

The following table gives the number of respondents who obtained each score.

score	9	8	7	6	5	4
number	24	4	3	0	1	1

The numbers in parentheses below show the number of people who missed each question.

For each of questions A and B, match the grammars on the left with the sets they generate on the right. The correspondence is one-to-one. The start symbol in all cases is S .

A.

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|--|-------------|--|
| 1. $S \rightarrow aSbb \mid \varepsilon$ | d(0) | a. $\{x \in \{a, b\}^* \mid x = \text{rev } x\}$ |
| 2. $S \rightarrow aaSb \mid \varepsilon$ | e(0) | b. $\{a, b\}^*$ |
| 3. $S \rightarrow aSb \mid bSa \mid SS \mid \varepsilon$ | c(0) | c. $\{x \in \{a, b\}^* \mid \#a(x) = \#b(x)\}$ |
| 4. $S \rightarrow aSa \mid bSb \mid a \mid b \mid \varepsilon$ | a(2) | d. $\{a^n b^m \mid m = 2n\}$ |
| 5. $S \rightarrow aSb \mid bSa \mid a \mid b \mid SS \mid \varepsilon$ | b(4) | e. $\{a^n b^m \mid n = 2m\}$ |

B.

- | | | | |
|-------------------------------|---|--------------------------------------|---|
| 6. $S \rightarrow aSb \mid T$ | 7. $T \rightarrow bTa \mid \varepsilon$ | b(3) | a. $\{a^n b^{n+m} a^m \mid n, m \geq 0\}$ |
| 7. $S \rightarrow TT$ | $T \rightarrow aTb \mid \varepsilon$ | c(2) | b. $\{a^n b^m a^m b^n \mid n, m \geq 0\}$ |
| 8. $S \rightarrow TU$ | $T \rightarrow aTb \mid \varepsilon$ | $U \rightarrow bUa \mid \varepsilon$ | a(4) |
| | | | c. $\{a^n b^n a^m b^m \mid n, m \geq 0\}$ |

C. The following is a grammar in Greibach normal form for the set of balanced parentheses. The start symbol is S .

$$S \rightarrow [B \qquad B \rightarrow] \mid]S \mid [BB$$

Which of the following sentential forms would *not* occur in any derivation of the string $[[[]][[]][[]]$?

- a. $[[BB$
- b. $[[[]B$
- c. $[[[]][BB$
- d. $[[[]][[]B$
- e. $[[[]][[]]B$ **(4)**
- f. $[[[]][[]][[]B$

In this Greibach normal form grammar, the number of B 's in any sentential form generated from S is always the same as the number of unmatched left parens in the terminal string generated so far.