CS4670/5670: Intro to Computer Vision

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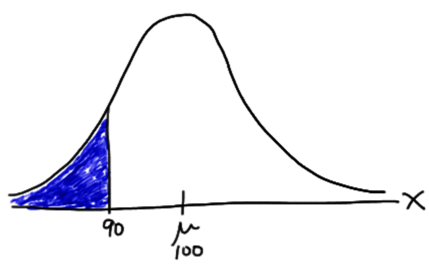
Lecture 26: Modeling probabilities



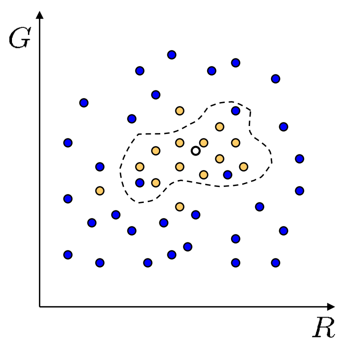
Project 4

- To be released soon
- Demo…

Face detection

- Do these images contain faces? Where?

Skin classification techniques



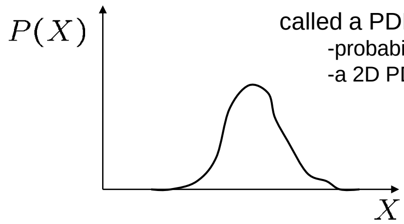
Skin classifier

- Given X = (R,G,B): how to determine if it is skin or not?
- Nearest neighbor
  - find labeled pixel closest to X
  - choose the label for that pixel
- Data modeling
  - fit a model (curve, surface, or volume) to each class
- Probabilistic data modeling
  - fit a probability model to each class

Probability

Basic probability

- **X** is a random variable
- **P(X)** is the probability that **X** achieves a certain value



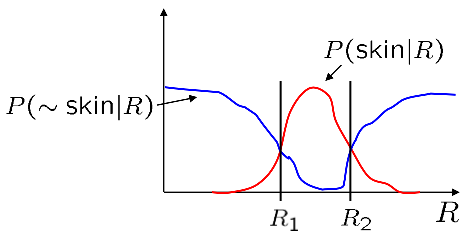
called a PDF
-probability distribution/density function
-a 2D PDF is a surface, 3D PDF is a volume

- $0 \leq P(X) \leq 1$
- $\int_{-\infty}^{\infty} P(X) dX = 1$ or $\sum P(X) = 1$

continuous **X** discrete **X**

- Conditional probability: **P(X | Y)**
  - probability of **X** given that we already know **Y**

Probabilistic skin classification



Now we can model uncertainty

- Each pixel has a probability of being skin or not skin
  - $P(\sim \text{skin}|R) = 1 - P(\text{skin}|R)$

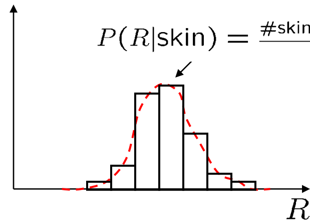
Skin classifier

- Given X = (R,G,B): how to determine if it is skin or not?
- Choose interpretation of highest probability
  - set X to be a skin pixel if and only if $R_1 < X \leq R_2$

Where do we get $P(\text{skin}|R)$ and $P(\sim \text{skin}|R)$?

Learning conditional PDF's

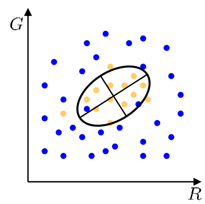
$$P(R|\text{skin}) = \frac{\text{\#skin pixels with color R}}{\text{\#skin pixels}}$$



We can calculate **P(R | skin)** from a set of training images

- It is simply a histogram over the pixels in the training images
  - each bin R_i contains the proportion of skin pixels with color R_i

This doesn't work as well in higher-dimensional spaces. Why not?

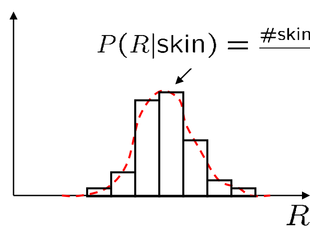


Approach: fit parametric PDF functions

- common choice is rotated Gaussian
  - center $\mathbf{c} = \overline{X}$
  - covariance $\sum_X (X - \overline{X})(X - \overline{X})^T$
    - » orientation, size defined by eigenvecs, eigenvals

Learning conditional PDF's

$$P(R|\text{skin}) = \frac{\text{\#skin pixels with color R}}{\text{\#skin pixels}}$$



We can calculate **P(R | skin)** from a set of training images

- It is simply a histogram over the pixels in the training images
  - each bin R_i contains the proportion of skin pixels with color R_i

But this isn't quite what we want

- Why not? How to determine if a pixel is skin?
- We want **P(skin | R)**, not **P(R | skin)**
- How can we get it?

Bayes rule

$$P(X|Y) = \frac{P(Y|X)P(X)}{P(Y)}$$

In terms of our problem:

what we measure (**likelihood**) domain knowledge (**prior**)

$$P(\text{skin}|R) = \frac{P(R|\text{skin})\ P(\text{skin})}{P(R)}$$

what we want (**posterior**)

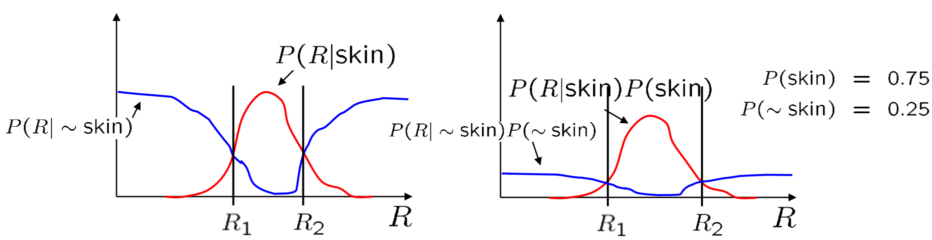
normalization term

$P(R) = P(R|\text{skin})P(\text{skin}) + P(R|\sim\text{skin})P(\sim\text{skin})$

The prior: **P(skin)**

- Could use domain knowledge
  - **P(skin)** may be larger if we know the image contains a person
  - for a portrait, **P(skin)** may be higher for pixels in the center
- Could learn the prior from the training set. How?
  - **P(skin)** could be the proportion of skin pixels in training set

Bayesian estimation



likelihood posterior (unnormalized)

Bayesian estimation = minimize probability of misclassification

- Goal is to choose the label (skin or ~skin) that maximizes the posterior
  - this is called **Maximum A Posteriori (MAP) estimation**
- Suppose the prior is uniform: **P(skin)** = **P(~skin)** =0.5
  - in this case $P(\text{skin}|R) = cP(R|\text{skin})$, $P(\sim\text{skin}|R) = cP(R|\sim\text{skin})$
  - maximizing the posterior is equivalent to maximizing the likelihood
    - » $P(\text{skin}|R) > P(\sim\text{skin}|R)$ if and only if $P(R|\text{skin}) > P(R|\sim\text{skin})$
  - this is called **Maximum Likelihood (ML) estimation**

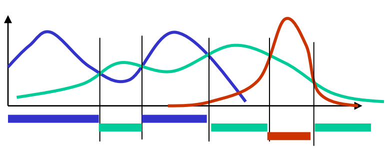
Skin detection results

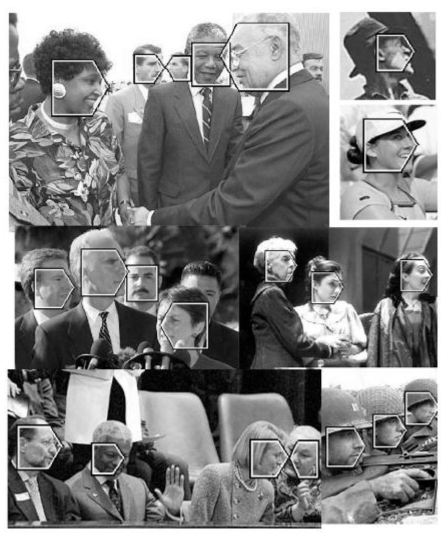
Figure 25.3. The figure shows a variety of images together with the output of the skin detector of Jones and Rehg applied to the image. Pixels marked black are skin pixels, and white are background. Notice that this process is relatively effective, and could certainly be used to focus attention on, say, faces and hands. *Figure from "Statistical color models with application to skin detection," M.J. Jones and J. Rehg, Proc. Computer Vision and Pattern Recognition, 1999 © 1999, IEEE*

General classification

This same procedure applies in more general circumstances

- More than two classes
- More than one dimension





H. Schneiderman and T.Kanade

Example: face detection

- Here, X is an image region
  - dimension = # pixels
  - each face can be thought of as a point in a high dimensional space

H. Schneiderman, T. Kanade. "A Statistical Method for 3D Object Detection Applied to Faces and Cars". IEEE Conference on Computer Vision and Pattern Recognition (CVPR 2000) http://www-2.cs.cmu.edu/afs/cs.cmu.edu/user/hws/www/CVPR00.pdf