## CS4670/5760: Computer Vision

 Noah SnavelyLecture 12: Robust Fitting and RANSAC


## Announcements

- Project 2 deadline extended to Wednesday at 5:59pm
- Quiz on Friday


## Reading

- Szeliski: Chapter 6.1.4

Homographies


## Image Alignment Algorithm

Given images $A$ and $B$

1. Compute image features for $A$ and $B$
2. Match features between $A$ and $B$
3. Compute homography between $A$ and $B$ using least squares on set of matches

What could go wrong?


## Robustness

- Let's consider a simpler example... linear regression


Problem: Fit a line to these datapoints


Least squares fit

- How can we fix this?


## We need a better cost function...

- Suggestions?


## Idea

- Given a hypothesized line
- Count the number of points that "agree" with the line
- "Agree" = within a small distance of the line
- I.e., the inliers to that line
- For all possible lines, select the one with the largest number of inliers


## Counting inliers



## Counting inliers



Inliers: 3

## Counting inliers



## How do we find the best line?

- Unlike least-squares, no simple closed-form solution
- Hypothesize-and-test
- Try out many lines, keep the best one
- Which lines?


## Translations



## RAndom SAmple Consensus



## RAndom SAmple Consensus



## RAndom SAmple Consensus



## RANSAC

- Idea:
- All the inliers will agree with each other on the translation vector; the (hopefully small) number of outliers will (hopefully) disagree with each other
- RANSAC only has guarantees if there are $<50 \%$ outliers
- "All good matches are alike; every bad match is bad in its own way."
- Tolstoy via Alyosha Efros


## RANSAC

- Inlier threshold related to the amount of noise we expect in inliers
- Often model noise as Gaussian with some standard deviation (e.g., 3 pixels)
- Number of rounds related to the percentage of outliers we expect, and the probability of success we'd like to guarantee
- Suppose there are $20 \%$ outliers, and we want to find the correct answer with $99 \%$ probability
- How many rounds do we need?



## RANSAC <br> 0

- Back to linear regression
- How do we generate a hypothesis?



## RANSAC

- Back to linear regression
- How do we generate a hypothesis?



## RANSAC

- General version:

1. Randomly choose $s$ samples

- Typically $s=$ minimum sample size that lets you fit a model

2. Fit a model (e.g., line) to those samples
3. Count the number of inliers that approximately fit the model
4. Repeat $N$ times
5. Choose the model that has the largest set of inliers

## How many rounds?

- If we have to choose s samples each time
- with an outlier ratio $e$
- and we want the right answer with probability $p$

| proportion of outliers $e$ |  |  |  |  |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| s | $5 \%$ | $10 \%$ | $20 \%$ | $25 \%$ | $30 \%$ | $40 \%$ | $50 \%$ |  |
| 2 | 2 | 3 | 5 | 6 | 7 | 11 | 17 |  |
| 3 | 3 | 4 | 7 | 9 | 11 | 19 | 35 |  |
| 4 | 3 | 5 | 9 | 13 | 17 | 34 | 72 |  |
| 5 | 4 | 6 | 12 | 17 | 26 | 57 | 146 |  |
| 6 | 4 | 7 | 16 | 24 | 37 | 97 | 293 |  |
| 7 | 4 | 8 | 20 | 33 | 54 | 163 | 588 |  |
| 8 | 5 | 9 | 26 | 44 | 78 | 272 | 1177 |  |



## How big is $s$ ?

- For alignment, depends on the motion model
- Here, each sample is a correspondence (pair of matching points)


| Name | Matrix | \# D.O.F. | Preserves: | Icon |
| :--- | :---: | :---: | :--- | :---: |
| translation | $[\boldsymbol{I} \mid \boldsymbol{t}]_{2 \times 3}$ | 2 | orientation $+\cdots$ | $\square$ |
| rigid (Euclidean) | $[\boldsymbol{R} \mid \boldsymbol{t}]_{2 \times 3}$ | 3 | lengths $+\cdots$ | $\square$ |
| similarity | $[s \boldsymbol{R} \mid \boldsymbol{t}]_{2 \times 3}$ | 4 | angles $+\cdots$ | $\square$ |
| affine | $[\boldsymbol{A}]_{2 \times 3}$ | 6 | parallelism $+\cdots$ | $\square$ |
| projective | $[\tilde{\boldsymbol{H}}]_{3 \times 3}$ | 8 | straight lines | $\square$ |

## RANSAC pros and cons

- Pros
- Simple and general
- Applicable to many different problems
- Often works well in practice
- Cons
- Parameters to tune
- Sometimes too many iterations are required
- Can fail for extremely low inlier ratios
- We can often do better than brute-force sampling


## Final step: least squares fit



## RANSAC

- An example of a "voting"-based fitting scheme
- Each hypothesis gets voted on by each data point, best hypothesis wins
- There are many other types of voting schemes
- E.g., Hough transforms...


## Hough transform



## Panoramas

- Now we know how to create panoramas!
- Given two images:
- Step 1: Detect features
- Step 2: Match features
- Step 3: Compute a homography using RANSAC
- Step 4: Combine the images together (somehow)
- What if we have more than two images?


## Can we use homographies to create a 360 panorama?



- In order to figure this out, we need to learn what a camera is


## 360 panorama



