

Last Class: Test :)...Parsing and Partial Parsing

Today: Probabilistic Parsing

Goal: Find the most likely parse.

1. Parsing with PCFGs
2. Problems
3. Probabilistic lexicalized CFGs

Slide CS474-1

### CFG's

A context free grammar consists of:

1. a set of non-terminal symbols  $N$
2. a set of terminal symbols  $\Sigma$  (disjoint from  $N$ )
3. a set of productions,  $P$ , each of the form  $A \rightarrow \alpha$ , where  $A$  is a non-terminal and  $\alpha$  is a string of symbols from the infinite set of strings  $(\Sigma \cup N)$
4. a designated start symbol  $S$

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### Probabilistic CFGs

Augments each rule in  $P$  with a conditional probability:

$$A \rightarrow \beta [p]$$

where  $p$  is the probability that the non-terminal  $A$  will be expanded to the sequence  $\beta$ . Often referred to as

$$P(A \rightarrow \beta) \text{ or}$$

$$P(A \rightarrow \beta | A).$$

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### Example

$S \rightarrow NP VP$	[.80]	$Det \rightarrow that$	[.05]   $the$	[.80]   $a$	[.15]
$S \rightarrow Aux NP VP$	[.15]	$Noun \rightarrow book$			[.10]
$S \rightarrow VP$	[.05]	$Noun \rightarrow flights$			[.50]
$NP \rightarrow Det Nom$	[.20]	$Noun \rightarrow meal$			[.40]
$NP \rightarrow Proper-Noun$	[.35]	$Verb \rightarrow book$			[.30]
$NP \rightarrow Nom$	[.05]	$Verb \rightarrow include$			[.30]
$NP \rightarrow Pronoun$	[.40]	$Verb \rightarrow want$			[.40]
$Nom \rightarrow Noun$	[.75]	$Aux \rightarrow can$			[.40]
$Nom \rightarrow Noun Nom$	[.20]	$Aux \rightarrow does$			[.30]
$Nom \rightarrow Proper-Noun Nom$	[.05]	$Aux \rightarrow do$			[.30]
$VP \rightarrow Verb$	[.55]	$Proper-Noun \rightarrow TWA$			[.40]
$VP \rightarrow Verb NP$	[.40]	$Proper-Noun \rightarrow Denver$			[.40]
$VP \rightarrow Verb NP NP$	[.05]	$Pronoun \rightarrow you$	[.40]   $I$	[.60]	

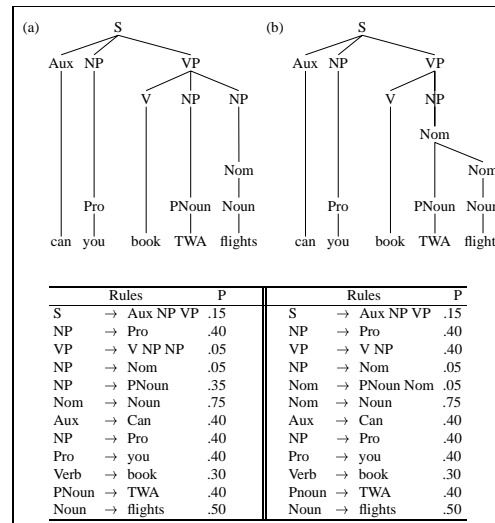
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### Why are PCFGs useful?

- Assigns a probability to each parse tree  $T$
- Useful in **disambiguation**
  - Choose the most likely parse
  - Computing the probability of a parse  
If we make independence assumptions,  $P(T) = \prod_{n \in T} p(r(n))$ .
- Useful in **language modeling** tasks

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### Example



Slide CS474-6

### Where do the probabilities come from?

1. from a **treebank**:

$$P(\alpha \rightarrow \beta | \alpha) = \text{Count}(\alpha \rightarrow \beta) / \text{Count}(\alpha)$$

2. use EM (forward-backward algorithm, inside-outside algorithm)

Slide CS474-7

### Parsing with PCFGs

Produce the most likely parse for a given sentence:

$$\hat{T}(S) = \underset{T \in \tau(S)}{\text{argmax}} P(T)$$

where  $\tau(S)$  is the set of possible parse trees for  $S$ .

- Augment the Earley algorithm to compute the probability of each of its parses.

When adding an entry  $E$  of category  $C$  to the chart using rule  $i$  with  $n$  constituents,  $E_1, \dots, E_n$ :

$$P(E) = P(\text{rule } i \mid C) * P(E_1) * \dots * P(E_n)$$

- probabilistic CYK (Cocke-Younger-Kasami) algorithm

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### Problems with PCFGs

Do not model *structural dependencies*.

Often the choice of how a non-terminal expands depends on the location of the node in the parse tree.

E.g. Strong tendency in English for the syntactic subject of a spoken sentence to be a pronoun.

- 91% of declarative sentences in the Switchboard corpus are pronouns (vs. lexical).
- In contrast, 34% of direct objects in Switchboard are pronouns.

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### Problems with PCFGs

Do not adequately model *lexical dependencies*.

*Moscow sent more than 100,000 soldiers into Afghanistan...*

PP can attach to either the NP or the VP:

NP → NP PP or VP → V NP PP?

Attachment choice depends (in part) on the verb: *send* subcategorizes for a destination (e.g. expressed via a PP that begins with *into* or *to* or ...).

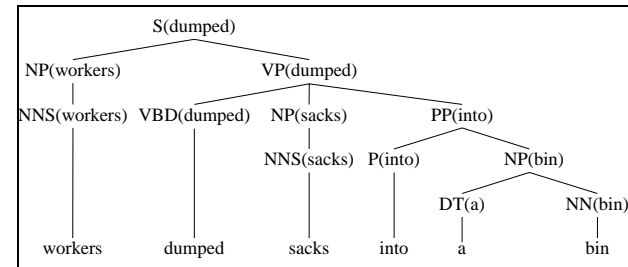
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### Probabilistic lexicalized CFGs

- Each non-terminal is associated with its head.
- Each PCFG rule needs to be augmented to identify one rhs constituent to be the head daughter.
- Headword for a node in the parse tree is set to the headword of its head daughter.

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### Example



Slide CS474–12

### Probabilistic lexicalized CFGs

View a lexicalized (P)CFG as a simple (P)CFG with a lot more rules.

VP(dumped)  $\rightarrow$  VBD(dumped) NP(sacks) PP(into) [ $3 \times 10^{-10}$ ]

VP(dumped)  $\rightarrow$  VBD(dumped) NP(cats) PP(into) [ $8 \times 10^{-10}$ ]

VP(dumped)  $\rightarrow$  VBD(dumped) NP(sacks) PP(above) [ $1 \times 10^{-12}$ ]

...

Problem?

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### Incorporating lexical dependency information

Incorporates lexical dependency information by:

1. relating the heads of phrases to the heads of their constituents;
2. including syntactic subcategorization information.

Syntactic subcategorization dependencies:

Probability of a rule  $r$  of syntactic category  $n$ :

$p(r(n) | n, h(n))$ .

Example: probability of expanding VP as VP  $\rightarrow$  VBD NP PP will be

$p(r | VP, dumped)$ .

Slide CS474-14

### Incorporating lexical dependency information

Condition the probability of a node  $n$  having a head  $h$  on two factors:

1. the syntactic category of the node  $n$
2. the head of the node's mother  $h(m(n))$

$p(h(n) = \text{word}_i | n, h(m(n)))$

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### Computing the probability of a parse

Producing the most likely parse for a given sentence changes from:

$$P(T) = \prod_{n \in T} p(r(n))$$

to

$$P(T) = \prod_{n \in T} p(r(n)|n, h(n)) * p(h(n)|n, h(m(n)))$$

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### **Evaluation Measures and State of the Art**

- labeled recall:  $\frac{\# \text{ correct constituents in candidate parse of } s}{\# \text{ correct constituents in treebank parse of } s}$
- labeled precision:  $\frac{\# \text{ correct constituents in candidate parse of } s}{\text{total } \# \text{ of constituents in candidate parse of } s}$
- crossing brackets: the number of crossed brackets

State of the art: 90% recall, 90% precision, 1% crossed bracketed constituents per sentence (WSJ treebank)

**Slide CS474-17**