

## CS5432 Homework 2: Authentication Logics

General Instructions. You may (but do not have to) collaborate with one other student on this assignment. If you do collaborate then both students should form a CMS group and submit their solution to that group. Both students are responsible for all of the answers.

Due: April 12, 2021 at 11:59pm. No late assignments will be accepted.

Submit your solution using CMS. Typeset your solution to produce .pdf, as follows:

- Use 10 point or larger font.
  - Start each problem on a separate page.
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**Problem 1.** Slides 61 - 63 (CAL Model for Spec Access) give hints to suggest a formal CAL proof that

A@Intel **says** (read page: Spec)

Fill-in the details by giving a full CAL proof as a list of CAL formulas with a formal justification for each. A justification you give must reference a CAL inference rule from the reading (where such a rule exists) or state a new axiom or rule that arises from the CAL modelling of the protocol.

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**Problem 2.** CAL currently supports two kinds of group principals: Conjunctive Group Principals and Disjunctive Group Principals. A proposal has been made to extend CAL with  $k$ -Group Principals (for integer  $k$ ).

Given a set of principals  $G = \{P_1, P_2, \dots, P_n\}$ , the worldview  $\omega(G^k)$  of the  $k$ -Group Principal  $G^k$  is defined to contain a belief  $C$  if and only if there are exactly  $k$  principals  $P_i \in G$  satisfying  $P_i$  says  $C$ .

Are there technical reasons to oppose this extension to CAL? Explain them.

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**Problem 3.** Consider a future where any person can carry an ID card that contains a certificate for the holder's public key. The card carried by a person  $P$  would contain  $P$ 's public key  $K_P$  and, to prevent spoofing, a PIN  $pin_P$  that  $P$  uses to authenticate:

$$Card_P = \langle pin_P, P, K_P \rangle$$

Here is a proposed protocol that  $P$  might use to start a session with some system that has a card-reader input device.

1.  $P \rightarrow Sys : Card_P$
2.  $Sys \rightarrow P$ : challenge is:  $r$  (where  $r$  is a fresh nonce)
3.  $P$  uses a calculator to compute  $\mathcal{H}(r, mypin)$  where  $\mathcal{H}$  is a well known hash function and  $mypin$  is a value that  $P$  is claiming to be its PIN. (The real  $P$  will get this right; an imposter won't guess the right value.)
4.  $P \rightarrow Sys : \mathcal{H}(r, mypin)$
5.  $Sys$ : Compute  $v := \mathcal{H}(r, pin_P)$  using stored info from lines 1 and 2. Compare  $v$  with  $\mathcal{H}(r, mypin)$  received in line 4. If they are equal then conclude  $K_P$  speaksfor  $P$

where  $P$  is a sub-principal of  $P$  corresponding to this session.

Give a CAL model for how this protocol works, including a CAL derivation of conclusion  $K_P$  speaksfor  $P$ .

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**Problem 4.** It is not unusual in security discussions to hear somebody say "A is trusted by B", meaning that A will only undertake actions that B is expecting. Give a CAL formula for modelling this situation. Justify your answer.