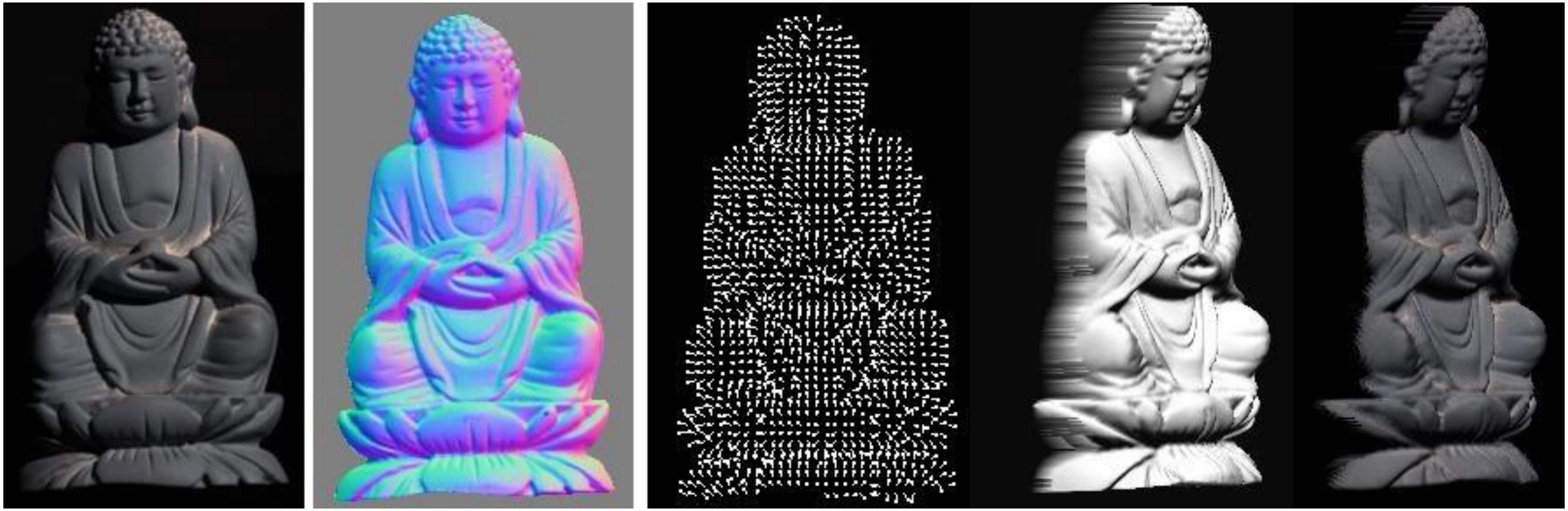
CS5670 : Computer Vision

Noah Snavely

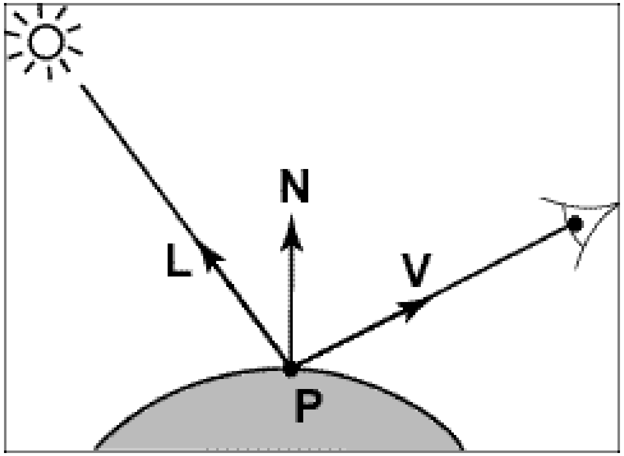
Photometric stereo



Announcements

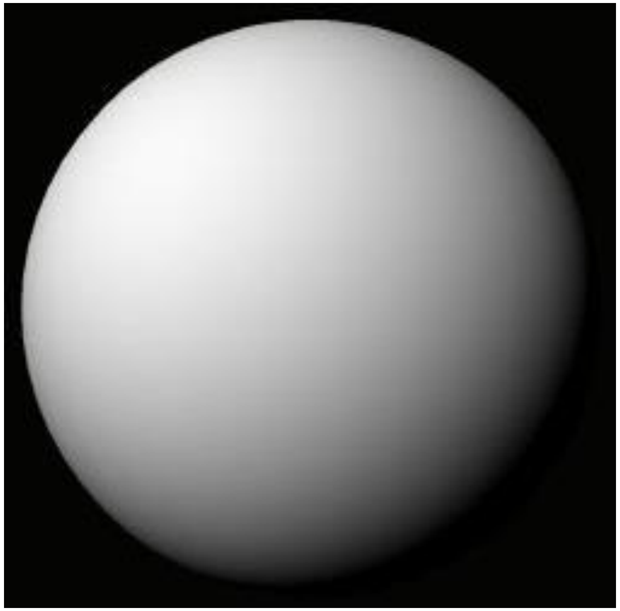
- Project 3 code due tomorrow, 3/29, by 11:59pm to CMS
  - Artifact due Friday, 3/30, by 11:59pm to CMS

Recap:
Lambertian (Diffuse) Reflectance

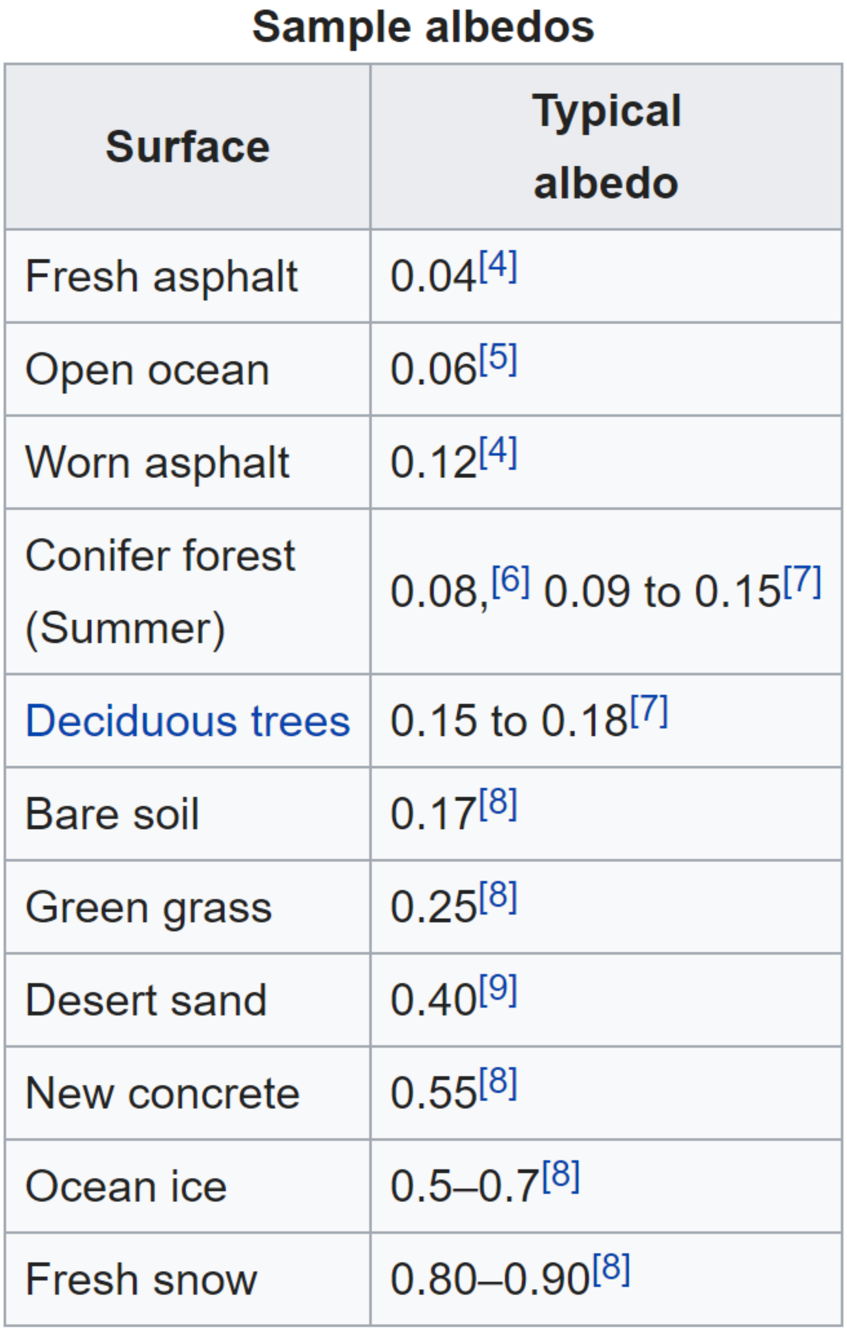


$$I = k_d \mathbf{N} \cdot \mathbf{L}$$

- I : observed image intensity
- k_d : object albedo
- $\mathbf{N}$: surface normal
- $\mathbf{L}$: light source direction

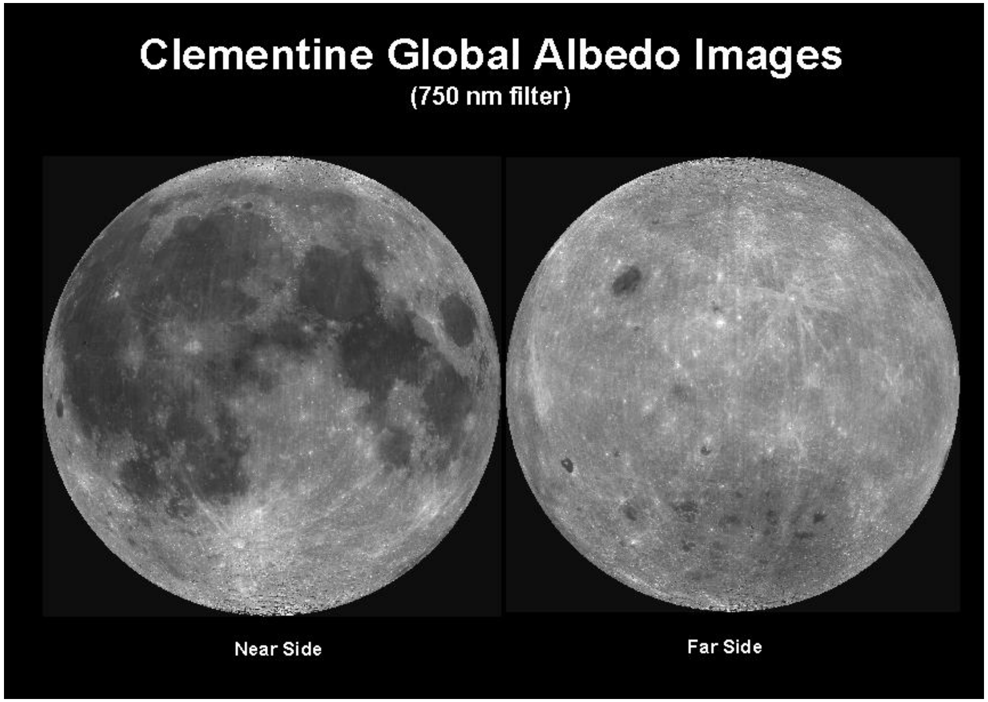


Lambertian sphere with constant albedo lit by a directional light source



Sample albedos

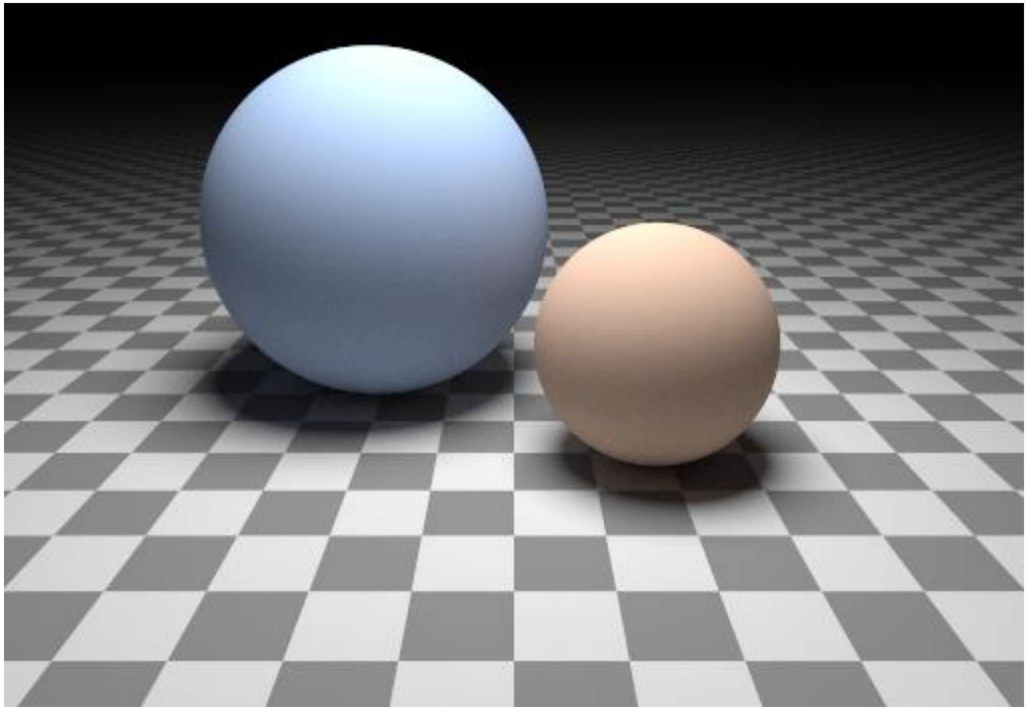
Surface	Typical albedo
Fresh asphalt	0.04[4]
Open ocean	0.06[5]
Worn asphalt	0.12[4]
Conifer forest (Summer)	0.08,[6] 0.09 to 0.15[7]
Deciduous trees	0.15 to 0.18[7]
Bare soil	0.17[8]
Green grass	0.25[8]
Desert sand	0.40[9]
New concrete	0.55[8]
Ocean ice	0.5–0.7[8]
Fresh snow	0.80–0.90[8]



Objects can have varying albedo and albedo varies with wavelength

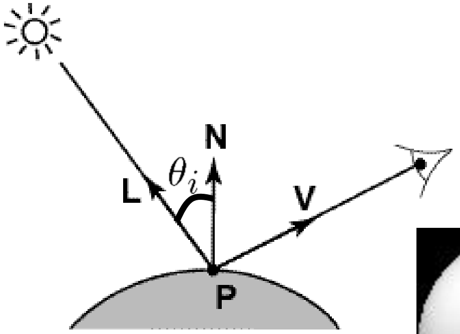
Source:
https://en.wikipedia.org/wiki/Albedo

Can we determine shape from lighting?



- Are these spheres?
  - Or just flat discs painted with varying albedo?

Shape from shading



Suppose $k_d = 1$

$$\begin{aligned} I &= k_d \mathbf{N} \cdot \mathbf{L} \\ &= \mathbf{N} \cdot \mathbf{L} \\ &= cos\ \theta_i \end{aligned}$$

You can directly measure angle between normal and light source

- Not quite enough information to compute surface shape
- But can be if you add some additional info, for example
  - assume a few of the normals are known (e.g., along silhouette)
  - constraints on neighboring normals—“integrability”
  - smoothness
- Hard to get it to work well in practice
  - plus, how many real objects have constant albedo?

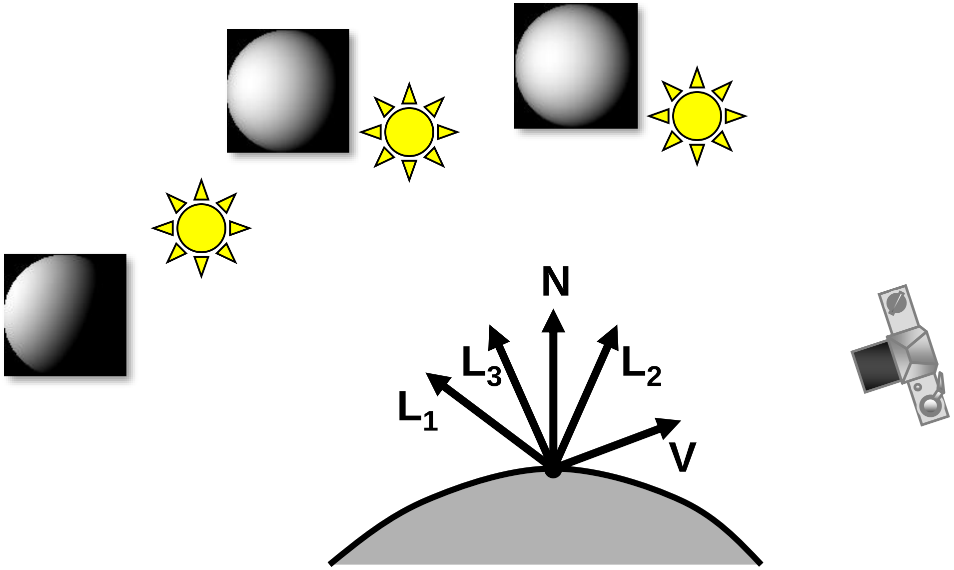
Application: Detecting composite photos

Real photo

Fake photo

Let’s take more than one photo!

Photometric stereo



$$\begin{aligned} I_1 &= k_d \mathbf{N} \cdot \mathbf{L_1} \\ I_2 &= k_d \mathbf{N} \cdot \mathbf{L_2} \\ I_3 &= k_d \mathbf{N} \cdot \mathbf{L_3} \end{aligned}$$

Can write this as a matrix equation:

$$\begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix} = k_d \begin{bmatrix} \mathbf{L_1}^T \\ \mathbf{L_2}^T \\ \mathbf{L_3}^T \end{bmatrix} \mathbf{N}$$

Solving the equations

$$\underbrace{\begin{bmatrix} I_1 \\ I_2 \\ I_3 \end{bmatrix}}_{\substack{\mathbf{I} \\ 3 \times 1}} = \underbrace{\begin{bmatrix} \mathbf{L_1}^T \\ \mathbf{L_2}^T \\ \mathbf{L_3}^T \end{bmatrix}}_{\substack{\mathbf{L} \\ 3 \times 3}} \underbrace{k_d \mathbf{N}}_{\substack{\mathbf{G} \\ 3 \times 1}}$$

$$\mathbf{G} = \mathbf{L}^{-1} \mathbf{I}$$

$$k_d = \|\mathbf{G}\|$$

$$\mathbf{N} = \frac{1}{k_d} \mathbf{G}$$

Solve one such linear system **per pixel** to solve for that pixel’s surface normal

More than three lights

Get better results by using more lights

$$\begin{bmatrix} I_1 \\ \vdots \\ I_n \end{bmatrix} = \begin{bmatrix} \mathbf{L_1} \\ \vdots \\ \mathbf{L_n} \end{bmatrix} k_d \mathbf{N}$$

Least squares solution:

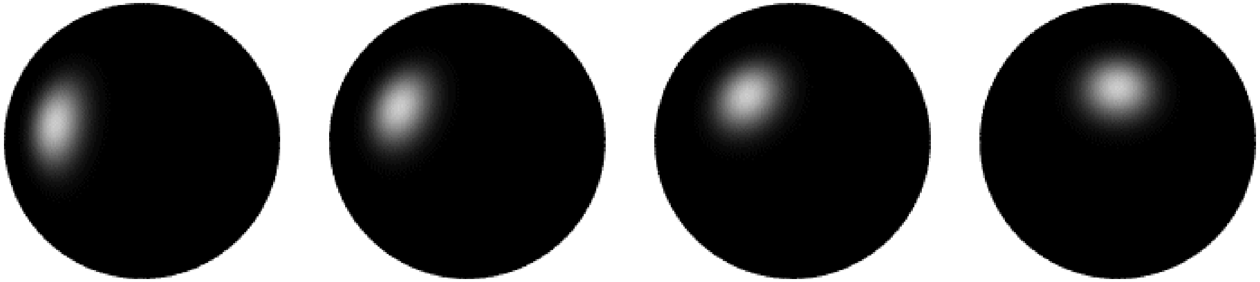
$$\begin{aligned} \mathbf{I} &= \mathbf{LG} \\ \mathbf{L^T I} &= \mathbf{L^T L G} \\ \mathbf{G} &= (\mathbf{L^T L})^{-1} (\mathbf{L^T I}) \end{aligned}$$

Solve for N, k_d as before

What’s the size of $\mathbf{L^T L}$?

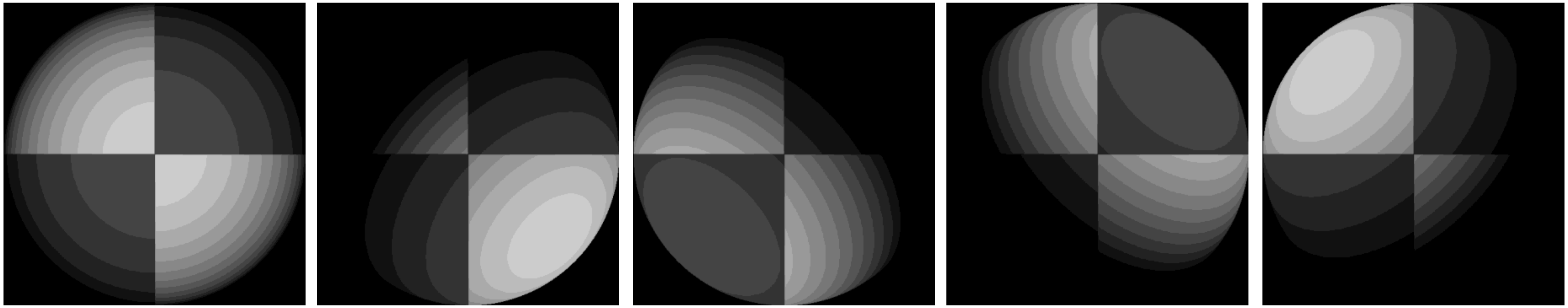
Computing light source directions

Trick: place a chrome sphere in the scene

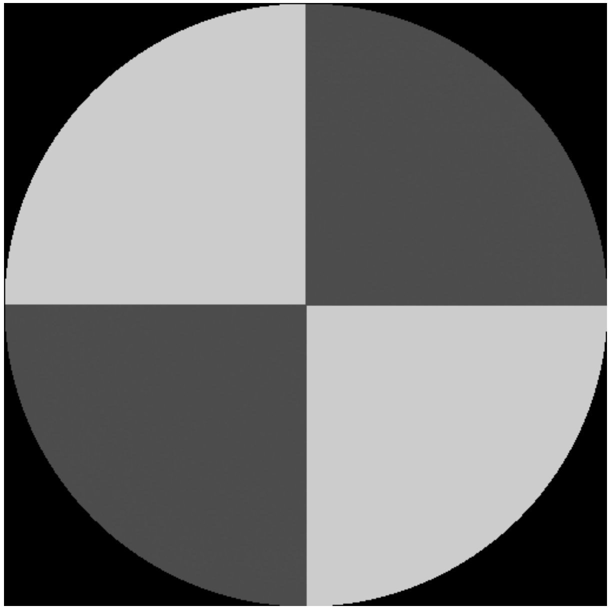


- the location of the highlight tells you where the light source is

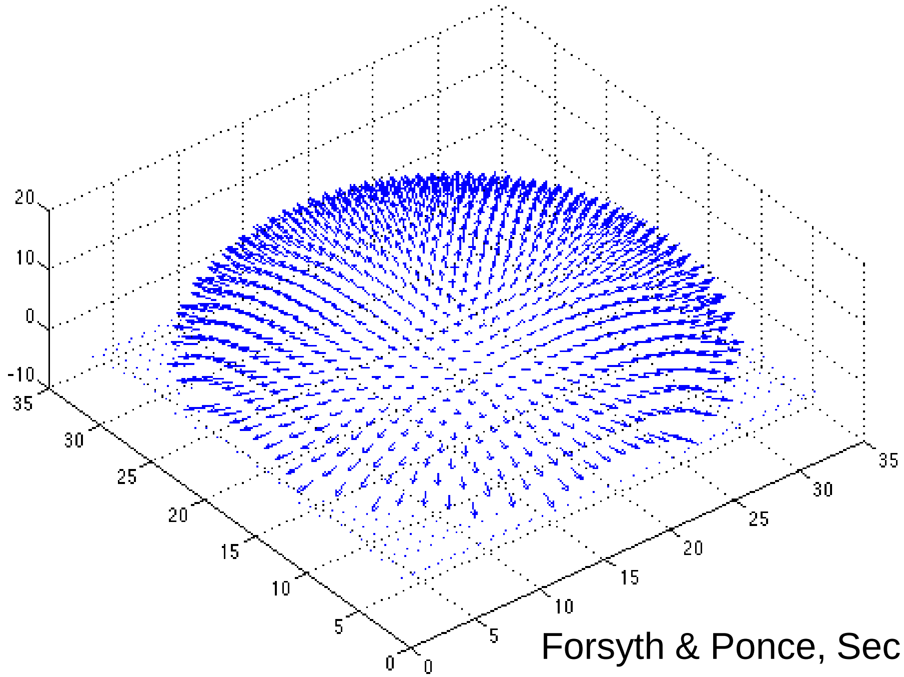
Example



Recovered albedo



Recovered normal field

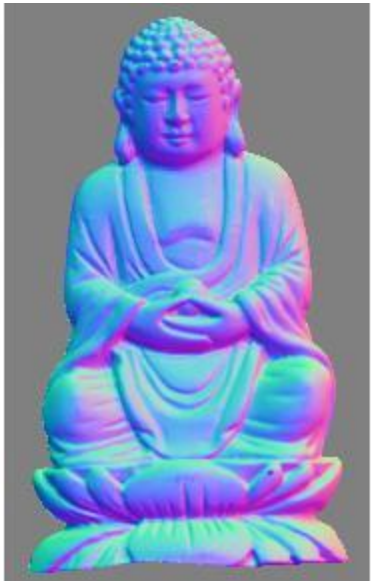


Forsyth & Ponce, Sec. 5.4

Depth from normals

- Solving the linear system per-pixel gives us an estimated surface normal for each pixel

Input photo



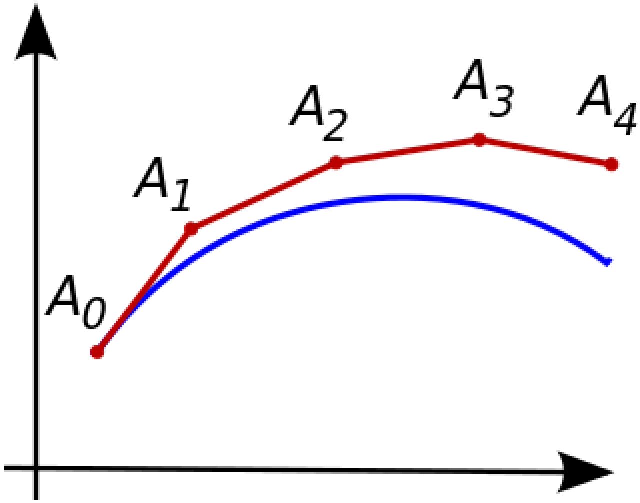
Estimated normals

Estimated normals
(needle diagram)

- How can we compute depth from normals?
  - Normals are like the “derivative” of the true depth

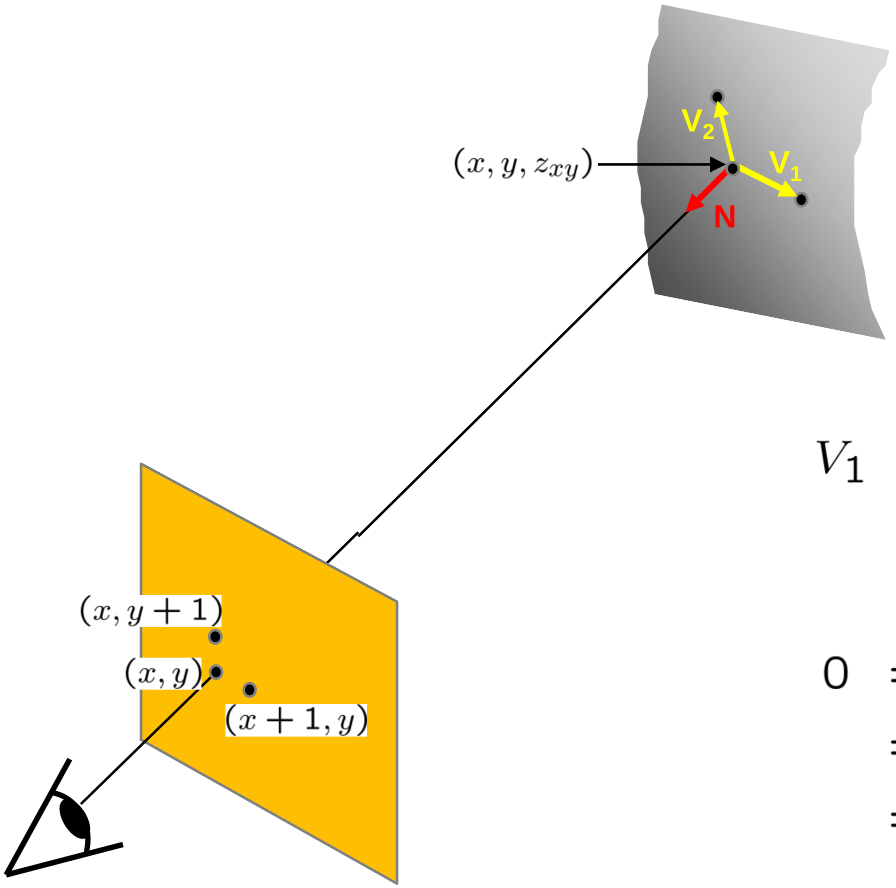
Normal Integration

- Integrating a set of derivatives is easy in 1D
    - (similar to Euler's method from diff. eq. class)



- Could just integrate normals in each column / row separately
- Instead, we formulate as a linear system and solve for depths that *best agree with the surface normals*

Depth from normals



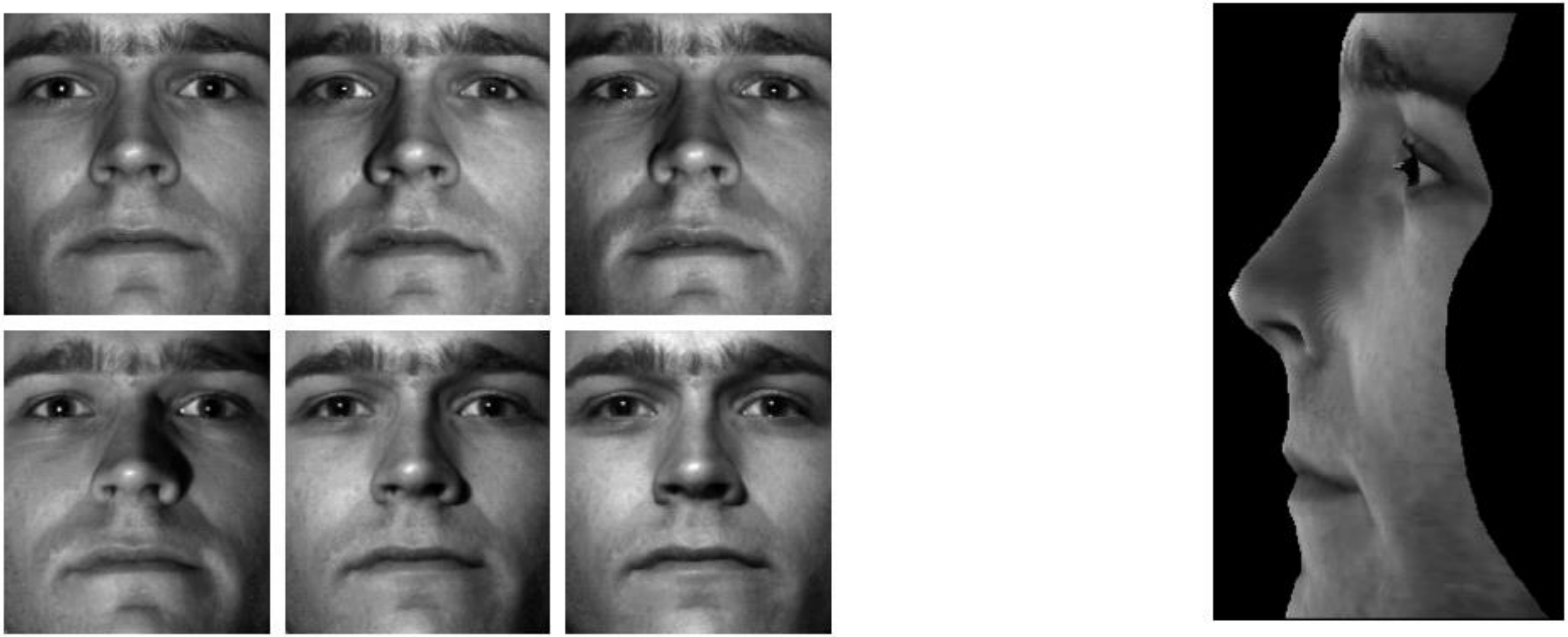
$$\begin{aligned} V_1 &= (x+1, y, z_{x+1,y}) - (x, y, z_{xy}) \\ &= (1, 0, z_{x+1,y} - z_{xy}) \end{aligned}$$

$$\begin{aligned} 0 &= N \cdot V_1 \\ &= (n_x, n_y, n_z) \cdot (1, 0, z_{x+1,y} - z_{xy}) \\ &= n_x + n_z(z_{x+1,y} - z_{xy}) \end{aligned}$$

Get a similar equation for **V_2**

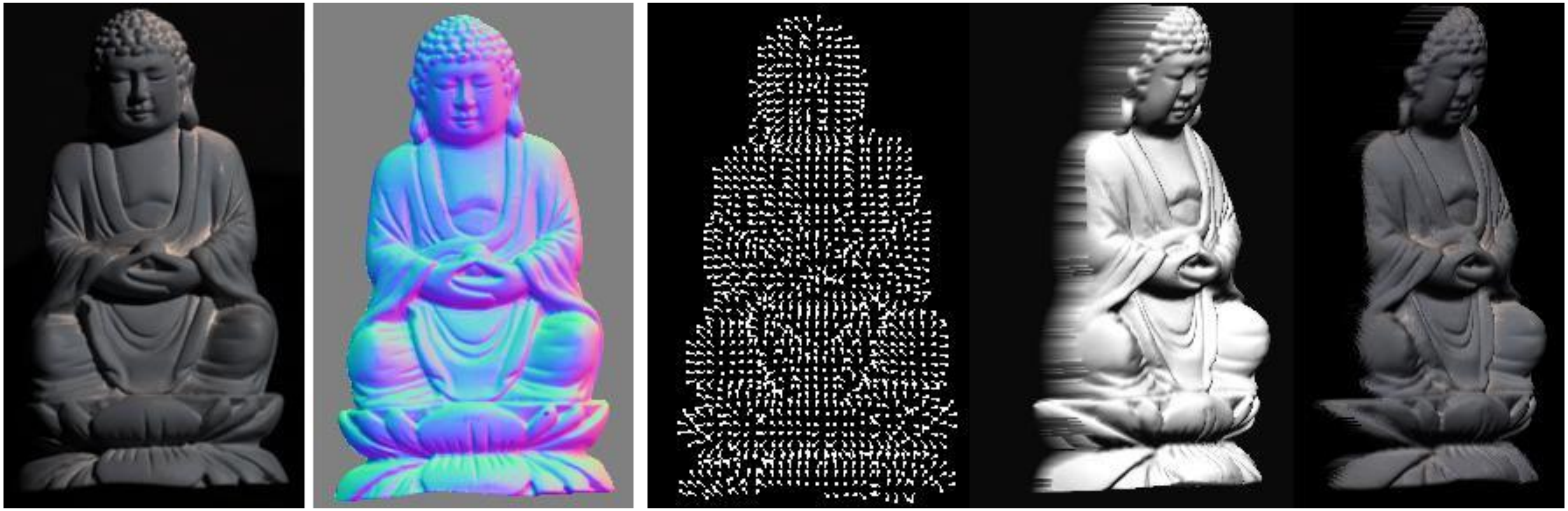
- Each normal gives us two linear constraints on z
- compute z values by solving a matrix equation

Results



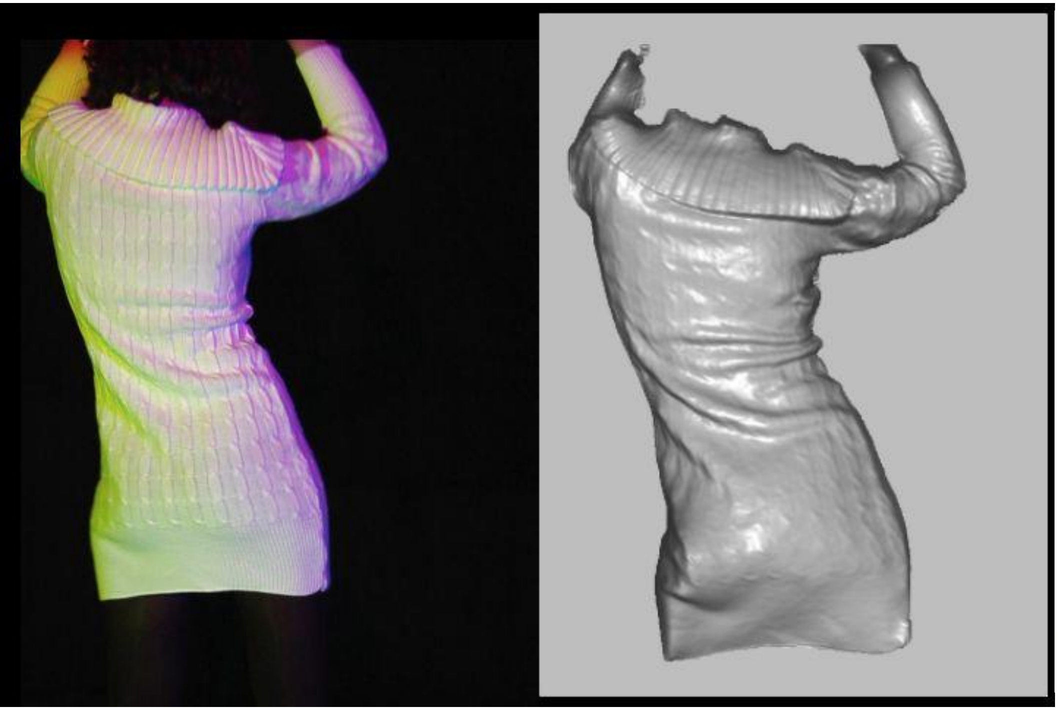
from Athos Georghiades

Results



Extension

Photometric Stereo from Colored Lighting



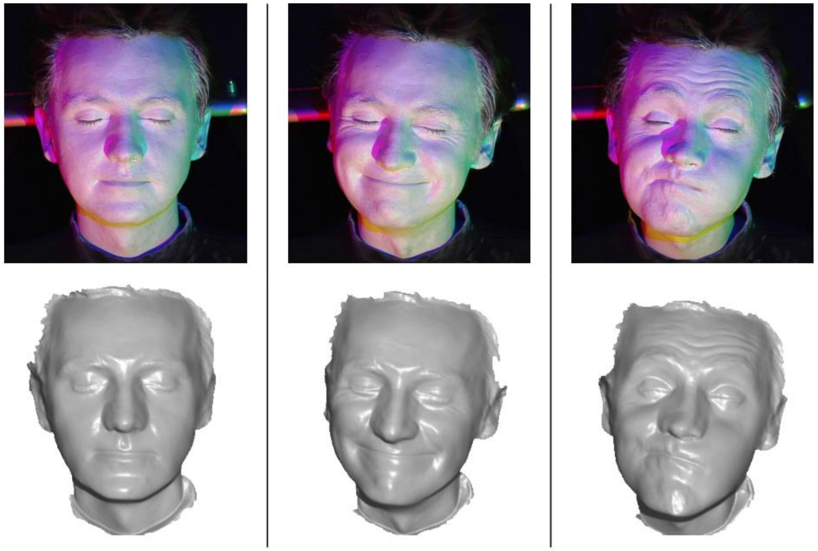


Fig. 2. **Applying the original algorithm to a face with white makeup.** Top: example input frames from video of an actor smiling and grimacing. Bottom: the resulting integrated surfaces.

Video Normals from Colored Lights
Gabriel J. Brostow, Carlos Hernández, George Vogiatzis, Björn Stenger, Roberto Cipolla
IEEE TPAMI, Vol. 33, No. 10, pages 2104-2114, October 2011.

Questions?

For now, ignore specular reflection

Slides from Photometric Methods for 3D Modeling, Matsushita, Wilburn, Ben-Ezra

And Refraction…

Slides from Photometric Methods for 3D Modeling, Matsushita, Wilburn, Ben-Ezra

And Interreflections…

Slides from Photometric Methods for 3D Modeling, Matsushita, Wilburn, Ben-Ezra

And Subsurface Scattering…

Slides from Photometric Methods for 3D Modeling, Matsushita, Wilburn, Ben-Ezra

Limitations

Bigger problems

- doesn’t work for shiny things, semi-translucent things
- shadows, inter-reflections

Smaller problems

- camera and lights have to be distant
- calibration requirements
  - measure light source directions, intensities
  - camera response function

Newer work addresses some of these issues

Some pointers for further reading:

- Zickler, Belhumeur, and Kriegman, *"Helmholtz Stereopsis: Exploiting Reciprocity for Surface Reconstruction."* IJCV, Vol. 49 No. 2/3, pp 215-227.
- Hertzmann & Seitz, “*Example-Based Photometric Stereo: Shape Reconstruction with General, Varying BRDFs*.” IEEE Trans. PAMI 2005

Johnson and Adelson, 2009

Cookie

Paint

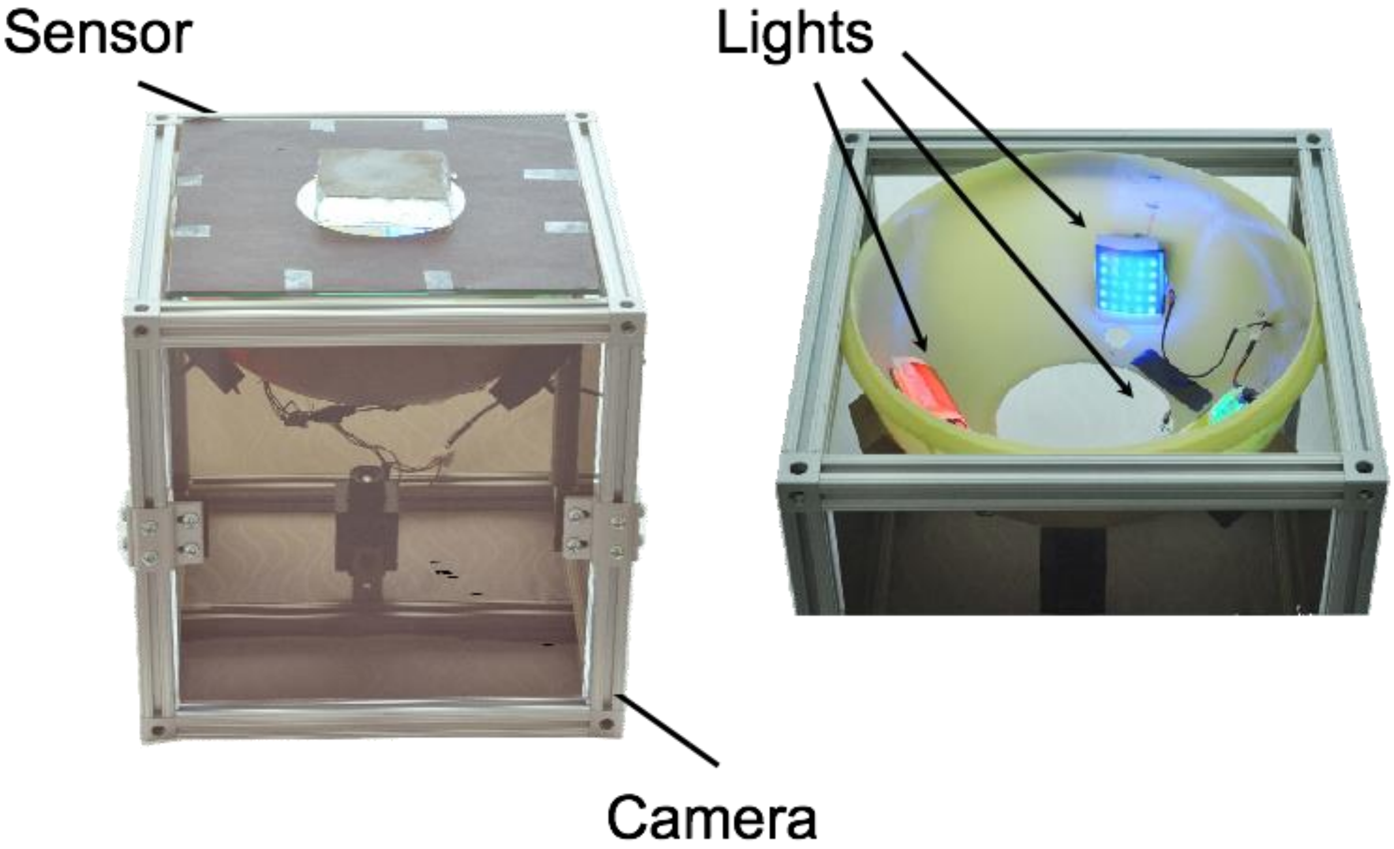
Clear Elastomer

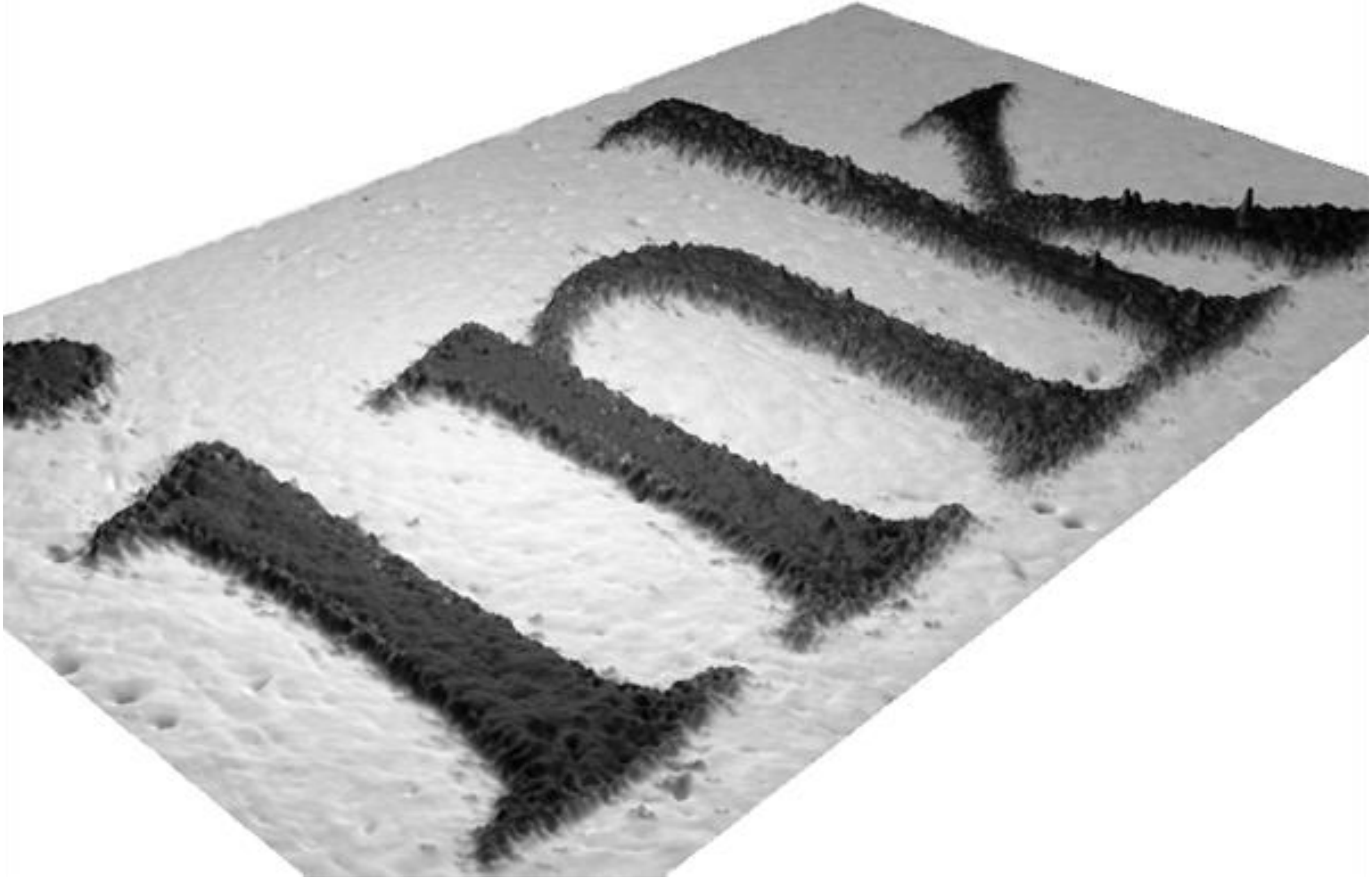
Johnson and Adelson, 2009

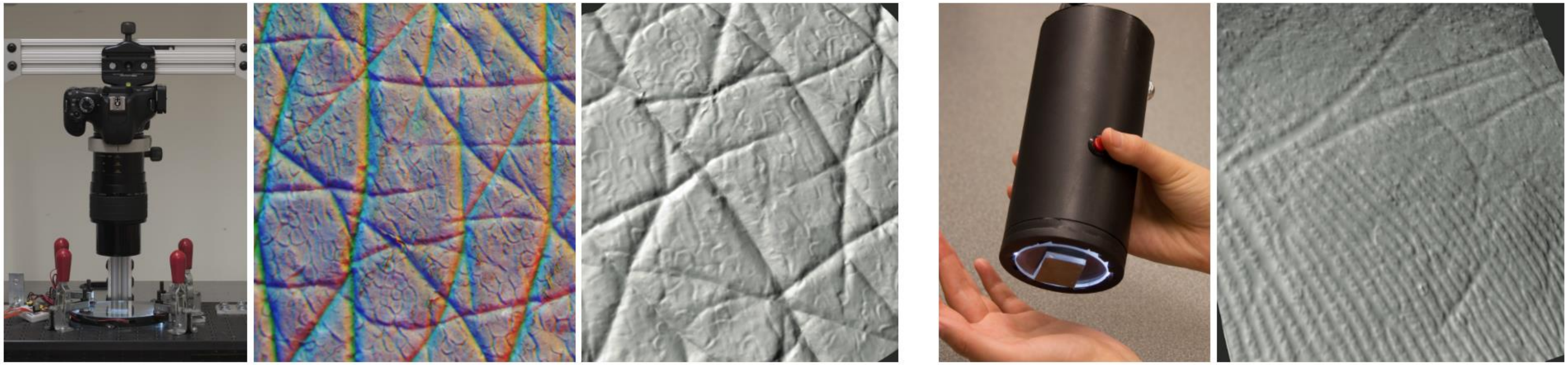

OREO

OREO

Lights, camera, action




ink



(a) bench configuration (b) captured (c) reconstruction (d) portable configuration (e) reconstruction

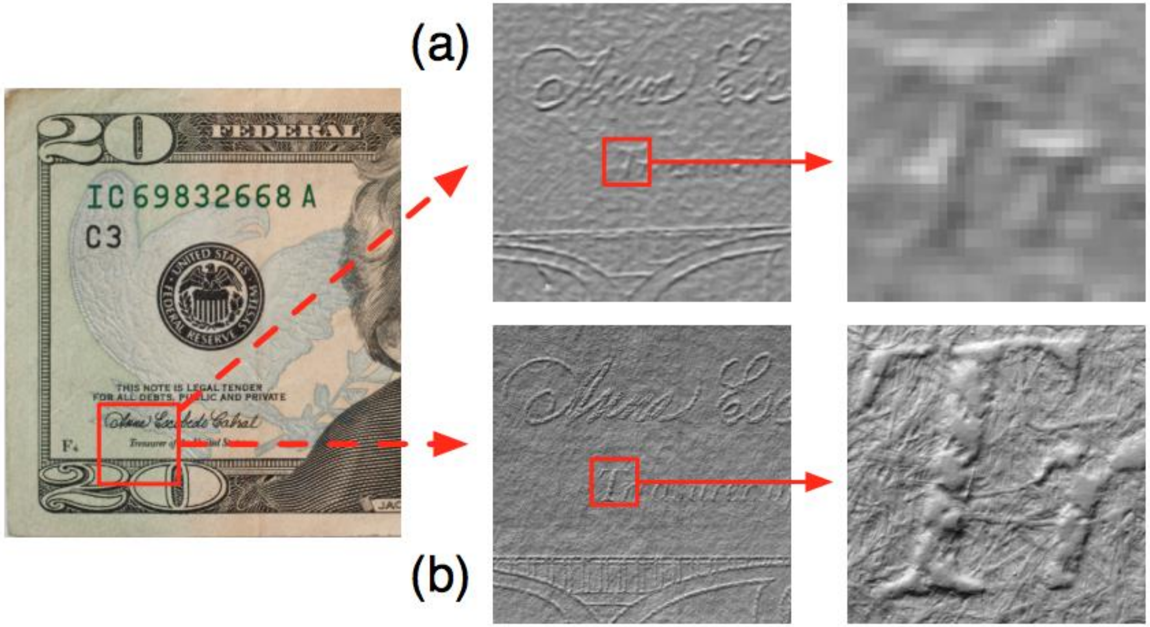
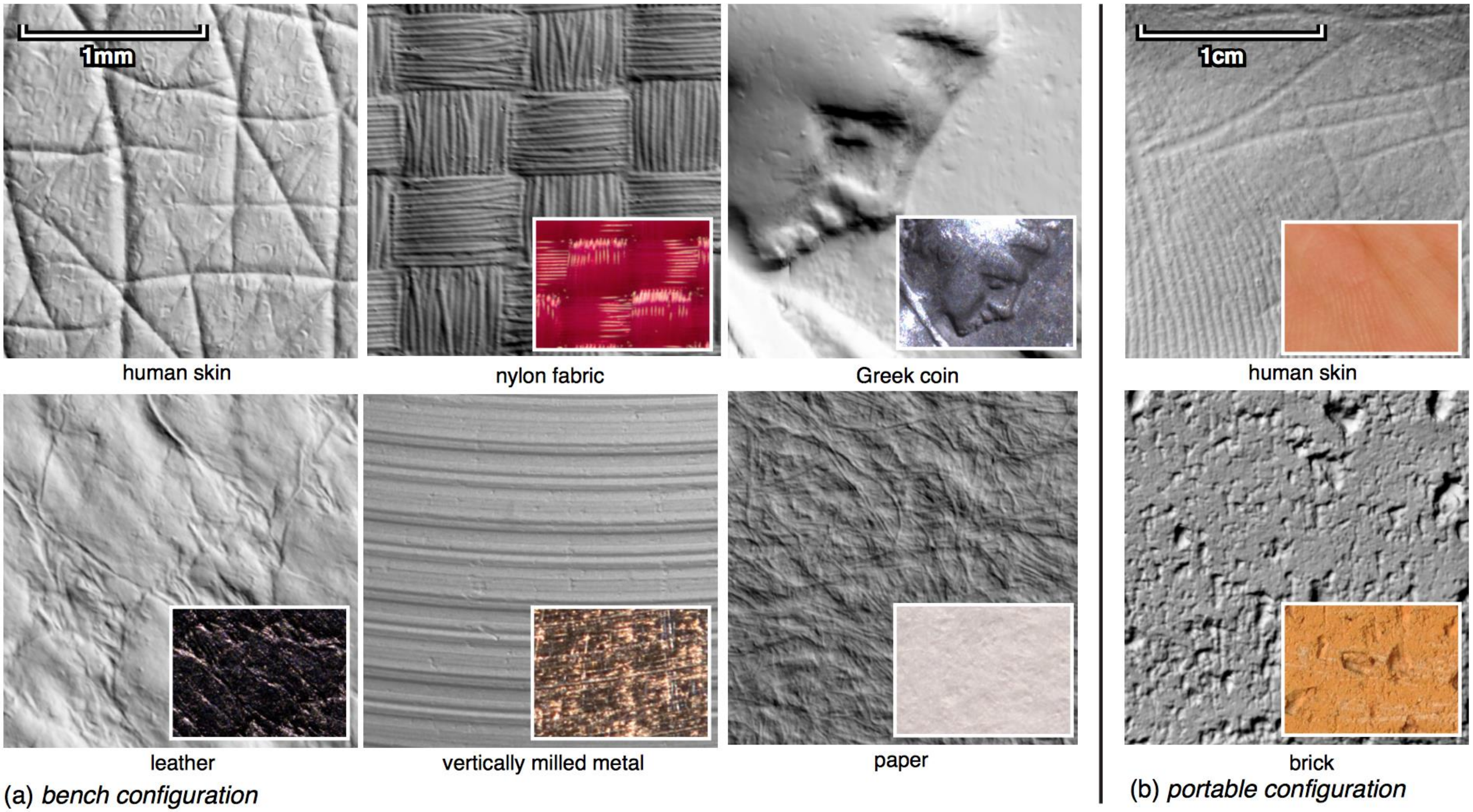


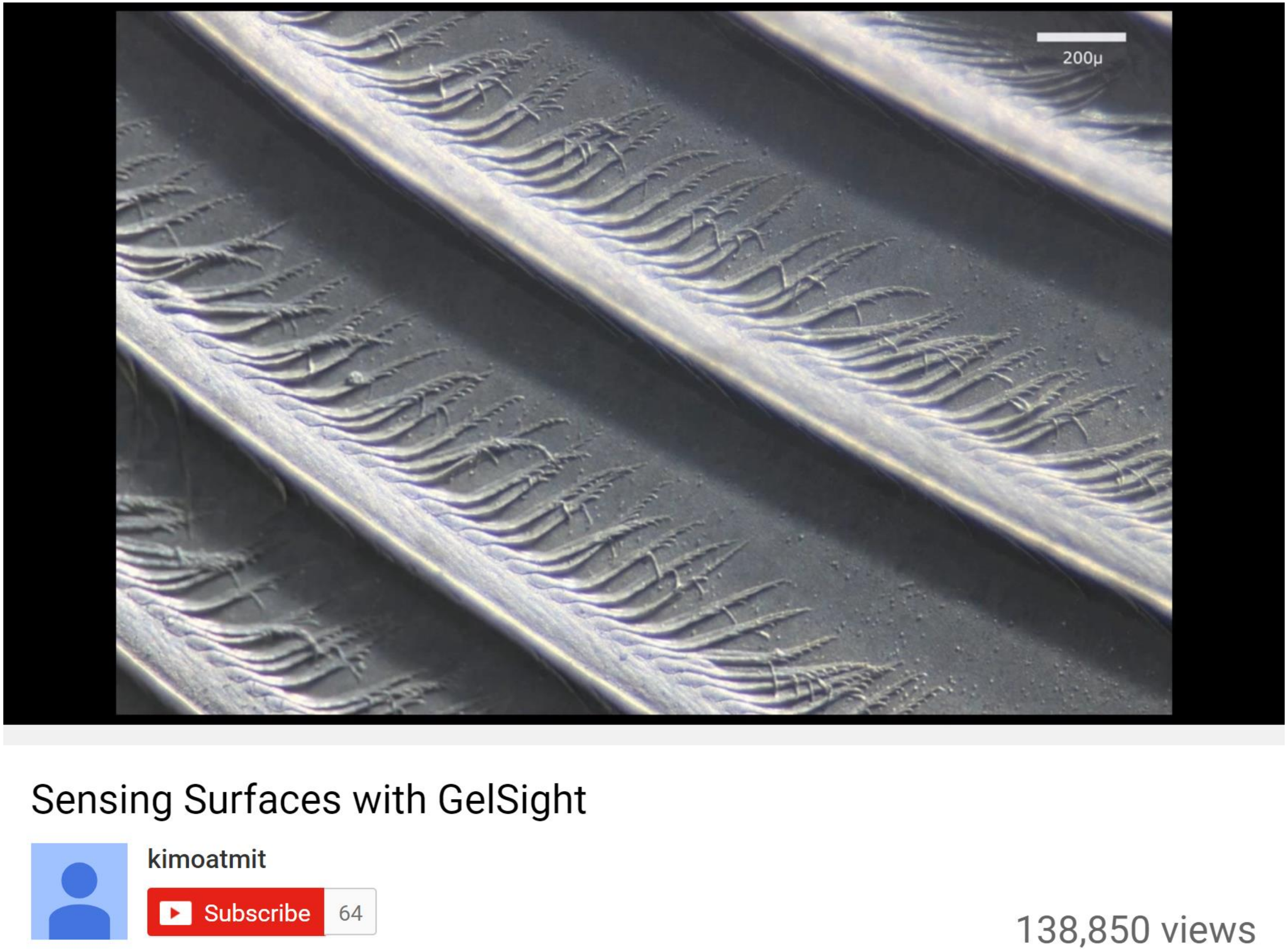
Figure 7: *Comparison with the high-resolution result from the original retrographic sensor. (a) Rendering of the high-resolution \$20 bill example from the original retrographic sensor with a close-up view. (b) Rendering of the captured geometry using our method.*



(a) *bench configuration*

(b) *portable configuration*

Figure 9: *Example geometry measured with the bench and portable configurations. Outer image: rendering under direct lighting. Inset: macro photograph of original sample. Scale shown in upper left. Color images are shown for context and are to similar, but not exact scale.*



Sensing Surfaces with GelSight

https://www.youtube.com/watch?v=S7gXih4XS7A

Questions?