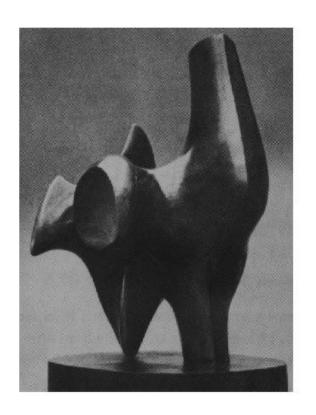
CS5670: Computer Vision Noah Snavely

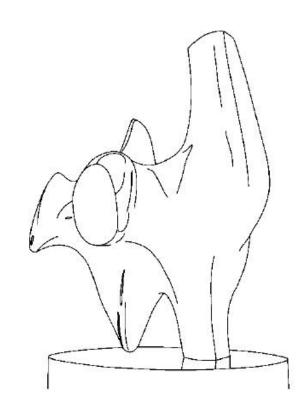
Lecture 2: Edge detection



From Sandlot Science

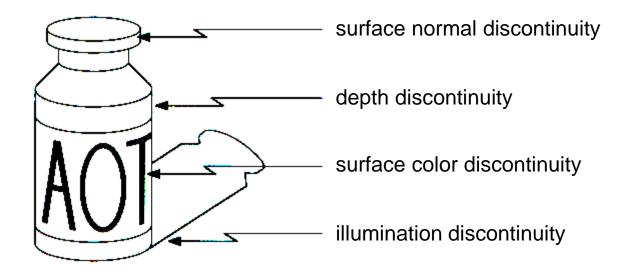
Edge detection





- Convert a 2D image into a set of curves
 - Extracts salient features of the scene
 - More compact than pixels

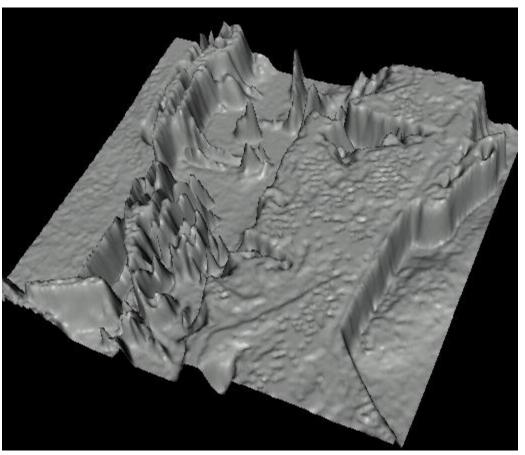
Origin of Edges



Edges are caused by a variety of factors

Images as functions...





 Edges look like steep cliffs

Characterizing edges

 An edge is a place of rapid change in the image intensity function

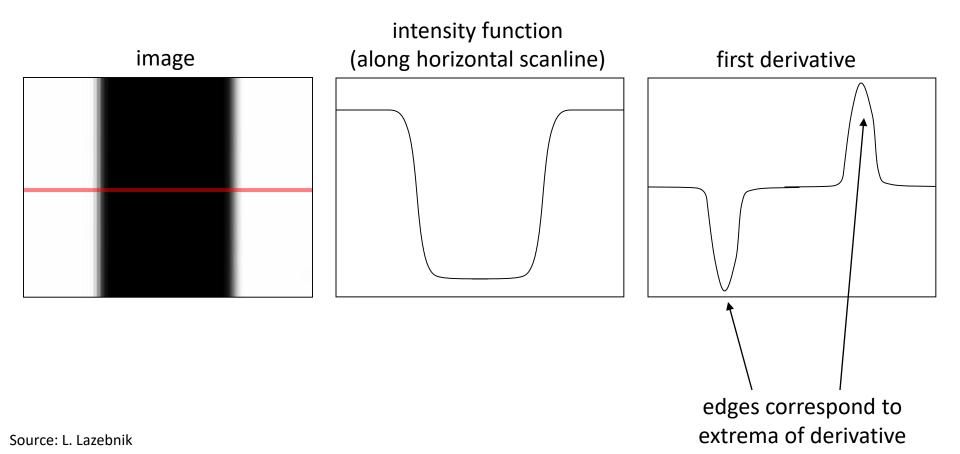
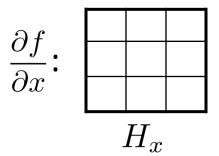


Image derivatives

- How can we differentiate a digital image F[x,y]?
 - Option 1: reconstruct a continuous image, f, then compute the derivative
 - Option 2: take discrete derivative (finite difference)

$$\frac{\partial f}{\partial x}[x,y] \approx F[x+1,y] - F[x,y]$$

How would you implement this as a linear filter?



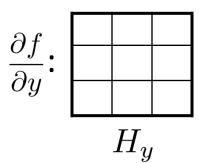


Image gradient

• The gradient of an image: $\nabla f = \left[\frac{\partial f}{\partial x}, \frac{\partial f}{\partial y}\right]$

The gradient points in the direction of most rapid increase in intensity

$$\nabla f = \begin{bmatrix} \frac{\partial f}{\partial x}, 0 \end{bmatrix}$$

$$\nabla f = \begin{bmatrix} \frac{\partial f}{\partial x}, \frac{\partial f}{\partial y} \end{bmatrix}$$

$$\nabla f = \begin{bmatrix} 0, \frac{\partial f}{\partial y} \end{bmatrix}$$

The *edge strength* is given by the gradient magnitude:

$$\|\nabla f\| = \sqrt{\left(\frac{\partial f}{\partial x}\right)^2 + \left(\frac{\partial f}{\partial y}\right)^2}$$

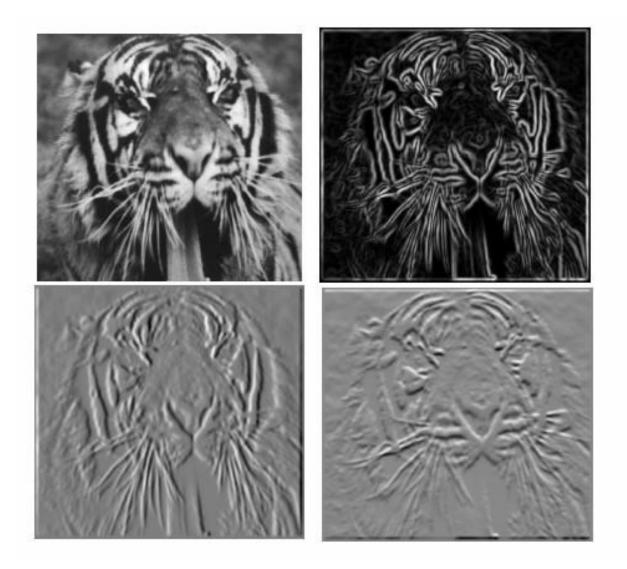
The gradient direction is given by:

$$\theta = \tan^{-1} \left(\frac{\partial f}{\partial y} / \frac{\partial f}{\partial x} \right)$$

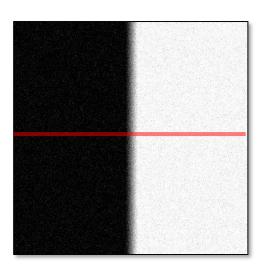
how does this relate to the direction of the edge?

Source: Steve Seitz

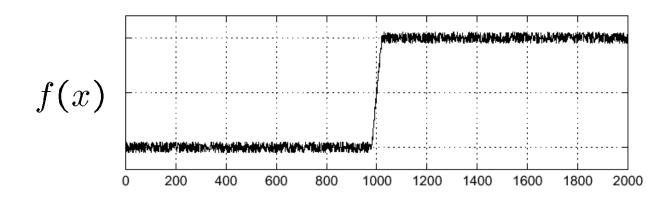
Image gradient

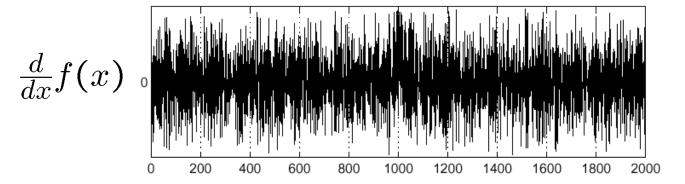


Effects of noise



Noisy input image

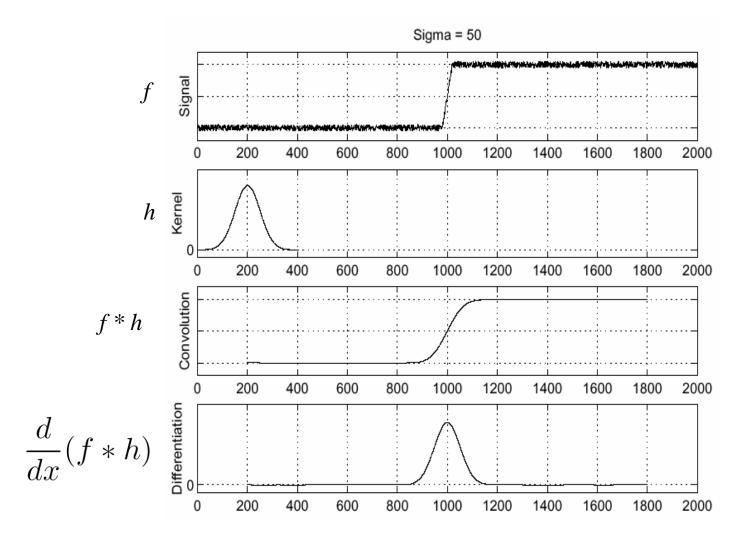




Where is the edge?

Source: S. Seitz

Solution: smooth first

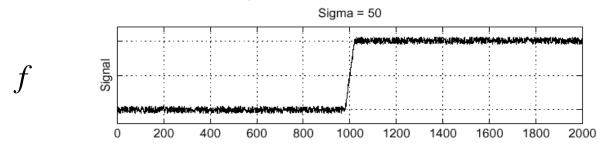


To find edges, look for peaks in $\frac{d}{dx}(f*h)$

Source: S. Seitz

Associative property of convolution

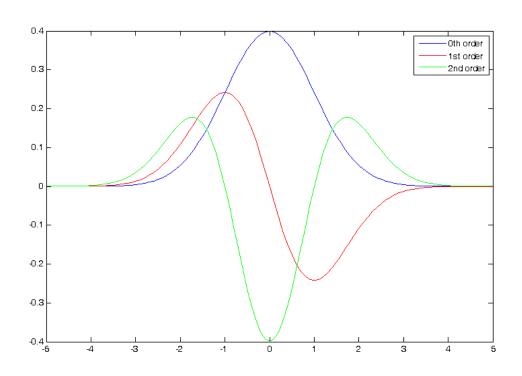
- Differentiation is convolution, and convolution is associative: $\frac{d}{dx}(f*h) = f*\frac{d}{dx}h$
- This saves us one operation:



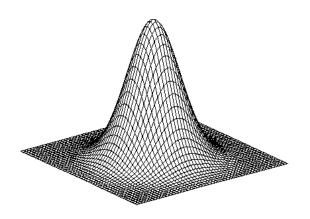
The 1D Gaussian and its derivatives

$$G_{\sigma}(x) = \frac{1}{\sqrt{2\pi}\sigma} e^{-\frac{x^2}{2\sigma^2}}$$

$$G_{\sigma}'(x) = \frac{d}{dx} G_{\sigma}(x) = -\frac{1}{\sigma} \left(\frac{x}{\sigma}\right) G_{\sigma}(x)$$

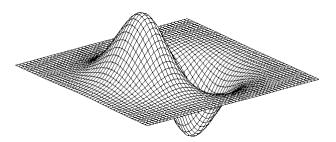


2D edge detection filters



Gaussian

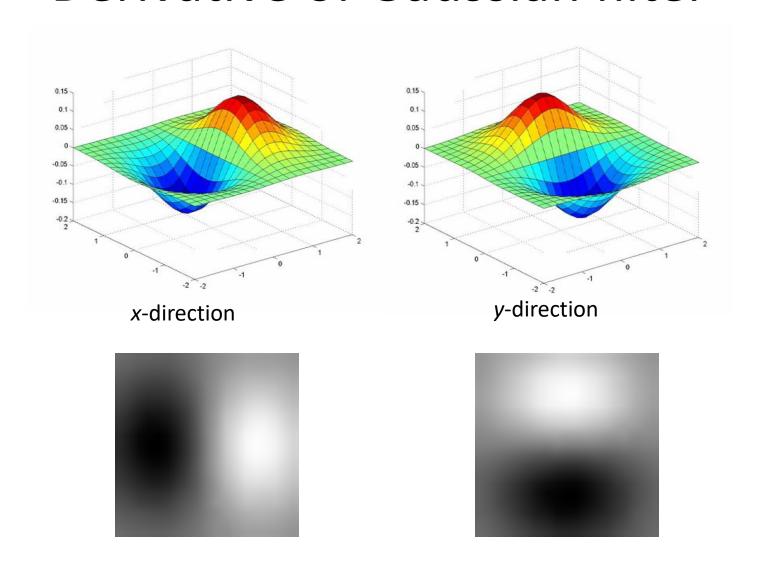
$$h_{\sigma}(u,v) = \frac{1}{2\pi\sigma^2} e^{-\frac{u^2+v^2}{2\sigma^2}}$$



derivative of Gaussian (x)

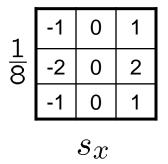
$$\frac{\partial}{\partial x}h_{\sigma}(u,v)$$

Derivative of Gaussian filter



The Sobel operator

Common approximation of derivative of Gaussian



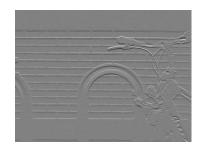
<u>1</u> 8	1	2	1
	0	0	0
	-1	-2	-1
$\overline{s_y}$			

- The standard defn. of the Sobel operator omits the 1/8 term
 - doesn't make a difference for edge detection
 - the 1/8 term is needed to get the right gradient magnitude

Sobel operator: example











Source: Wikipedia

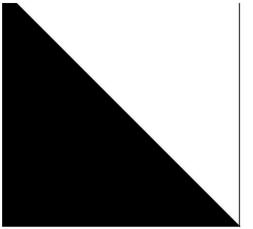
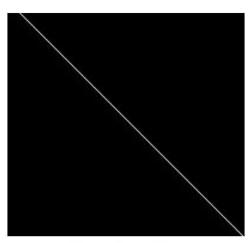


Image with Edge



Edge Location

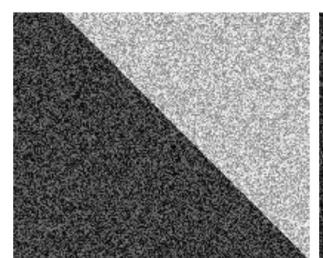
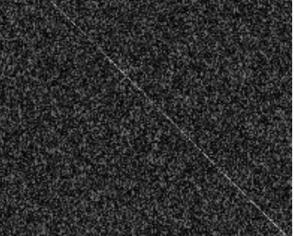
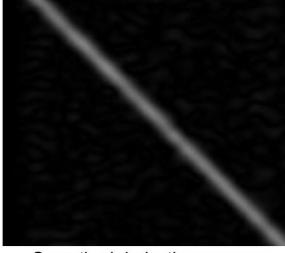


Image + Noise



Derivatives detect edge and noise



Smoothed derivative removes noise, but blurs edge

Example



original image (Lena)

Finding edges



gradient magnitude

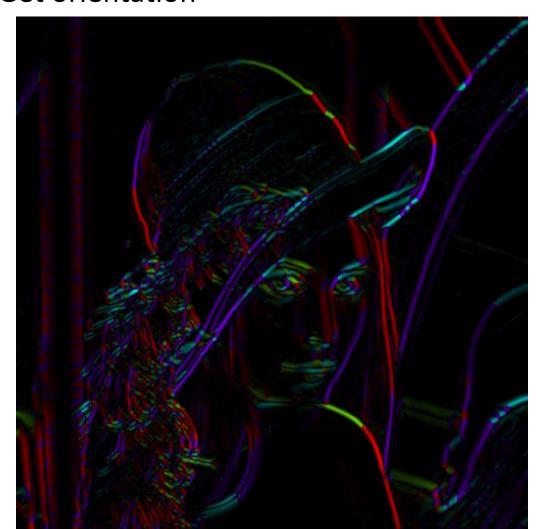
Finding edges



thresholding

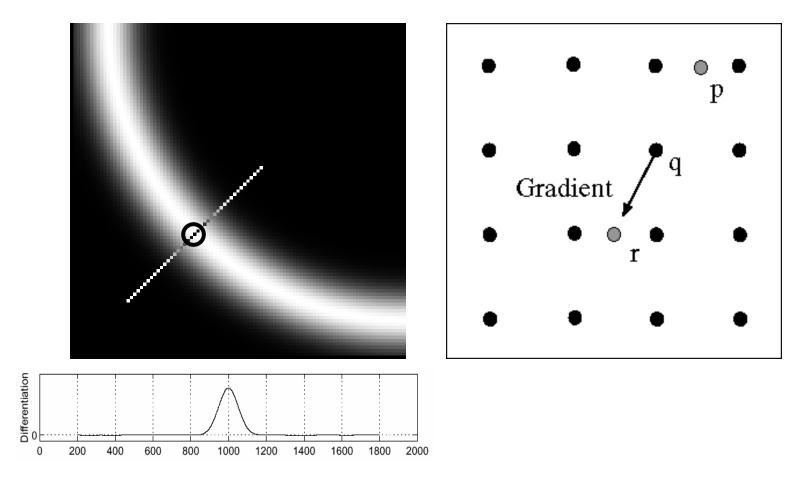
Get Orientation at Each Pixel

- Threshold at minimum level
- Get orientation



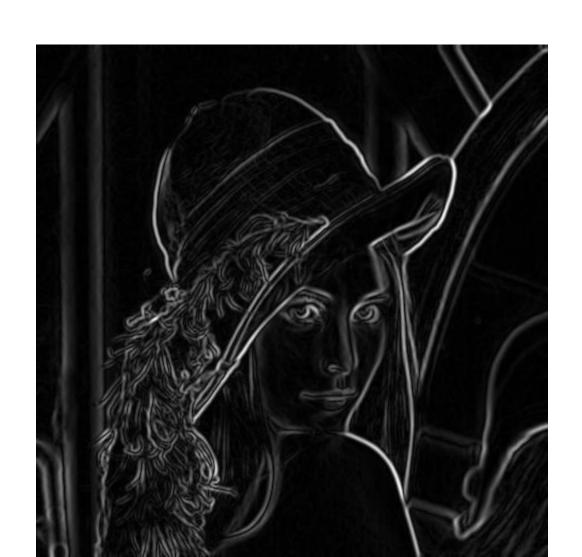
theta = atan2(gy, gx)

Non-maximum supression



- Check if pixel is local maximum along gradient direction
 - requires interpolating pixels p and r

Before Non-max Suppression



After Non-max Suppression



Finding edges



thresholding

Finding edges



thinning

(non-maximum suppression)

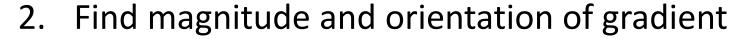


Canny edge detector

MATLAB: edge (image, 'canny')



1. Filter image with derivative of Gaussian





3. Non-maximum suppression

- 4. Linking and thresholding (hysteresis):
 - Define two thresholds: low and high
 - Use the high threshold to start edge curves and the low threshold to continue them

Canny edge detector

 Still one of the most widely used edge detectors in computer vision

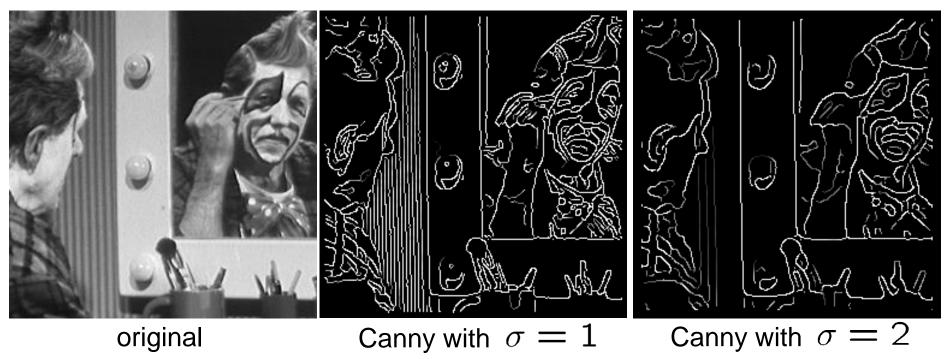
J. Canny, <u>A Computational Approach To Edge Detection</u>, IEEE Trans. Pattern Analysis and Machine Intelligence, 8:679-714, 1986.

Depends on several parameters:

 σ : width of the Gaussian blur

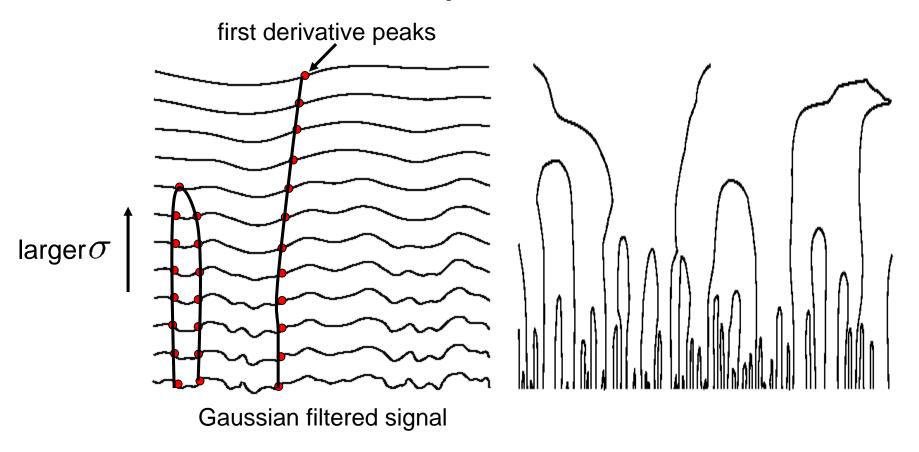
high threshold low threshold

Canny edge detector



- ullet The choice of ${oldsymbol{\sigma}}$ depends on desired behavior
 - large σ detects "large-scale" edges
 - small σ detects fine edges

Scale space (Witkin 83)



- Properties of scale space (w/ Gaussian smoothing)
 - edge position may shift with increasing scale (σ)
 - two edges may merge with increasing scale
 - an edge may *not* split into two with increasing scale

Questions?