## Reading

Please read pp. 57-65 in Smullyan for Tuesday, March 24.

## **Project Work**

During the second half of this course you should work on a self-chosen project related to the topic of applied logic. This could, for instance, be a literature study about an interesting or the implementation (and documentation) of a proof environment. We will discuss a few possibilities in class. Please prepare a project proposal (about half a page) for Tuesday, March 31.

## Questions

- (1) Reduce these  $P^2$  formulas to purely propositional formulas.
  - (a)  $(\forall p) \ p \supset \bot$
  - (b)  $(\forall p)(\forall q) ((\sim p \lor q) \supset (p \supset q))$
  - (c)  $(\forall p)(\forall q) ((p \supset p \lor q) \land (p \land q \supset p))$
- (2) Give Refinement logic rules for  $P^2$ .
- (3) Construct an example of a formula that is satisfiable in a denumerable universe but not in any finite one (exercise 3, page 50 of Smullyan).
- (4) Show that a first-order formula A is valid if and only if  $\sim A$  is satisfiable. Show that A is satisfiable if and only if  $\sim A$  is valid (exercise 4, page 50 of Smullyan).
- (5) **Bonus** (1): There is a simple proof for cut elimination in  $P^2$ . State the theorem and outline a proof. Details are not necessary.
- (6) **Bonus (2)**: Solve exercise 3, page 52 of Smullyan.