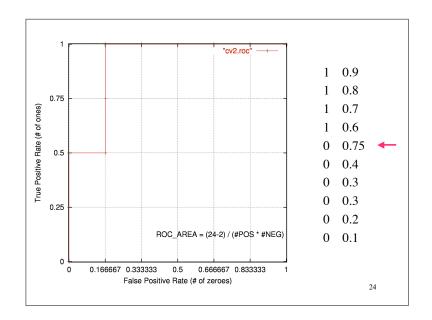
where

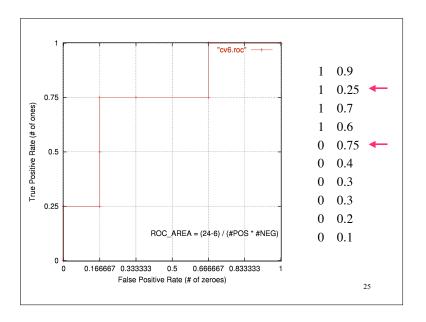
$$\#\_pair\_inversions =$$

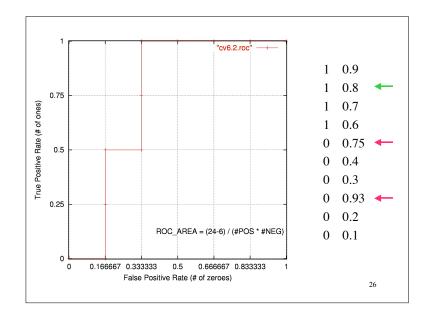
$$\sum_{i,j} I[(P(x_i) > P(x_j)) \& (T(x_i) < T(x_j))]$$

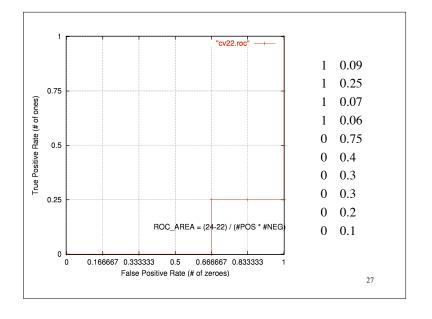


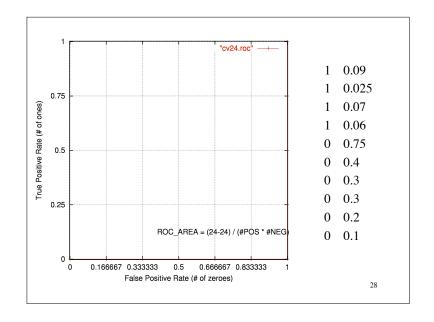








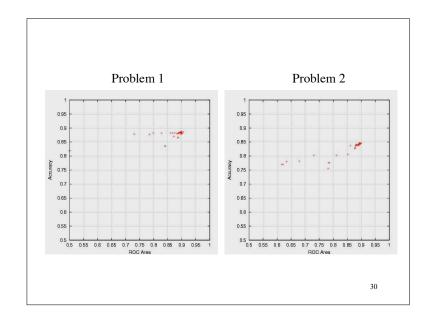




# Properties of ROC

- Slope is non-increasing
- Each point on ROC represents different tradeoff (cost ratio) between false positives and false negatives
- Slope of line tangent to curve defines the cost ratio
- ROC Area represents performance averaged over all possible cost ratios
- If two ROC curves do not intersect, one method dominates the other
- If two ROC curves intersect, one method is better for some cost ratios, and other method is better for other cost ratios

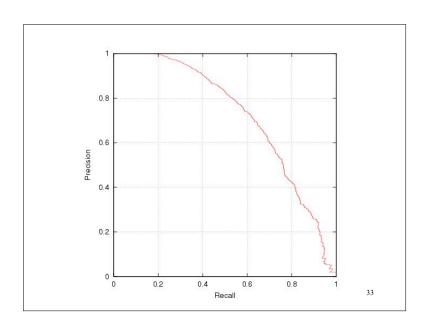
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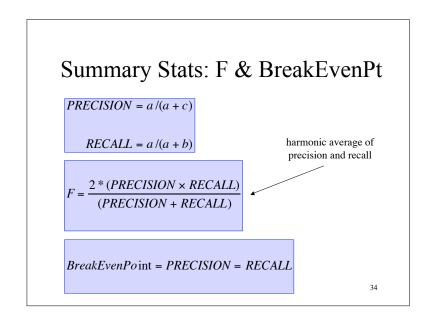


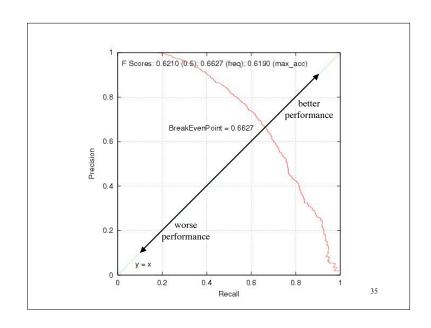
### Precision and Recall

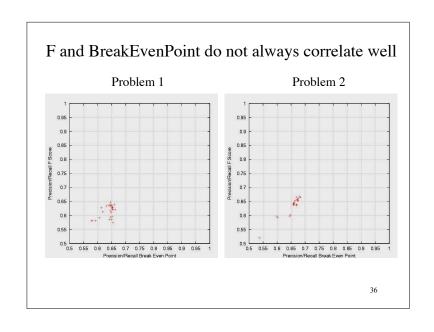
- typically used in document retrieval
- Precision:
  - how many of the returned documents are correct
  - precision(threshold)
- Recall:
  - how many of the positives does the model return
  - recall(threshold)
- Precision/Recall Curve: sweep thresholds

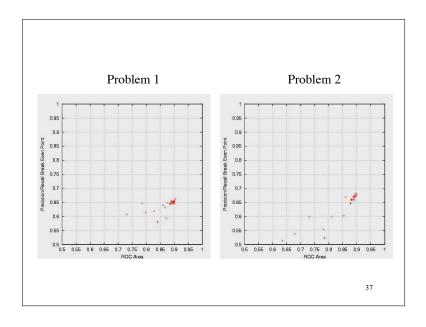
 $\frac{\text{Precision/Recall}}{\text{predicted 1}} = \frac{\text{Predicted 0}}{\text{a}}$   $\frac{\text{Precision/Recall}}{\text{a}} = \frac{\text{Predicted 0}}{\text{b}}$   $\frac{\text{PRECISION} = a/(a+c)}{\text{RECALL} = a/(a+b)}$ threshold

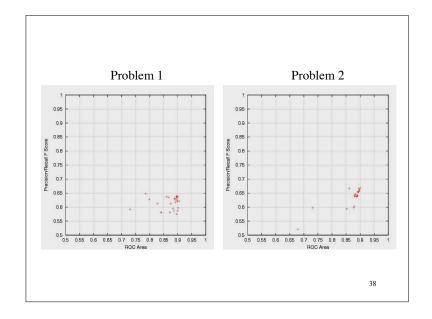












# Many Other Metrics

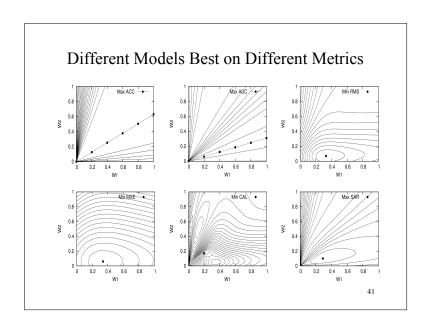
- Mitre F-Score
- Kappa score
- Balanced Accuracy
- RMSE (squared error)
- Log-loss (cross entropy)
- Calibration
  - $\,-\,$  reliability diagrams and summary scores

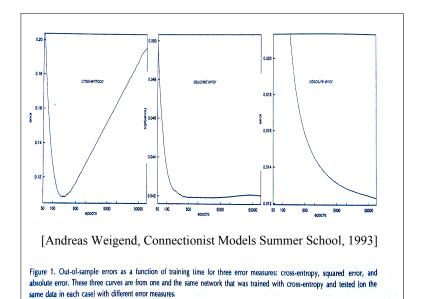
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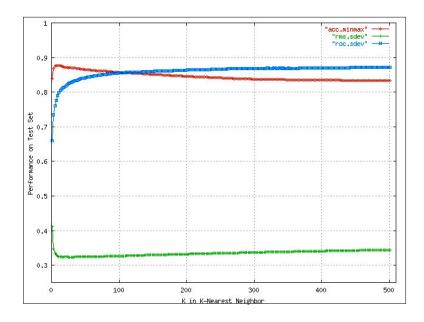
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# Summary

- the measure you optimize to makes a difference
- the measure you report makes a difference
- use measure appropriate for problem/community
- accuracy often is not sufficient/appropriate
- ROC is gaining popularity in the ML community
- only a few of these (e.g. accuracy) generalize easily to >2 classes







Really does matter what you optimize!

