

CS5670: Computer Vision

Panoramas



What's inside your fridge?

Announcements

- Project 3: Autostitch (Panorama Stitching)
 - Released today, March 22
 - Due on Friday, April 2, by 7pm
 - To be done in groups of 2
 - If you need help finding a team member, let me know
- Quiz this Wednesday, March 24 (ends 7 minutes after start of class)

From Last Time: Perspective distortion: People



Distortion-Free Wide-Angle Portraits on Camera Phones



(a) A wide-angle photo with distortions on subjects' faces.

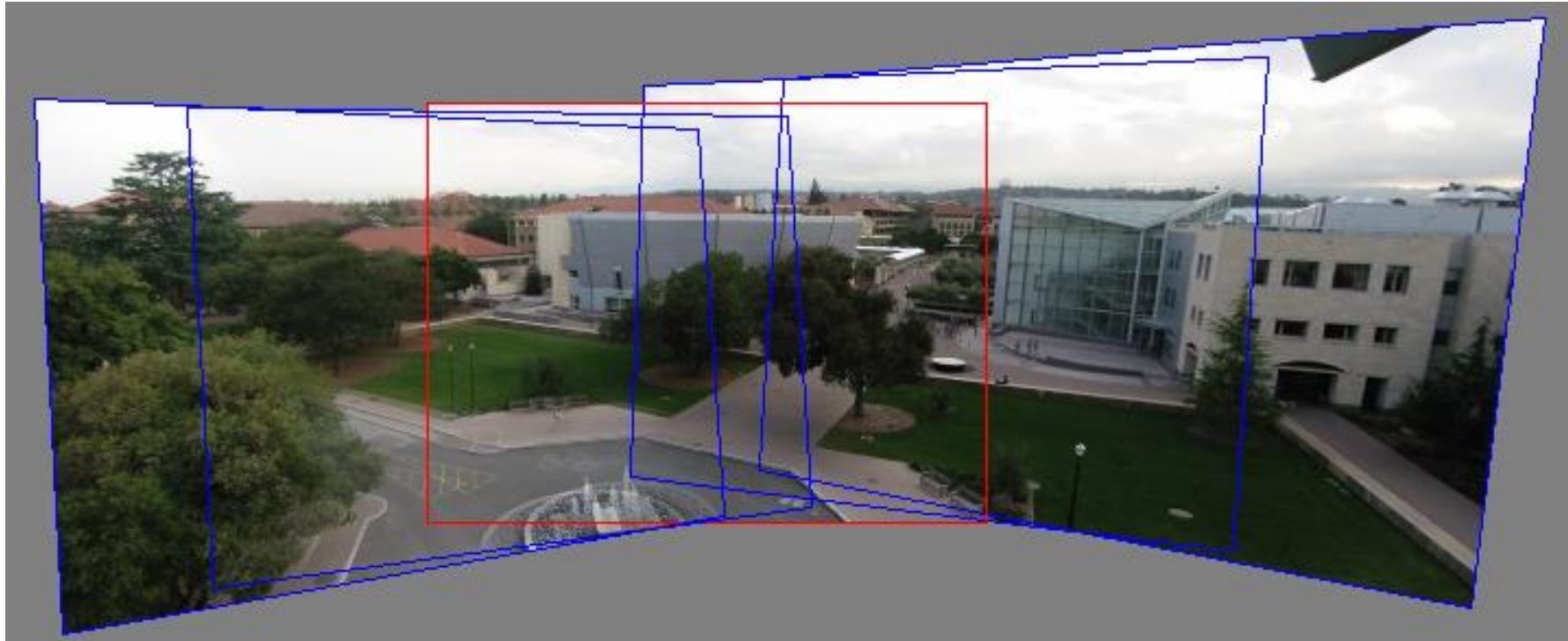


(b) Distortion-free photo by our method.

YiChang Shih, Wei-Sheng Lai, and Chia-Kai Liang, Distortion-Free Wide-Angle Portraits on Camera Phones, SIGGRAPH 2019

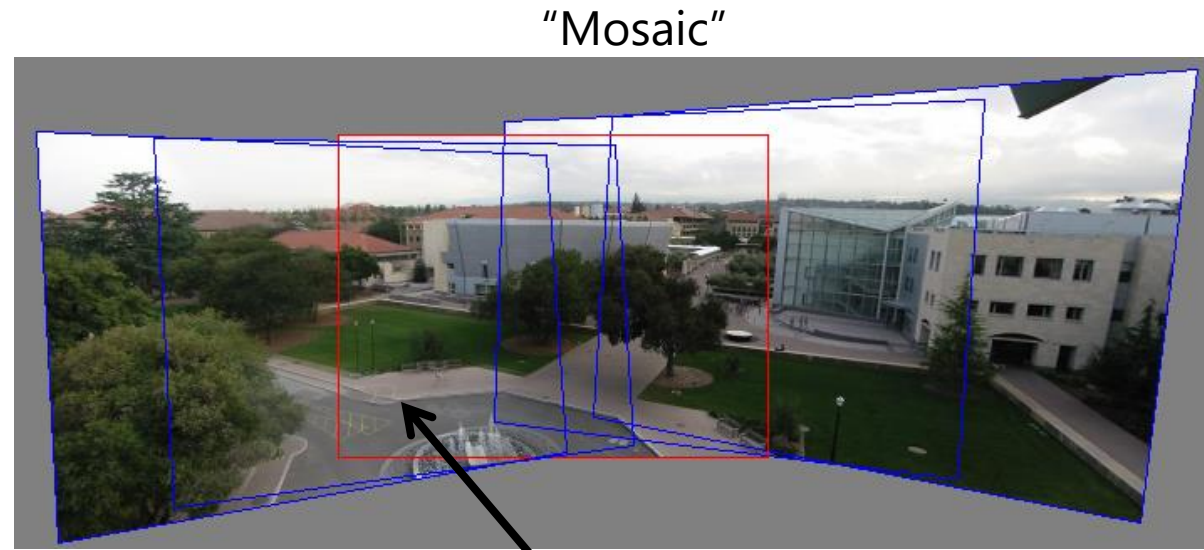
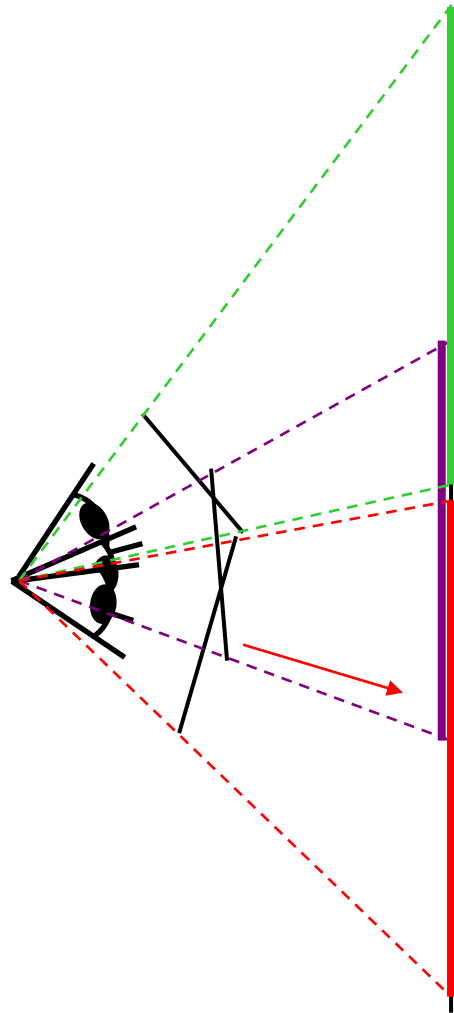
https://people.csail.mit.edu/yichangshih/wide_angle_portrait/

Back to panoramas



Can we use homographies to create a 360 degree panorama?

Idea: project images onto a common plane



each image is warped
with a homography \mathbf{H}

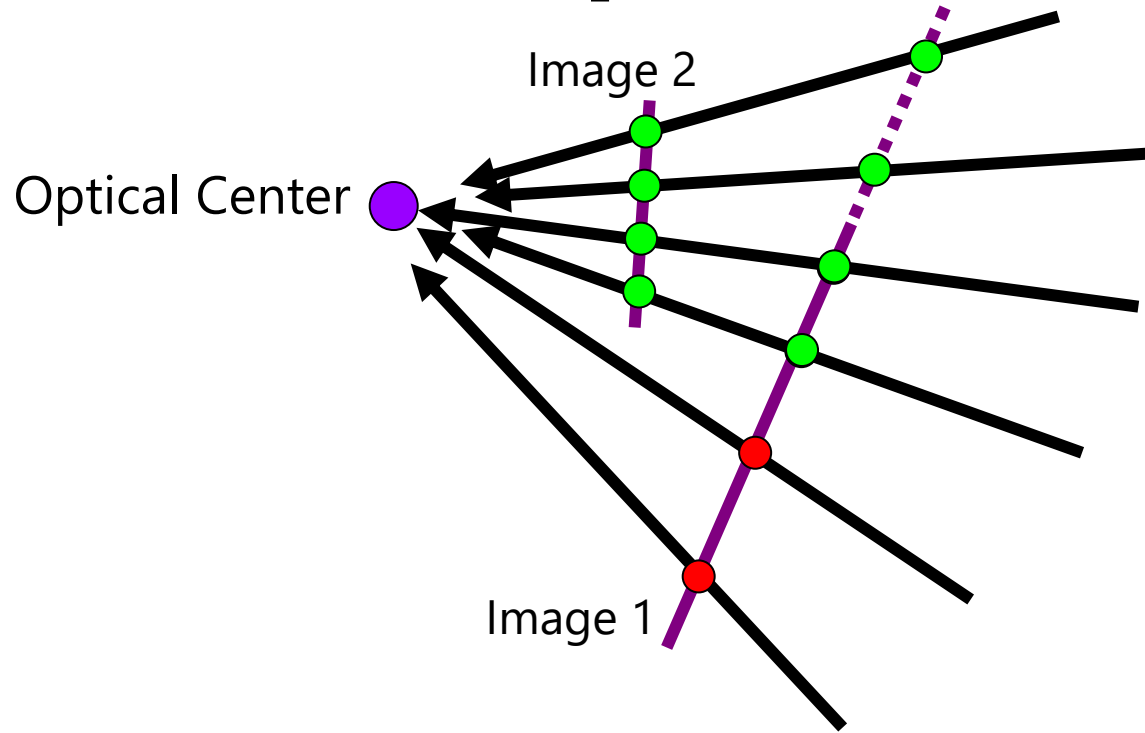
We'll see what this homography means next
Can't create a 360 panorama this way... we'll fix this shortly

mosaic projection plane

Creating a panorama

- Basic Procedure
 - Take a sequence of images from the same position
 - Rotate the camera about its optical center
 - Compute transformation between second image and first
 - Transform the second image to overlap with the first
 - Blend the two together to create a mosaic
 - If there are more images, repeat

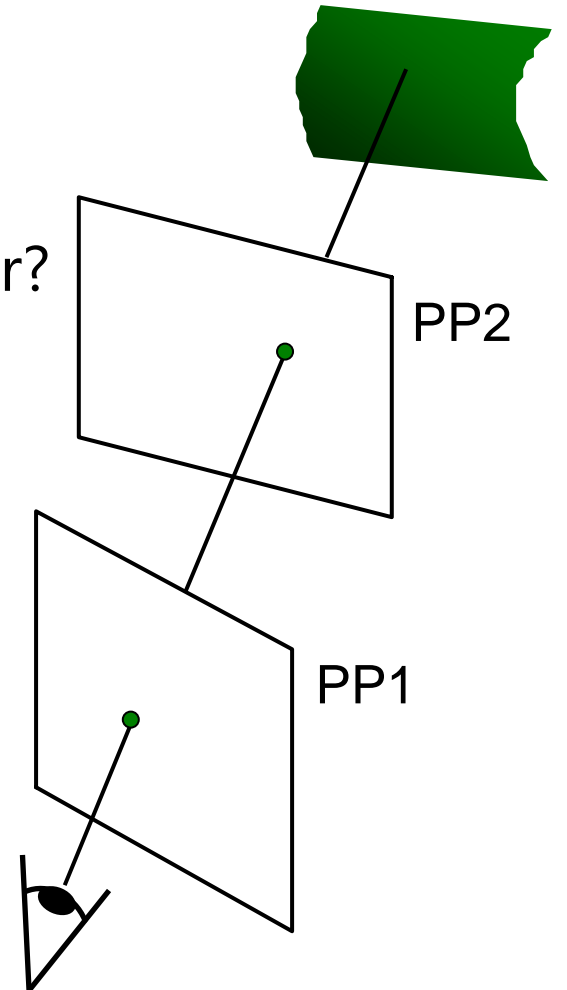
Geometric interpretation of mosaics



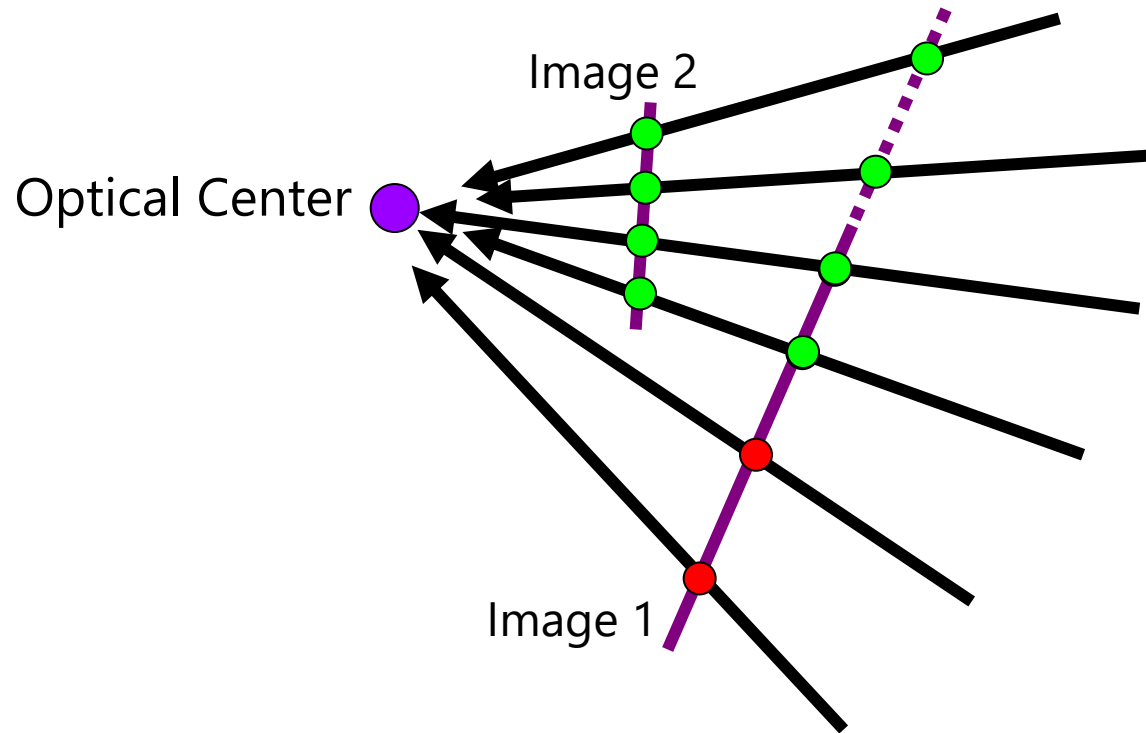
- If we capture all 360° of rays, we can create a 360° panorama
- The basic operation is *projecting* an image from one plane to another
- The projective transformation is scene-INDEPENDENT
 - This depends on all the images having the same optical center

Image reprojection

- Basic question
 - How to relate two images from the same camera center?
 - how to map a pixel from PP1 to PP2
- Answer
 - Cast a ray through each pixel in PP1
 - Draw the pixel where that ray intersects PP2



What is the transformation?



Step 1: Convert pixels in image 2 to rays in camera 2's coordinate system.

$$\begin{bmatrix} X_2 \\ Y_2 \\ Z_2 \end{bmatrix} = \mathbf{K}_2^{-1} \begin{bmatrix} x_2 \\ y_2 \\ 1 \end{bmatrix}$$

Step 2: Convert rays in camera 2's coordinates to rays in camera 1's coordinates.

$$\begin{bmatrix} X_1 \\ Y_1 \\ Z_1 \end{bmatrix} = \mathbf{R}_2^T \mathbf{K}_2^{-1} \begin{bmatrix} x_2 \\ y_2 \\ 1 \end{bmatrix}$$

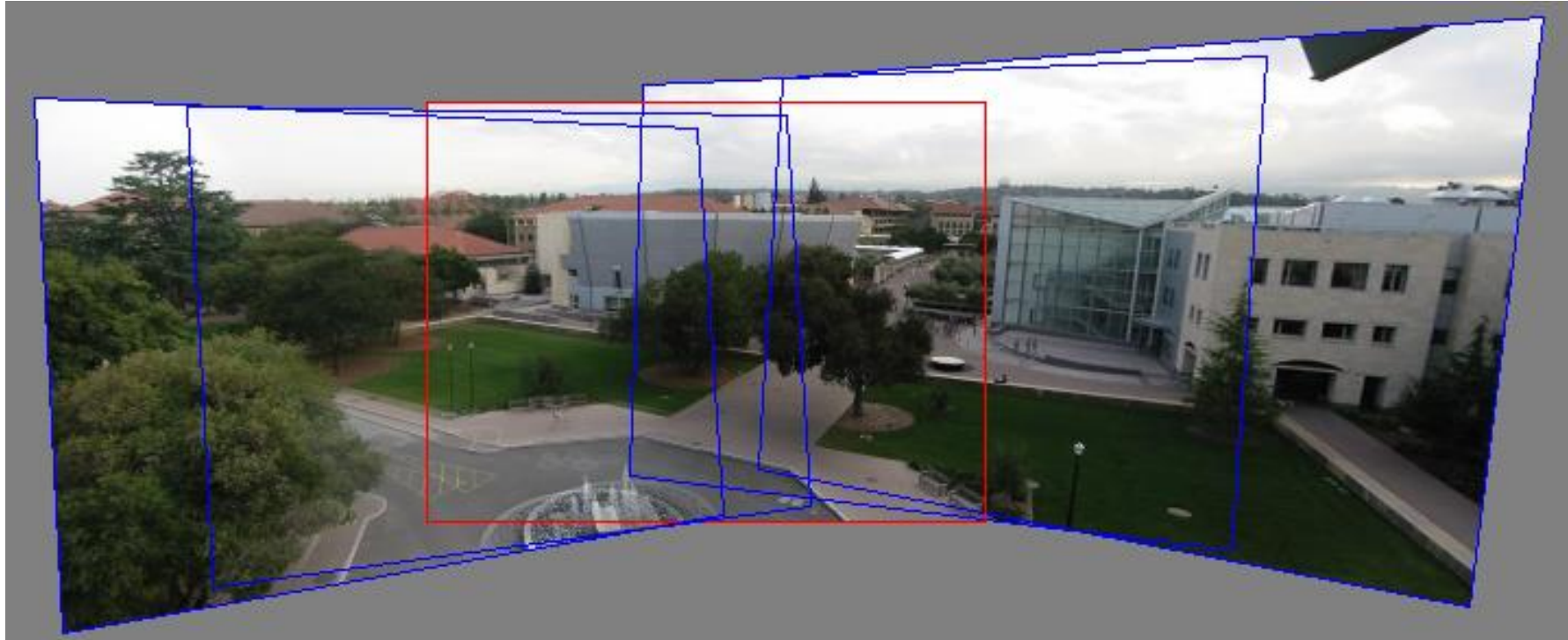
Step 3: Convert rays in camera 1's coordinates to pixels in image 1's coordinates.

$$\begin{bmatrix} x_1 \\ y_1 \\ 1 \end{bmatrix} \sim \underbrace{\mathbf{K}_1 \mathbf{R}_2^T \mathbf{K}_2^{-1}}_{\substack{\text{3x3 homography} \\ \uparrow}} \begin{bmatrix} x_2 \\ y_2 \\ 1 \end{bmatrix}$$

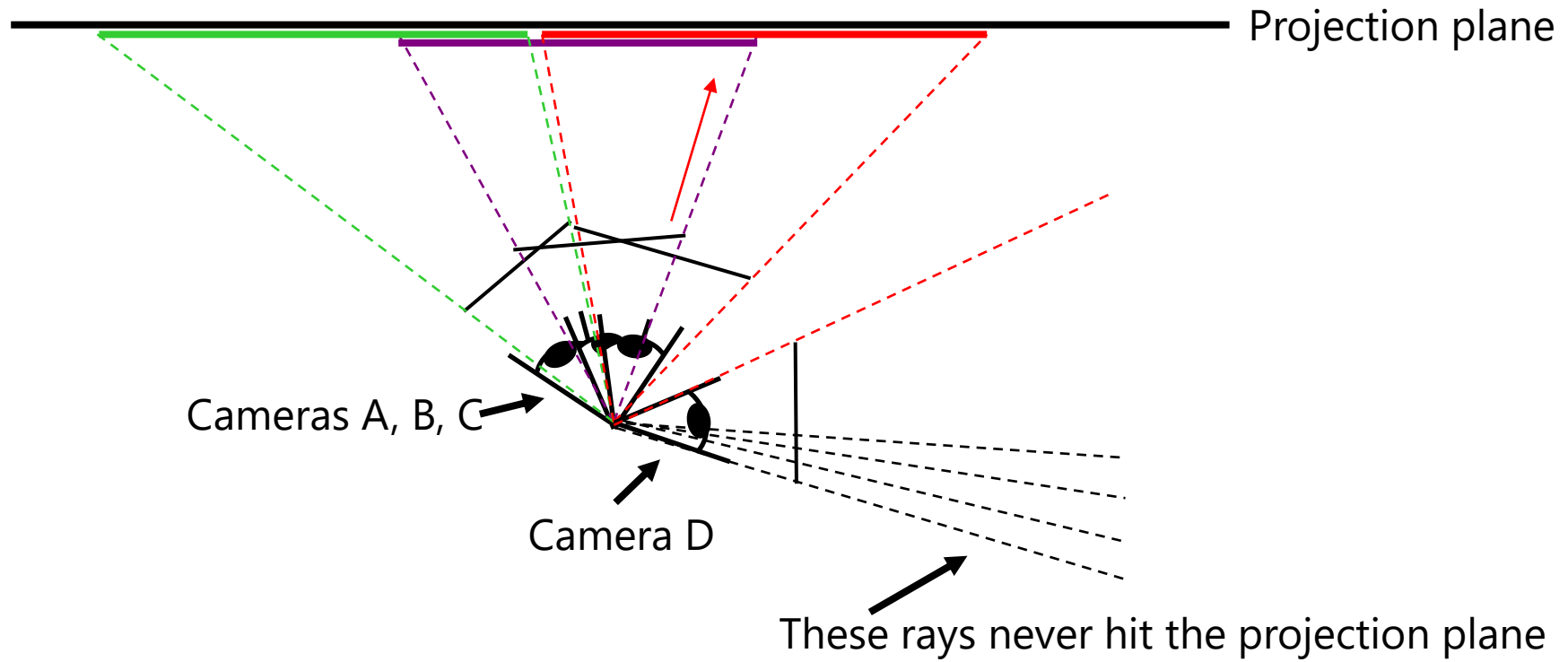
How do we map points in image 2 into image 1?

	image 1	image 2
intrinsics	\mathbf{K}_1	\mathbf{K}_2
extrinsics (rotation only)	$\mathbf{R}_1 = \mathbf{I}_{3 \times 3}$	\mathbf{R}_2

Can we use homography to create a 360 panorama?

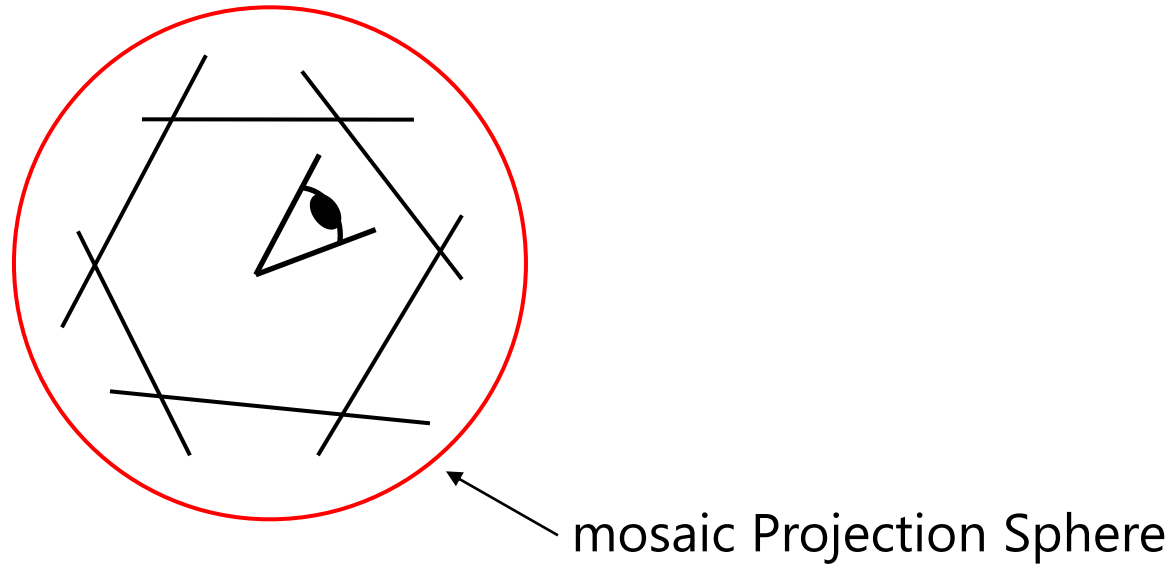


Answer: No

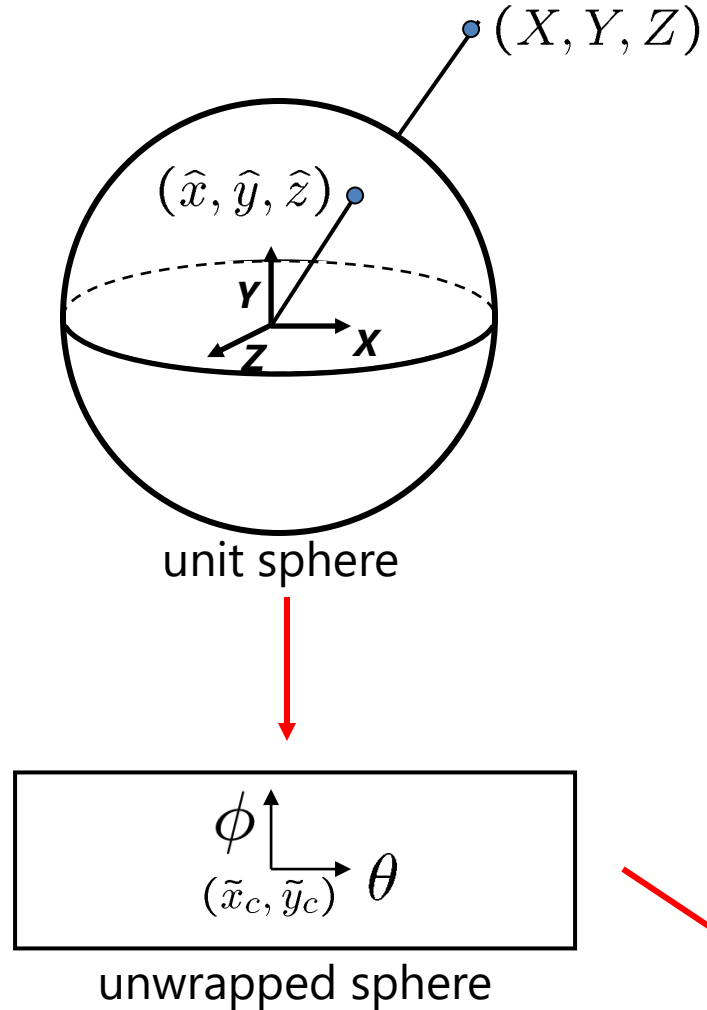


Panoramas

- What if you want a 360° field of view?



Spherical projection



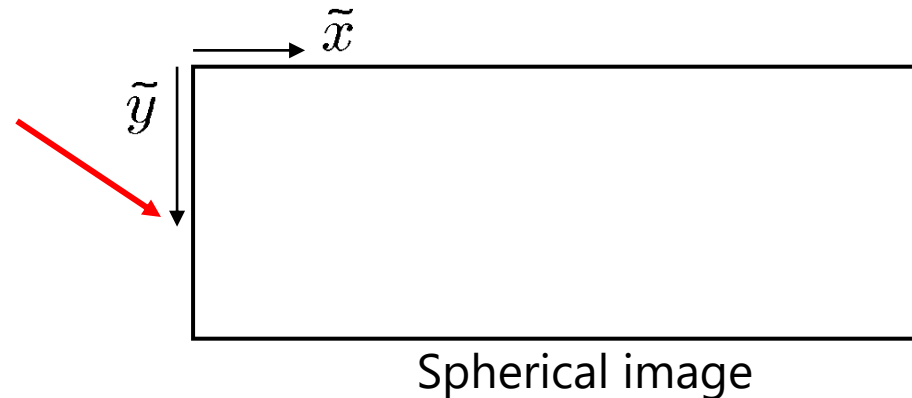
- Map 3D point (X, Y, Z) onto sphere

$$(\hat{x}, \hat{y}, \hat{z}) = \frac{1}{\sqrt{X^2 + Y^2 + Z^2}}(X, Y, Z)$$

- Convert to spherical coordinates
 $(\sin\theta\cos\phi, \sin\phi, \cos\theta\cos\phi) = (\hat{x}, \hat{y}, \hat{z})$
- Convert to spherical image coordinates

$$(\tilde{x}, \tilde{y}) = (s\theta, s\phi) + (\tilde{x}_c, \tilde{y}_c)$$

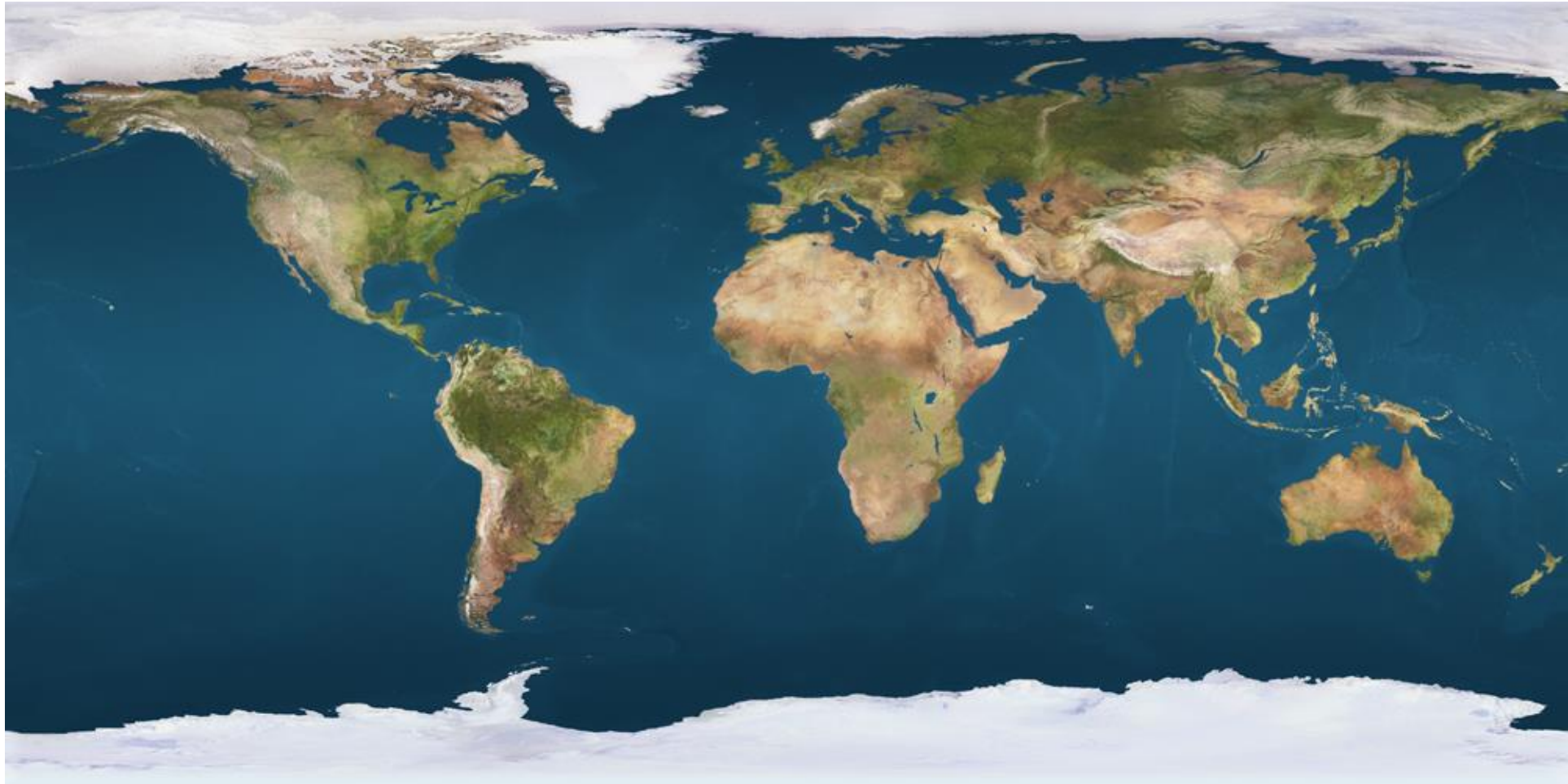
- s defines size of the final image
» often convenient to set $s = \text{camera focal length}$



Unwrapping a sphere



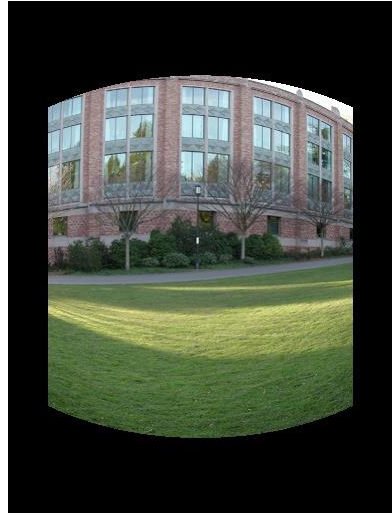
Credit: JHT's Planetary Pixel Emporium



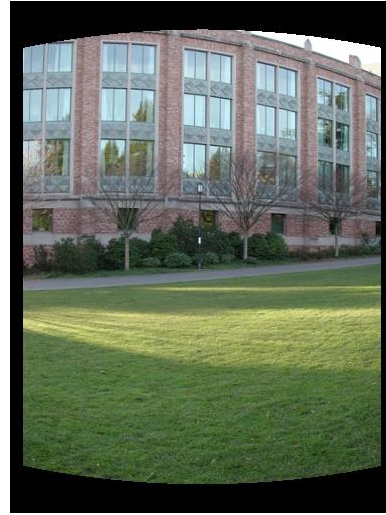
Spherical reprojection



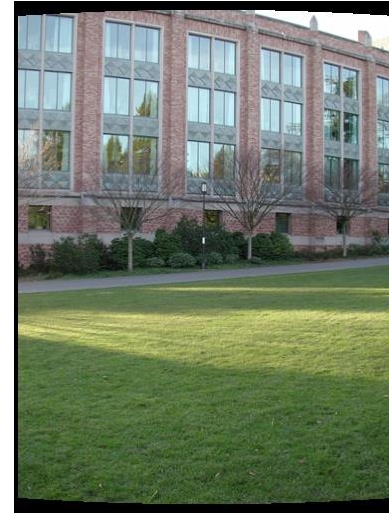
input



$f = 200$ (pixels)



$f = 400$



$f = 800$

- Map image to spherical coordinates
 - need to know the focal length

Aligning spherical images



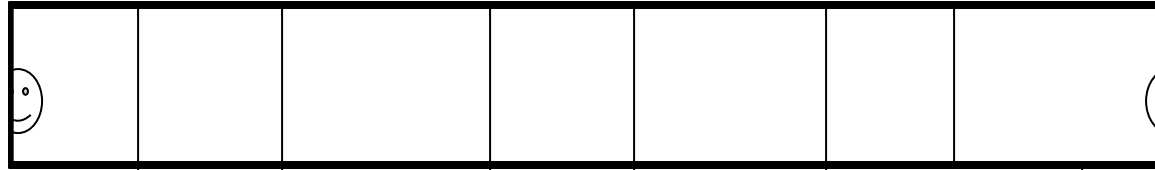
- Suppose we rotate the camera by θ about the vertical axis
 - How does this change the spherical image?

Aligning spherical images



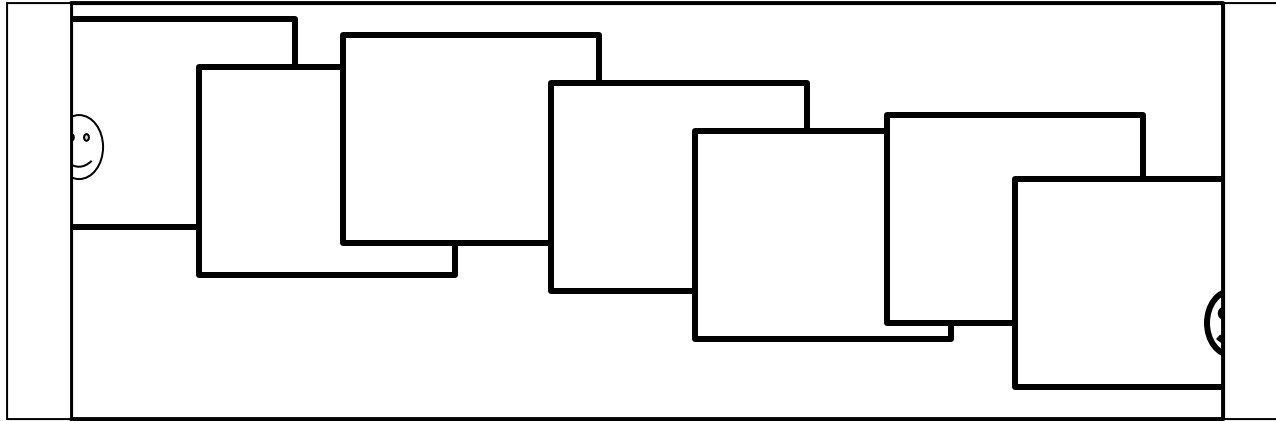
- Suppose we rotate the camera by θ about the vertical axis
 - How does this change the spherical image?
 - Translation by θ
 - This means that we can align spherical images by translation

Assembling the panorama



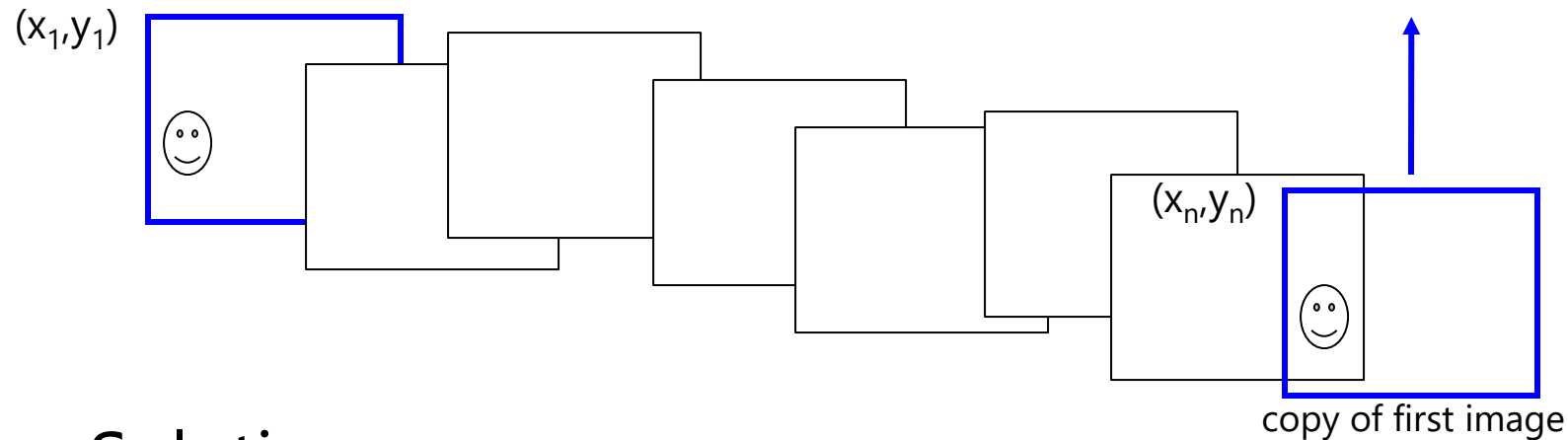
- Stitch pairs together, blend, then crop

Problem: Drift



- Error accumulation
 - small errors accumulate over time

Problem: Drift



- Solution

- add another copy of first image at the end
- this gives a constraint: $y_n = y_1$
- there are a bunch of ways to solve this problem
 - add displacement of $(y_1 - y_n)/(n - 1)$ to each image after the first
 - **apply an affine warp: $y' = y + ax$ [you will implement this for P3]**
 - run a big optimization problem, incorporating this constraint
 - best solution, but more complicated
 - known as “bundle adjustment”

Project 3

1. Take pictures on a tripod (or handheld)
 2. Warp to spherical coordinates (not needed if using homographies to align images)
 3. Extract features
 4. Align neighboring pairs using feature matching + RANSAC
 5. Write out list of neighboring translations
 6. Correct for drift
 7. Read in warped images and blend them
 8. Crop the result and import into a viewer
- Roughly based on **Autostitch**
 - By Matthew Brown and David Lowe
 - <http://www.cs.ubc.ca/~mbrown/autostitch/autostitch.html>

Spherical panoramas



Microsoft Lobby: <http://www.acm.org/pubs/citations/proceedings/graph/258734/p251-szeliski>

Different projections are possible



Cube-map

Blending

- We've aligned the images – now what?

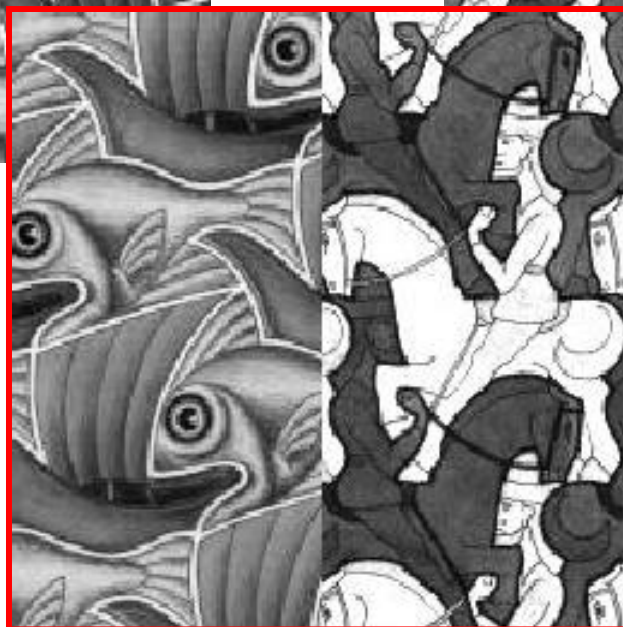
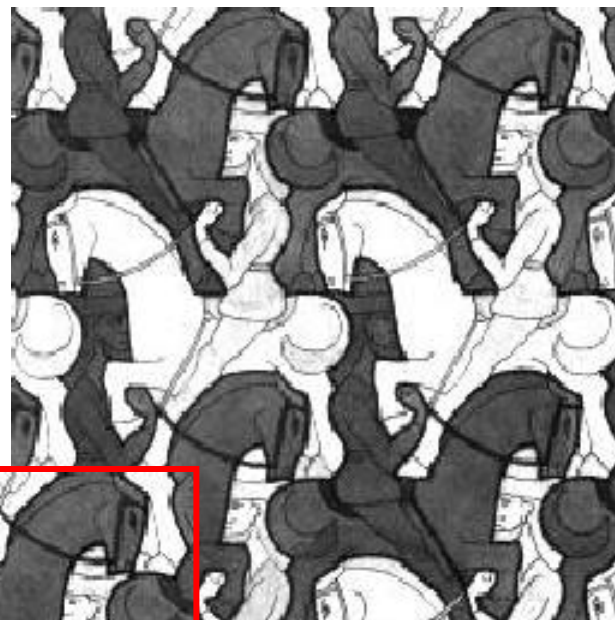
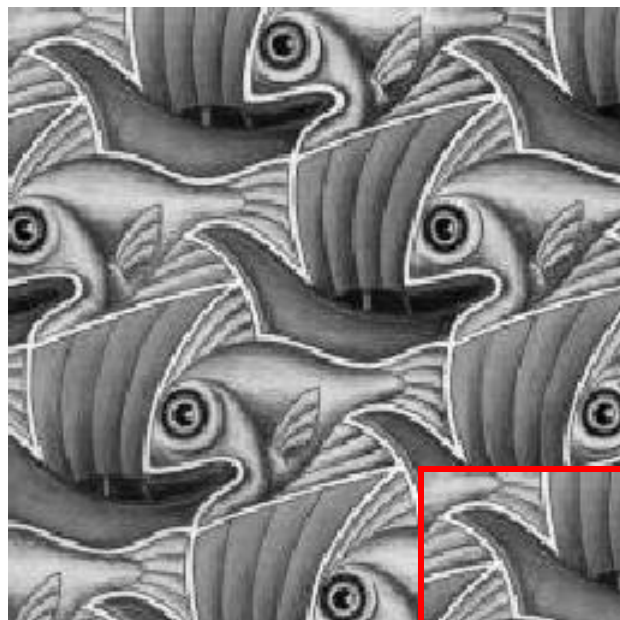


Blending

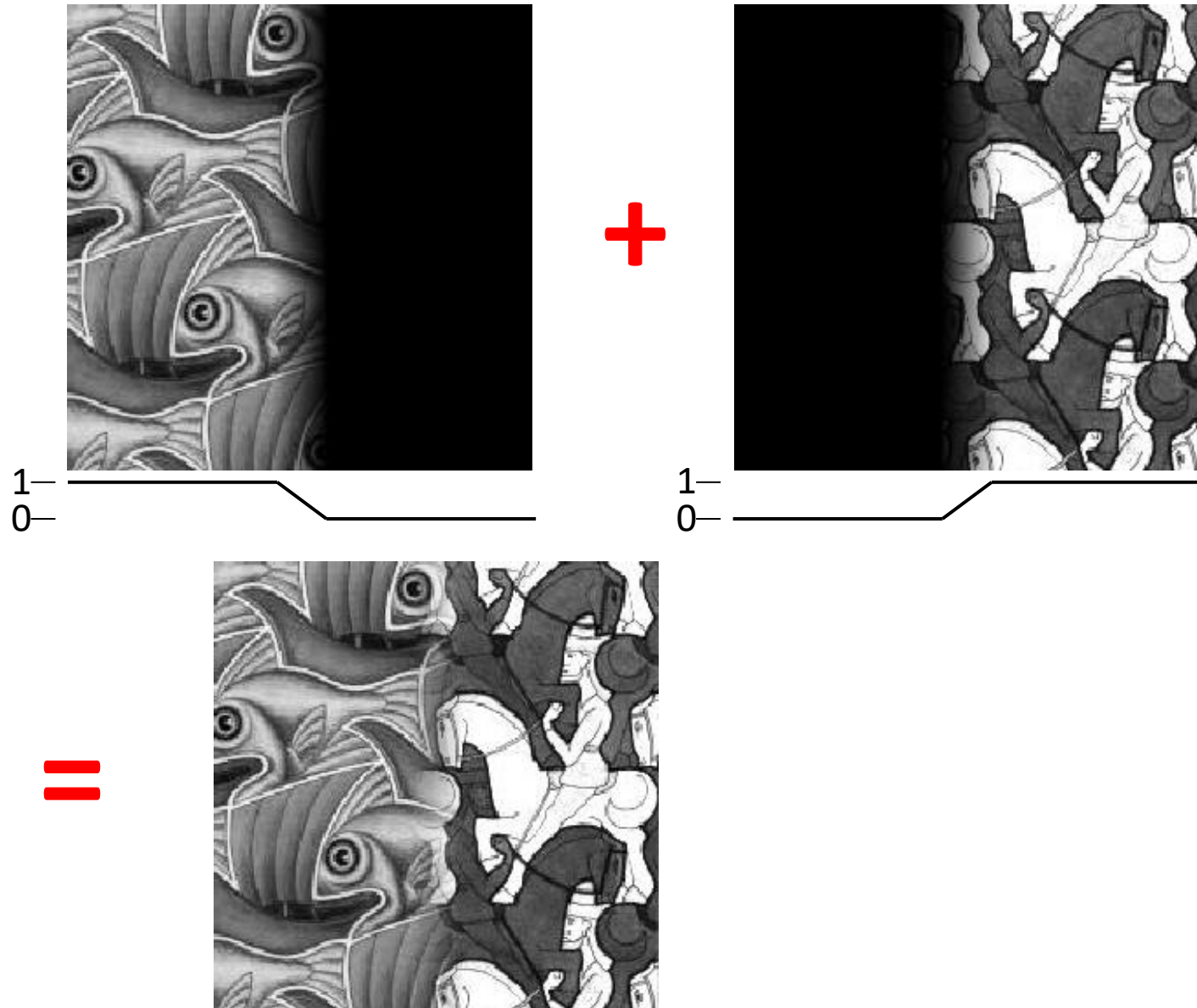
- Want to seamlessly blend them together



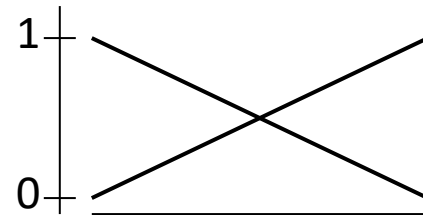
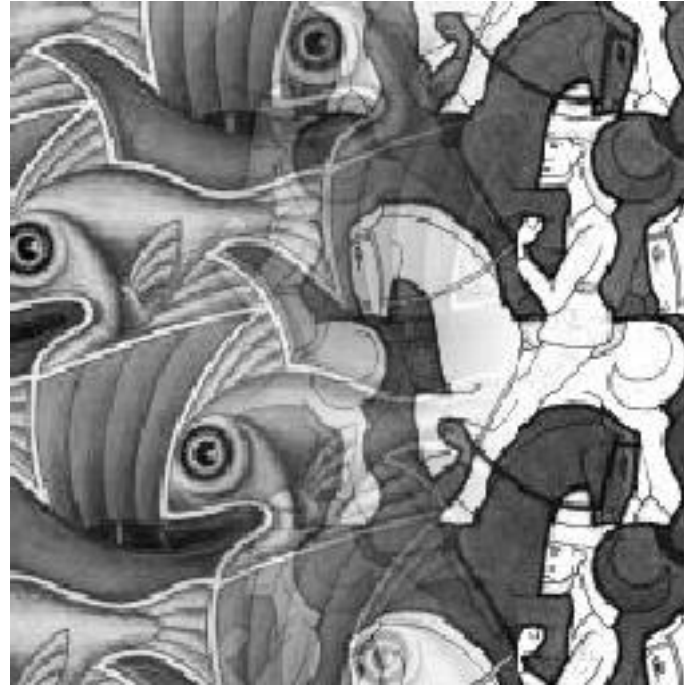
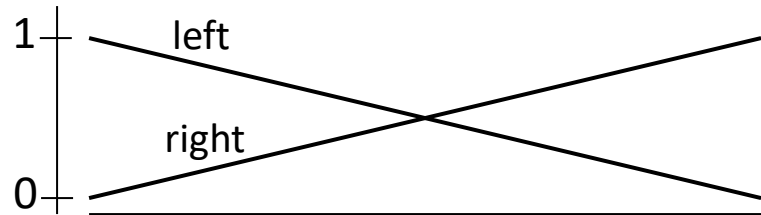
Image Blending



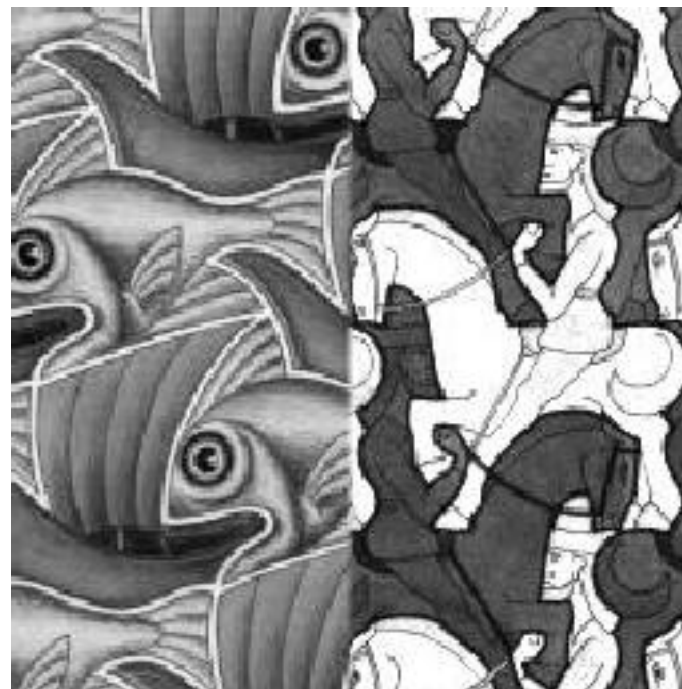
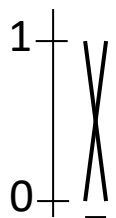
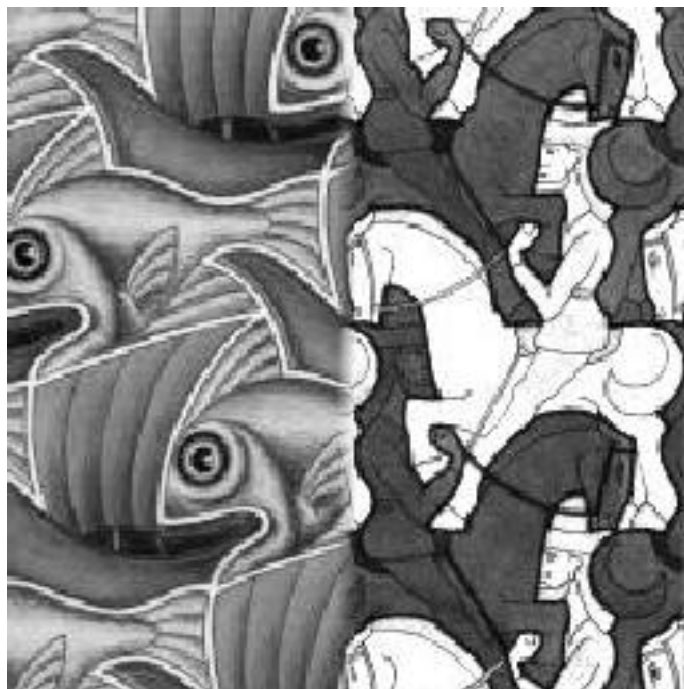
Feathering



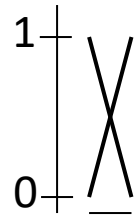
Effect of window size



Effect of window size



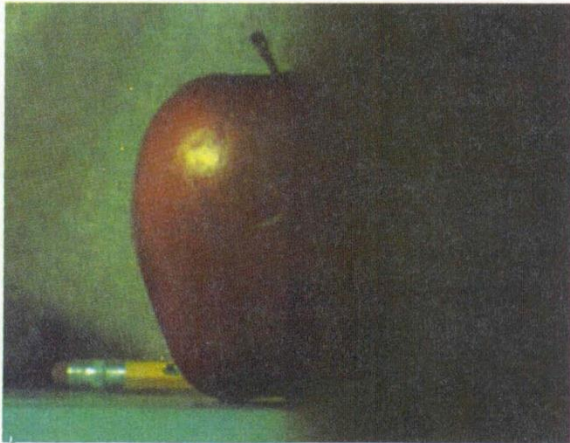
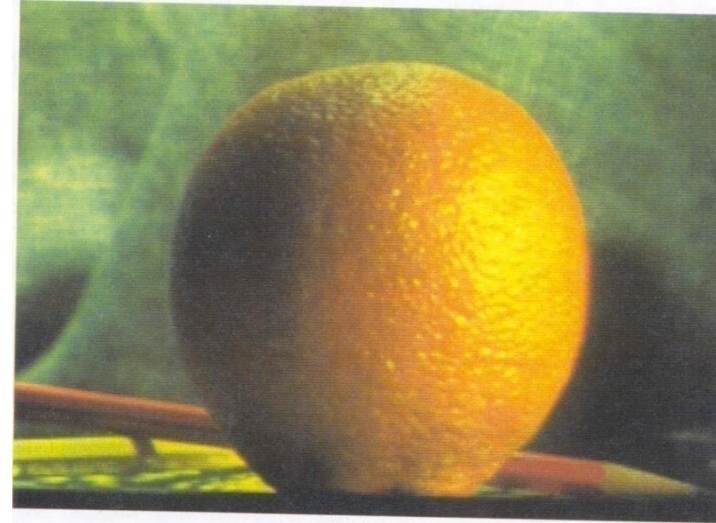
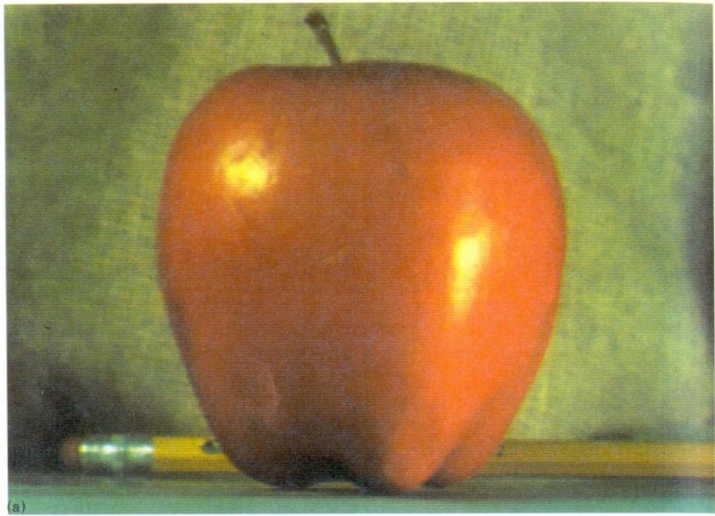
Good window size



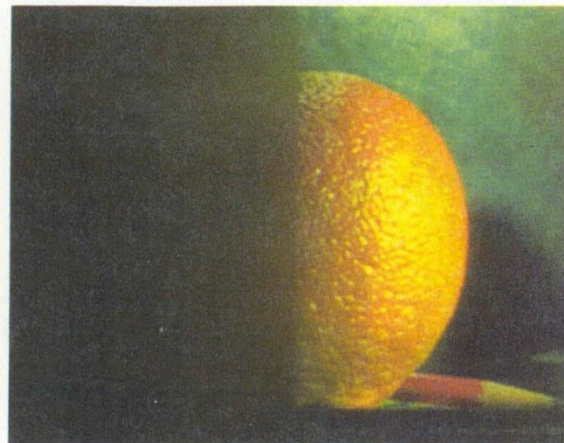
“Optimal” window: smooth but not ghosted

- Doesn't always work...

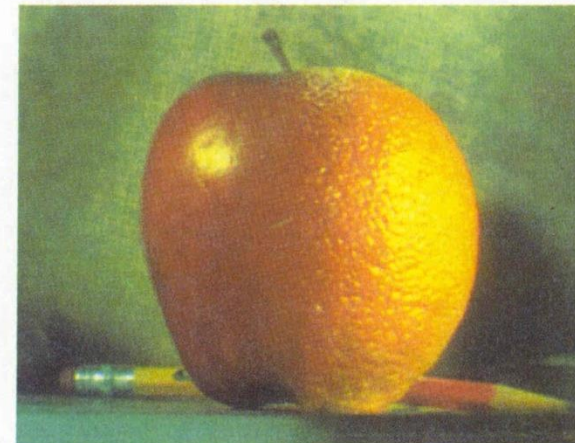
Pyramid blending



(d)



(h)

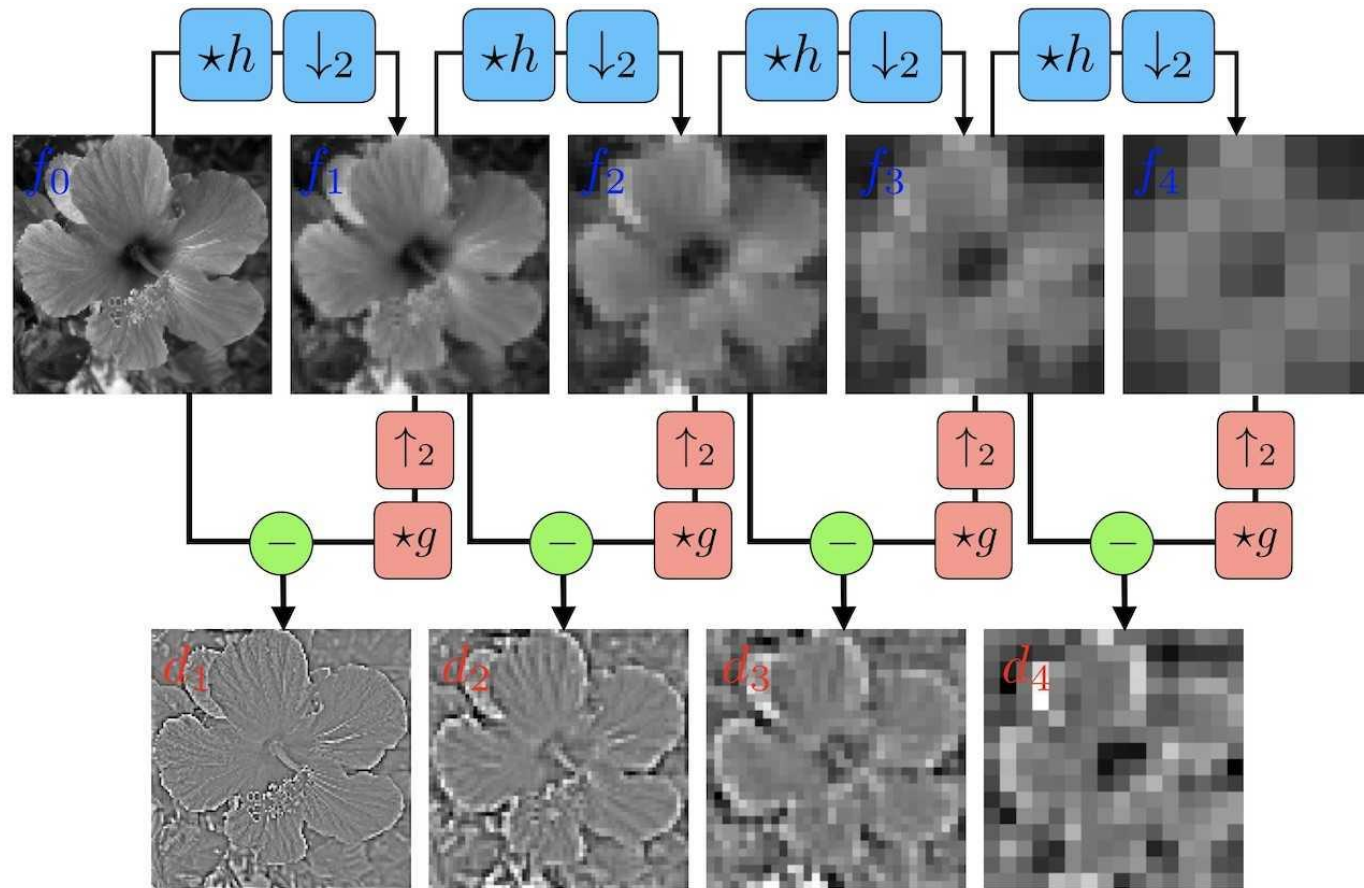


(l)

Create a Laplacian pyramid, blend each level

- Burt, P. J. and Adelson, E. H., [A multiresolution spline with applications to image mosaics](#), ACM Transactions on Graphics, 42(4), October 1983, 217-236.

The Laplacian Pyramid



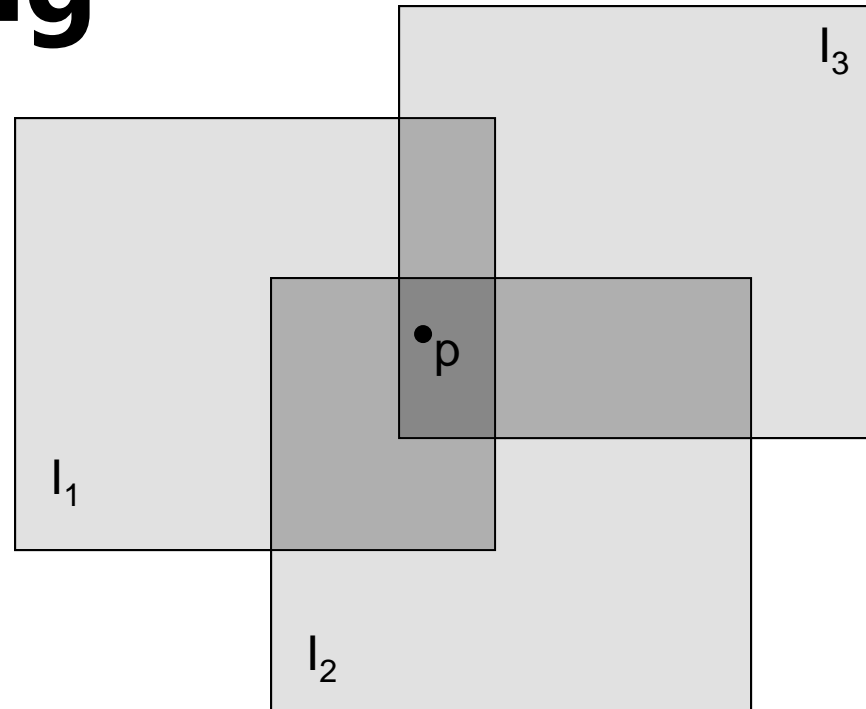
Forward transform:

$$f_j = (f_{j-1} \star h) \downarrow_2$$
$$d_j = f_j - (f_{j-1} \uparrow_2) \star g$$

Backward transform:

$$f_j = d_j + (f_{j-1} \uparrow_2) \star g$$

Alpha Blending



see Blinn (CGA, 1994) for details:

[Compositing, Part 1: Theory](#)

Encoding blend weights: $I(x,y) = (\alpha R, \alpha G, \alpha B, \alpha)$

color at $p = \frac{(\alpha_1 R_1, \alpha_1 G_1, \alpha_1 B_1) + (\alpha_2 R_2, \alpha_2 G_2, \alpha_2 B_2) + (\alpha_3 R_3, \alpha_3 G_3, \alpha_3 B_3)}{\alpha_1 + \alpha_2 + \alpha_3}$

Implement this in two steps:

1. accumulate: add up the (α premultiplied) $RGB\alpha$ values at each pixel
2. normalize: divide each pixel's accumulated RGB by its α value

Q: what if $\alpha = 0$?

Poisson Image Editing



For more info: [Perez et al, SIGGRAPH 2003](#)

Some panorama examples



"Before SIGGRAPH Deadline" Photo credit: Doug Zongker

Some panorama examples

- Every image on Google Streetview



Magic: ghost removal



M. Uyttendaele, A. Eden, and R. Szeliski.
Eliminating ghosting and exposure artifacts in image mosaics.
ICCV 2001

Magic: ghost removal



M. Uyttendaele, A. Eden, and R. Szeliski.
Eliminating ghosting and exposure artifacts in image mosaics.
ICCV 2001

Other types of mosaics



- Can mosaic onto *any* surface if you know the geometry
 - See NASA's [Visible Earth project](#) for some stunning earth mosaics

An EPIC Eclipse



<https://earthobservatory.nasa.gov/images/87675/an-epic-eclipse>

Questions?

Alternative to feathering

- **Cut and fuse**

Interactive Digital Photomontage



Aseem Agarwala, Mira Dontcheva
Maneesh Agrawala, Steven Drucker, Alex Colburn
Brian Curless, David Salesin, Michael Cohen

