Special Topic:

Missing Values
Missing Values Common in Real Data

- **Pneumonia**:  
  - 6.3% of attribute values are missing  
  - one attribute is missing in 61% of cases
- **C-Section**:  
  - only about 1/2% of attribute values are missing  
  - but 27.9% of cases have at least 1 missing value
- **UCI machine learning repository**:  
  - 31 of 68 data sets reported to have missing values
“Missing” Can Mean Many Things

- **MAR: "Missing at Random":**
  - usually best case
  - usually not true
- **Non-randomly missing**
- **Presumed normal, so not measured**
- **Causally missing:**
  - attribute value is missing because of other attribute values (or because of the outcome value!)
Dealing With Missing Data

- Some learning methods can handle missing values
- Throw away cases with missing values
  - in some data sets, most cases get thrown away
  - if not missing at random, throwing away cases can bias sample towards certain kinds of cases
- Treat “missing” as a new attribute value
  - what value should we use to code for missing with continuous or ordinal attributes?
  - if missing causally related to what is being predicted?
- Impute (fill-in) missing values
  - once filled in, data set is easy to use
  - if missing values poorly predicted, may hurt performance of subsequent uses of data set
Imputing Missing Values

- Fill-in with mean, median, or most common value
- Predict missing values using machine learning
- Expectation Minimization (EM):
  - Build model of data values (ignore missing vals)
  - Use model to estimate missing values
  - Build new model of data values (including estimated values from previous step)
  - Use new model to re-estimate missing values
  - Re-estimate model
  - Repeat until convergence
Potential Problems

- Imputed values may be inappropriate:
  - in medical databases, if missing values not imputed separately for male and female patients, may end up with male patients with 1.3 prior pregnancies, and female patients with low sperm counts
  - many of these situations will not be so humorous/obvious!
- If some attributes are difficult to predict, filled-in values may be random (or worse)
- Some of the best performing machine learning methods are impractical to use for filling in missing values (neural nets)
- Beware of coding - reliably detect missing cases can be difficult
Research in Handling Missing Values

- Lazy learning:
  - don’t train a model until you know test case
  - missing in test case may “shadow” missing values in train set
- Better algorithms:
  - Expectation maximization (EM)
  - Non-parametric methods (since parametric methods often work poorly when assumptions are violated)
- Faster Algorithms:
  - apply to very large datasets
Special Topic:

Feature Selection
Anti-Motivation

- Most learning methods implicitly do feature selection:
  - decision trees: use info gain or gain ratio to decide what attributes to use as tests. Many features don’t get used.
  - neural nets: backprop learns strong connections to some inputs, and near-zero connections to other inputs.
  - kNN, MBL: weights in Weighted Euclidean Distance determine how important each feature is. Weights near zero mean feature is not used.
  - SVMs: maximum margin hyperplane may focus on important features, ignore irrelevant features.
- So why do we need feature selection?
Motivation
Motivation
Motivation
Features selected: Total 65 removed, 78 used. Please refer to Appendix A for

Performance comparison to original model (without feature selection):

![Graph showing performance comparison with different models and parameters](image)
Motivation
Brute-Force Approach

- Try all possible combinations of features
- Given N features, $2^N$ subsets of features
  - usually too many to try
  - danger of overfitting
- Train on train set, evaluate on test set (or use cross-validation)
- Use set of features that performs best on test set(s)
Two Basic Approaches

- **Wrapper Methods:**
  - give different sets of features to the learning algorithm and see which works better
  - *algorithm dependent*

- **Proxy Methods (relevance determination methods):**
  - determine what features are important or not important for the prediction problem without knowing/using what learning algorithm will be employed
  - *algorithm independent*
Wrapper Methods

• Wrapper methods find features that work best with some particular learning algorithm:
  – best features for kNN and neural nets may not be best features for decision trees
  – can eliminate features learning algorithm “has trouble with”

• Forward stepwise selection
• Backwards elimination
• Bi-directional stepwise selection and elimination
Relevance Determination Methods

- Rank features by information gain
  - Info Gain = reduction in entropy due to attribute

\[
\text{Entropy} = - p_+ \log_2 p_+ - p_- \log_2 p_-
\]

\[
\text{Gain}(S, A) = \text{Entropy}(S) \sum_{v \in \text{Values}(A)} \frac{|S_v|}{|S|} \text{Entropy}(S_v)
\]

- Try first 10, 20, 30, ..., N features with learner
- Evaluate on test set (or use cross validation)
- May be only practical method if thousands of attributes
Advantages of Feature Selection

• Improved accuracy!
• Less complex models:
  – run faster
  – easier to understand, verify, explain
• Feature selection points you to most important features
• Don’t need to collect/process features not used in models
Limitations of Feature Selection

• Given many features, feature selection can overfit
  – consider 10 relevant features, and $10^9$ random irrelevant features
• Wrapper methods require running base learning algorithm many times, which can be expensive!
• Just because feature selection doesn’t select a feature, doesn’t mean that feature isn’t a strong predictor
  – redundant features
• May throw away features domain experts want in model
• Most feature selection methods are greedy and won’t find optimal feature set
Current Research in Feature Selection

• Speeding-up feature selection (1000’s of features)
• Preventing overfitting (1000’s of features)
• Better proxy methods
  – would be nice to know what the good/relevant features are independent of the learning algorithm
• Irrelevance detection:
  – truly irrelevant attributes can be ignored
  – better algorithms
  – better definition(s)
Bottom Line

- Feature selection almost always improves accuracy on real problems
- Plus:
  - simpler, more intelligible models
  - features selected can tell you about problem
  - less features to collect when using model in future

*Feature selection usually is a win.*