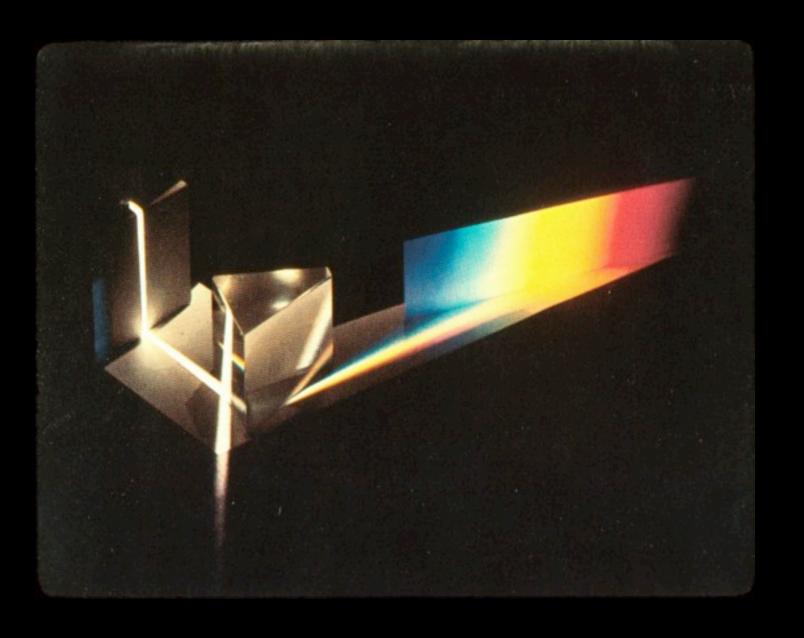
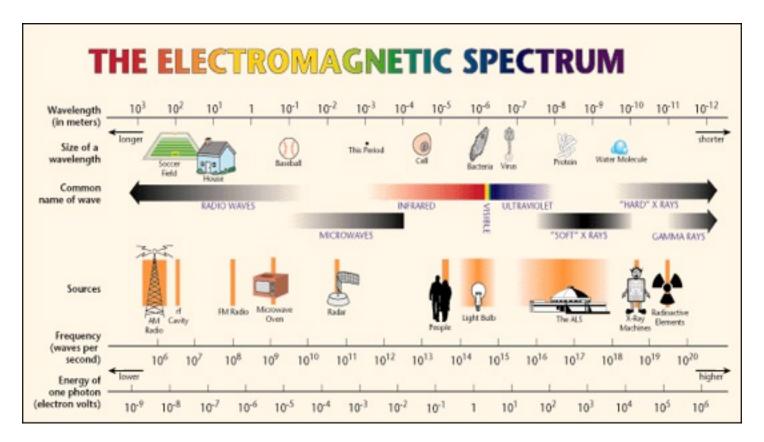
#### **Color Science**

**CS 4620 Lecture 15** 



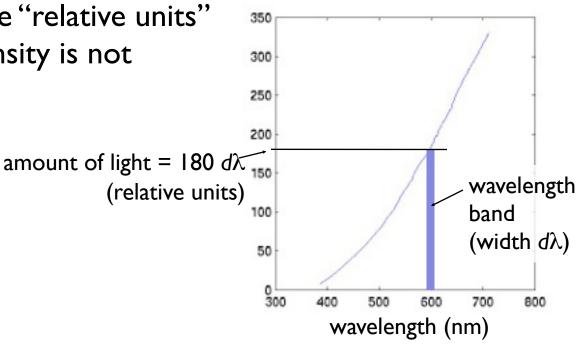
#### What light is

- Light is electromagnetic radiation
  - exists as oscillations of different frequency (or, wavelength)



# Measuring light

- Salient property is the spectral power distribution (SPD)
  - the amount of light present at each wavelength
  - units: Watts per nanometer (tells you how much power you'll find in a narrow range of wavelengths)
  - for color, often use "relative units"
     when overall intensity is not important

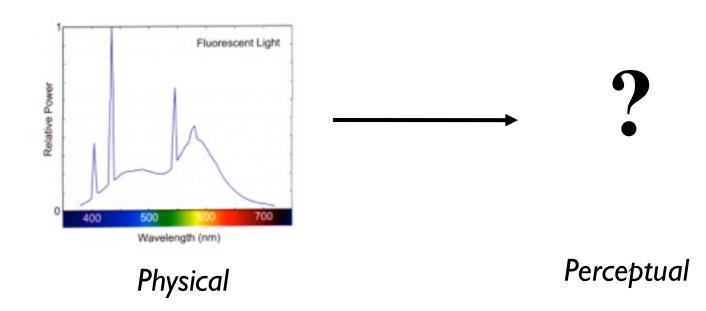


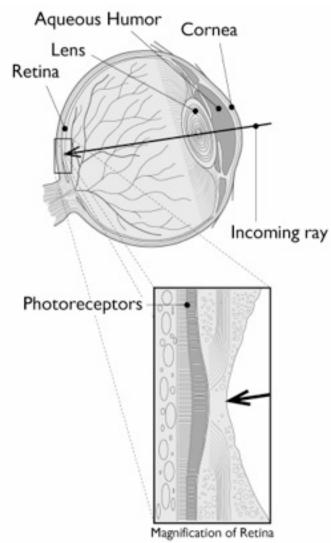
#### What color is

- Colors are the sensations that arise from light energy of different wavelengths
  - we are sensitive from about 380 to 760 nm—one "octave"
- Color is a phenomenon of human perception; it is not a universal property of light
- Roughly speaking, things appear "colored" when they depend on wavelength and "gray" when they do not.

#### The problem of color science

- Build a model for human color perception
- That is, map a Physical light description to a Perceptual color sensation



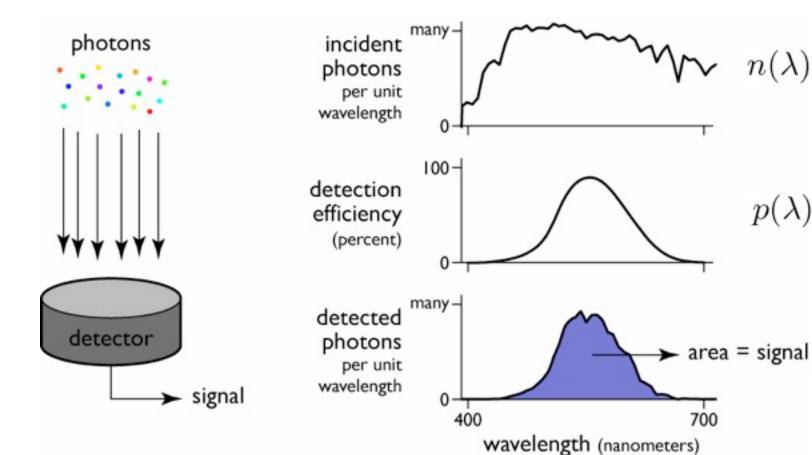


- We can model the low-level behavior of the eye by thinking of it as a light-measuring machine
  - its optics are much like a camera
  - its detection mechanism is also much like a camera
- Light is measured by the photoreceptors in the retina
  - they respond to visible light
  - different types respond to different wavelengths

# A simple light detector

- Produces a scalar value (a number) when photons land on it
  - this value depends strictly on the number of photons detected
  - each photon has a probability of being detected that depends on the wavelength
  - there is no way to tell the difference between signals caused by light of different wavelengths: there is just a number
- This model works for many detectors:
  - based on semiconductors (such as in a digital camera)
  - based on visual photopigments (such as in human eyes)

# A simple light detector

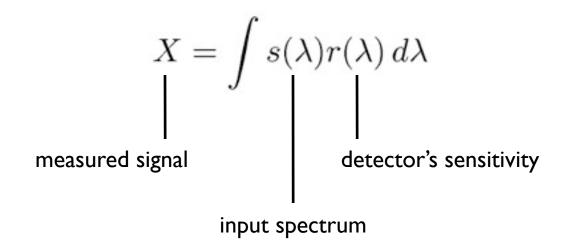


$$X = \int n(\lambda)p(\lambda) \, d\lambda$$

 $p(\lambda)$ 

# **Light detection math**

- Same math carries over to power distributions
  - spectrum entering the detector has its spectral power distribution (SPD),  $s(\lambda)$
  - detector has its spectral sensitivity or spectral response,  $r(\lambda)$



# Light detection math

$$X = \int s(\lambda)r(\lambda) d\lambda$$
 or  $X = s \cdot r$ 

- If we think of s and r as vectors, this operation is a dot product (aka inner product)
  - in fact, the computation is done exactly this way, using sampled representations of the spectra.
    - let  $\lambda_i$  be regularly spaced sample points  $\Delta\lambda$  apart; then:

$$\tilde{s}[i] = s(\lambda_i); \tilde{r}[i] = r(\lambda_i)$$

$$\int s(\lambda)r(\lambda) d\lambda \approx \sum_{i} \tilde{s}[i]\tilde{r}[i] \Delta\lambda$$

this sum is very clearly a dot product

#### **Human observation**

- Human eye observes electro-magnetic wavelengths
  - Humans 'see' different spectra as different colors
  - Color is a phenomenon of human perception; it is not a universal property of light
- Other animals observe other wavelengths
  - Bees: 340 540 nm
    - (they see no red, but can see ultra-violet)

#### **Insects and color**

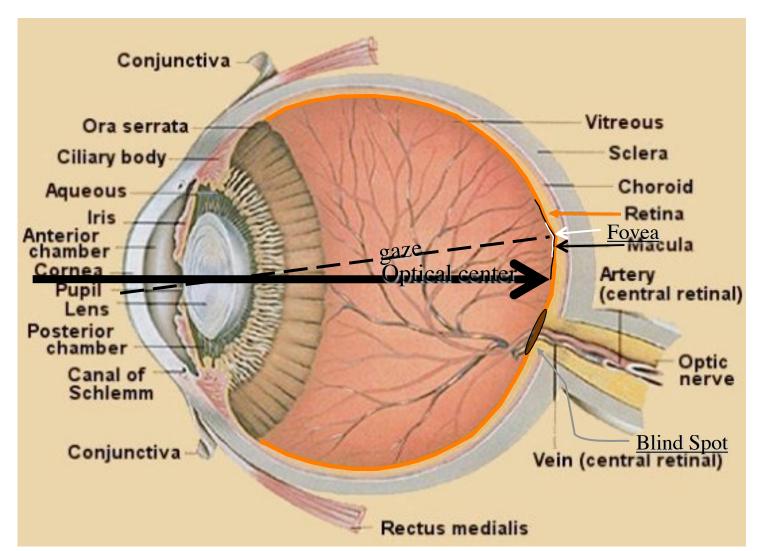




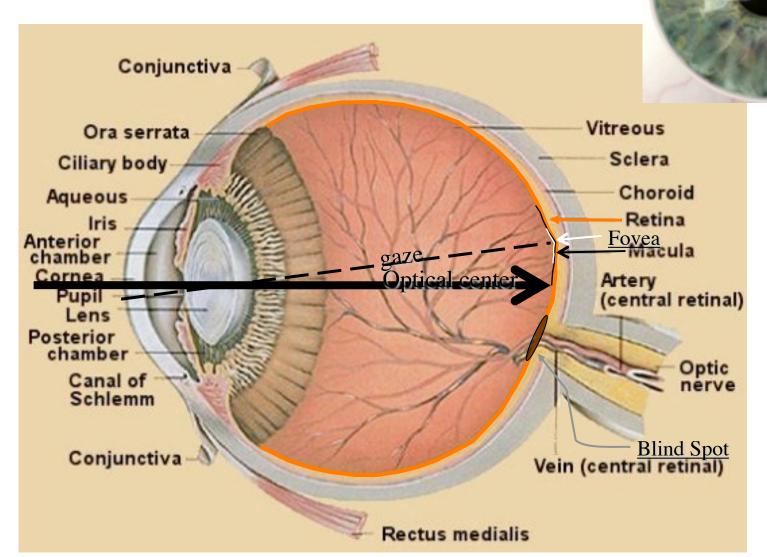


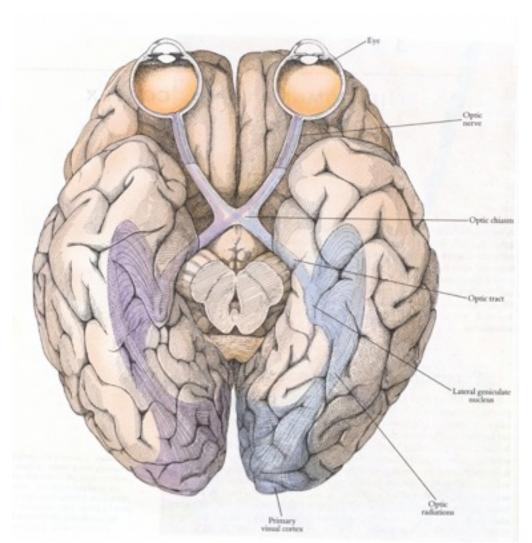
'Honey Bee'

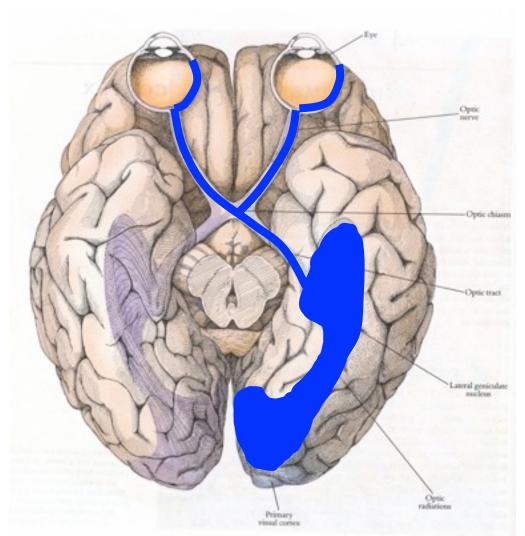
# **Human eye**

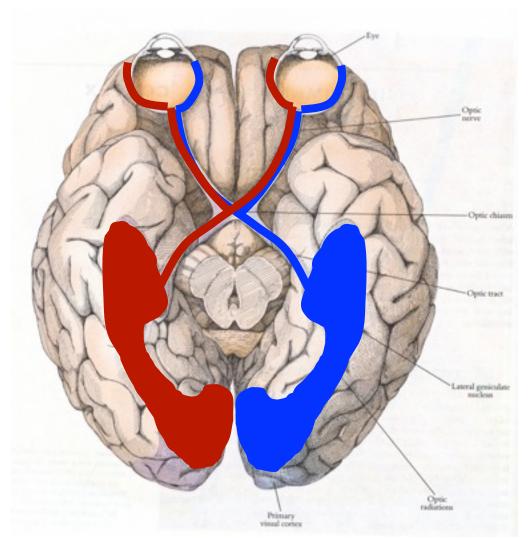


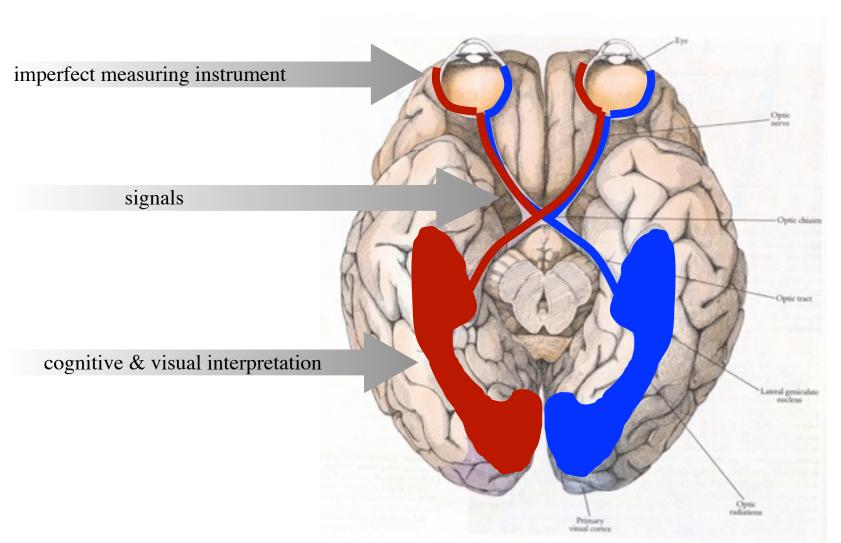
# **Human eye**



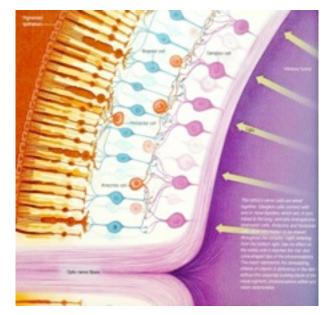






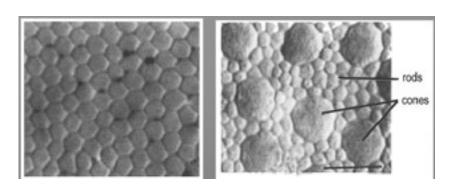


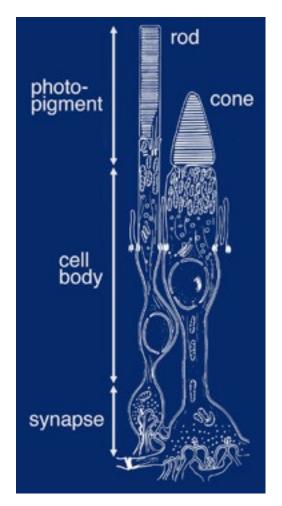
#### Human eye: retina



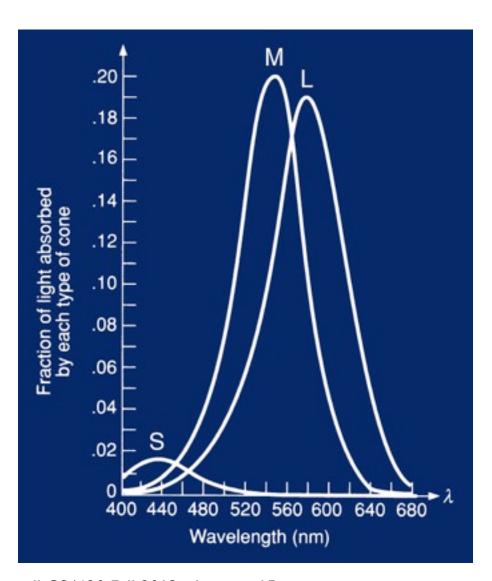
Light passes through blood vessels & retinal layers before reaching the light-sensitive cells

("rods" & "cones")

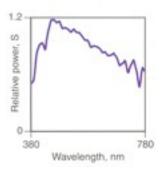


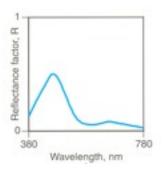


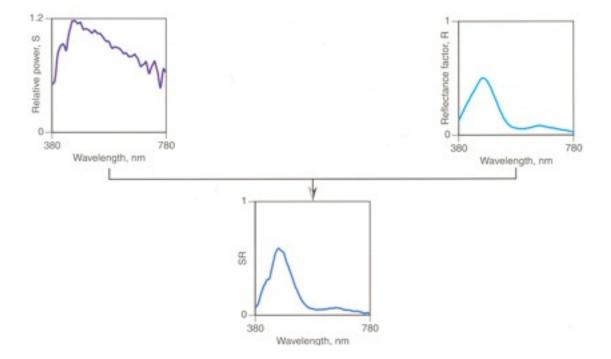
#### **Cone Responses**

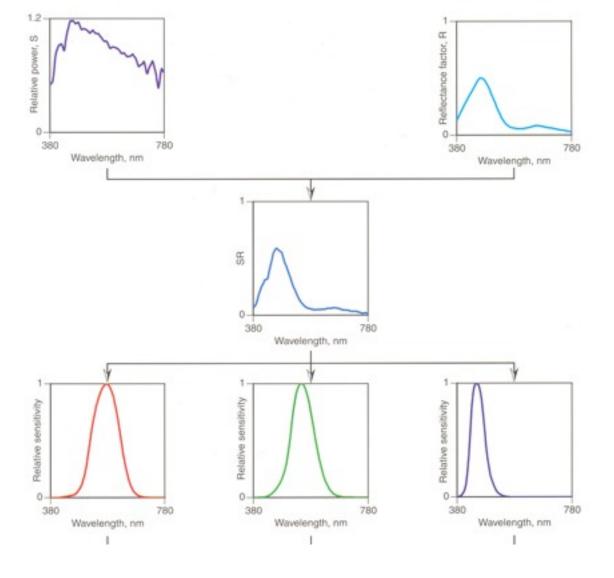


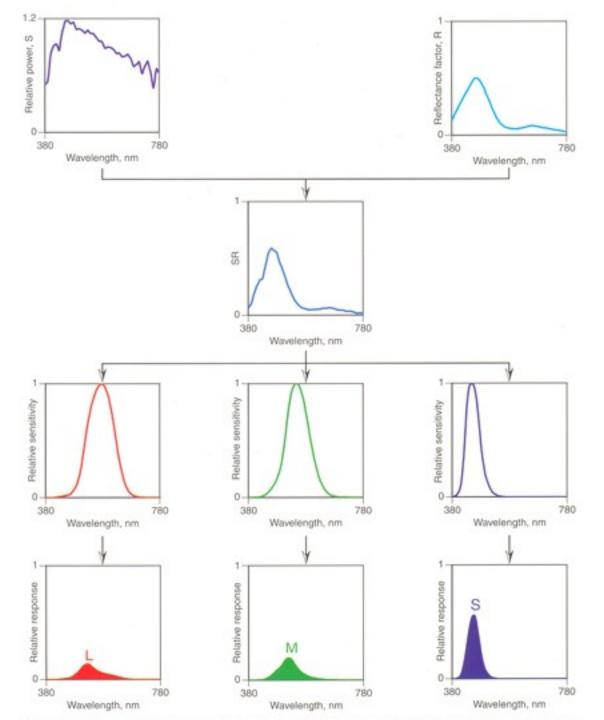
- S,M,L cones have broadband spectral sensitivity
- S,M,L neural response is integrated w.r.t.  $\lambda$ 
  - we'll call the response functions  $r_S$ ,  $r_M$ ,  $r_L$
- Results in a trichromatic visual system
- S, M, and L are tristimulus values



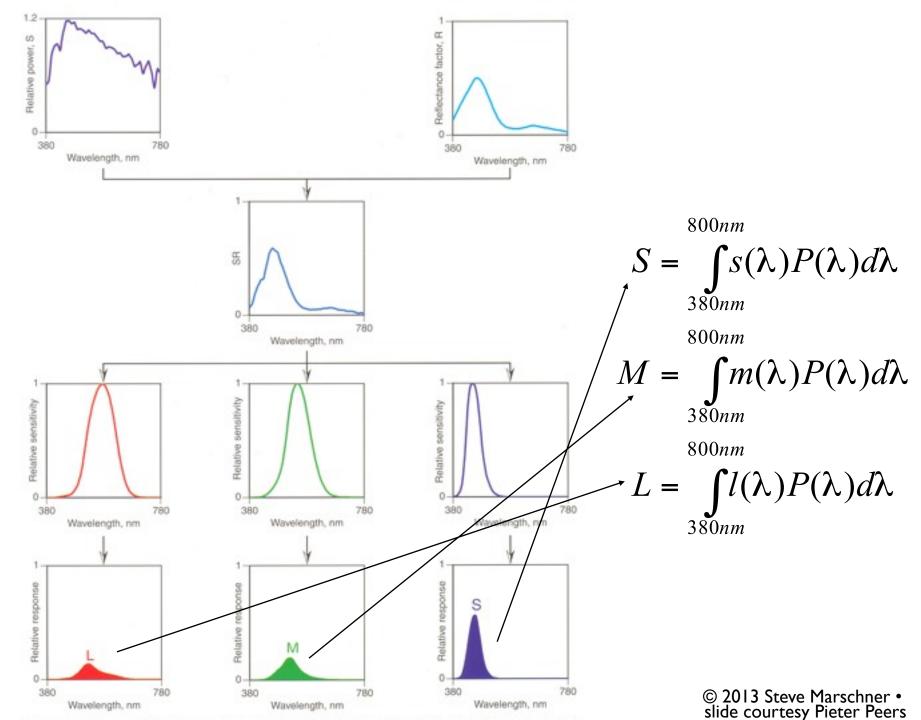


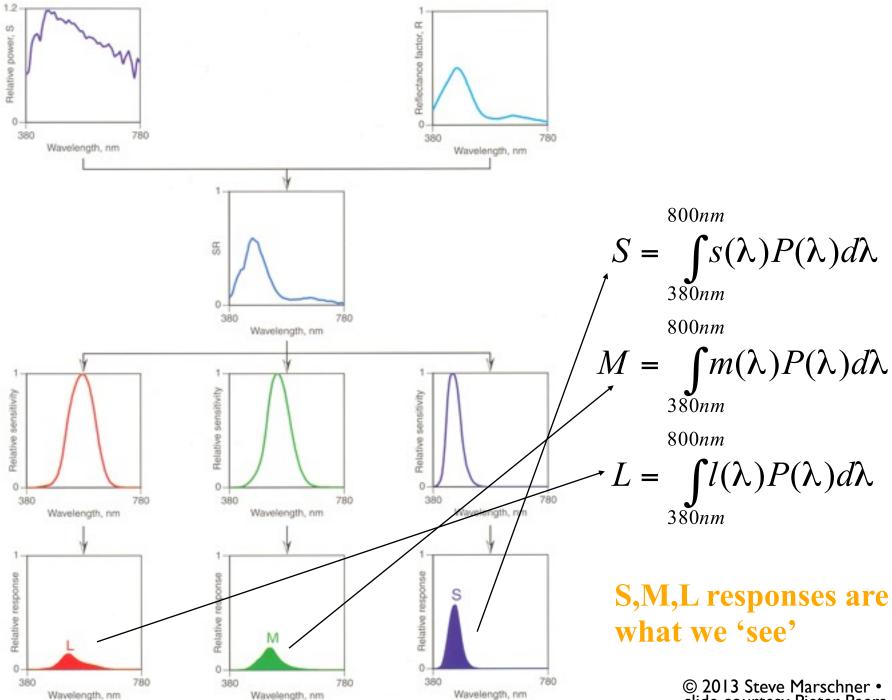






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#### Cone responses to a spectrum s

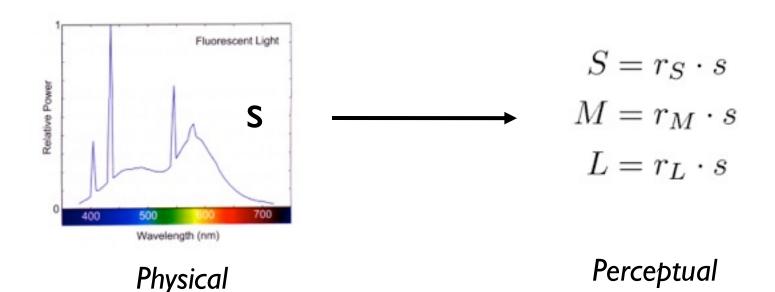
$$S = \int r_S(\lambda)s(\lambda) d\lambda = r_S \cdot s$$

$$M = \int r_M(\lambda)s(\lambda) d\lambda = r_M \cdot s$$

$$L = \int r_L(\lambda)s(\lambda) d\lambda = r_L \cdot s$$

# Colorimetry: an answer to the problem

- Wanted to map a Physical light description to a Perceptual color sensation
- Basic solution was known and standardized by 1930
  - Though not quite in this form—more on that in a bit



#### **Basic fact of colorimetry**

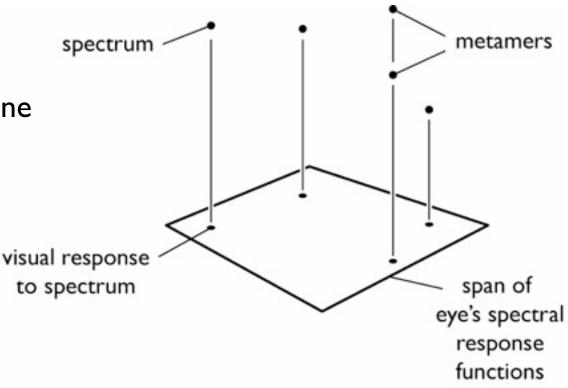
- Take a spectrum (which is a function)
- Eye produces three numbers
- This throws away a lot of information!
  - Quite possible to have two different spectra that have the same S, M, L tristimulus values
  - Two such spectra are metamers

#### Pseudo-geometric interpretation

- A dot product is a projection
- We are projecting a high dimensional vector (a spectrum) onto three vectors
  - differences that are perpendicular to all 3 vectors are not detectable
- For intuition, we can imagine a 3D analog
  - 3D stands in for high-D vectors
  - 2D stands in for 3D
  - Then vision is just projection onto a plane

# Pseudo-geometric interpretation

- The information available to the visual system about a spectrum is three values
  - this amounts to a loss of information analogous to projection on a plane
- Two spectra that produce the same response are metamers



# [Stone 2003]

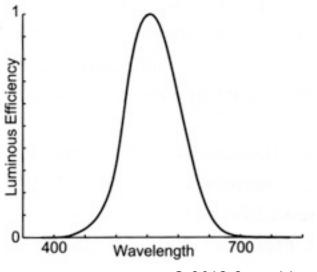
# **Basic colorimetric concepts**

#### Luminance

- the overall magnitude of the the visual response to a spectrum (independent of its color)
  - corresponds to the everyday concept "brightness"
- determined by product of SPD with the *luminous efficiency* function  $V_{\lambda}$  that describes the eye's overall ability to detect

light at each wavelength

e.g. lamps are optimized
 to improve their luminous
 efficiency (tungsten vs.
 fluorescent vs. sodium vapor)



#### Luminance, mathematically

• Y just has another response curve (like S, M, and L)

$$Y = r_Y \cdot s$$

- $r_{\gamma}$  is really called " $V_{\lambda}$ "
- $V_{\lambda}$  is a linear combination of S, M, and L
  - Has to be, since it's derived from cone outputs

#### More basic colorimetric concepts

#### Chromaticity

- what's left after luminance is factored out (the color without regard for overall brightness)
- scaling a spectrum up or down leaves chromaticity alone

#### Dominant wavelength

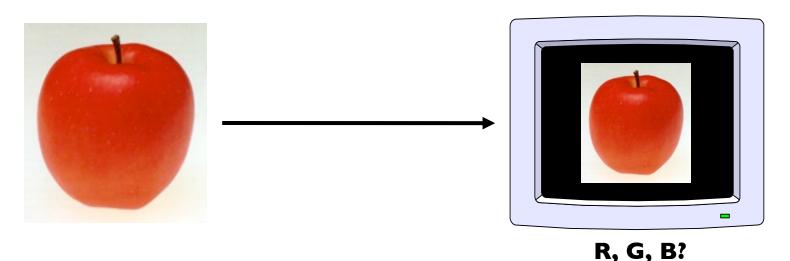
- many colors can be matched by white plus a spectral color
- correlates to everyday concept "hue"

#### Purity

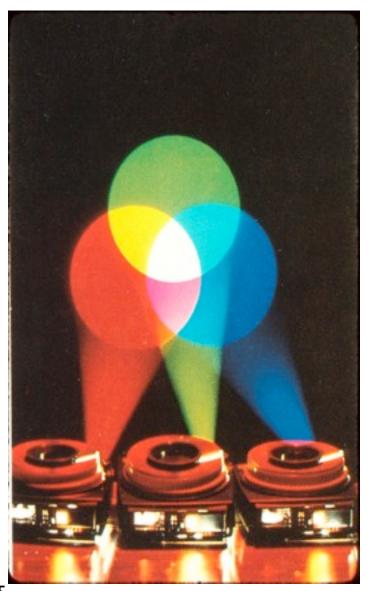
- ratio of pure color to white in matching mixture
- correlates to everyday concept "colorfulness" or "saturation"

#### **Color reproduction**

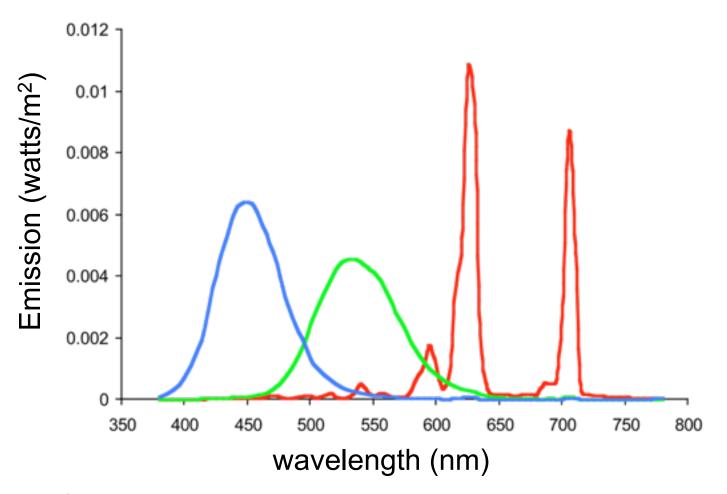
- Have a spectrum s; want to match on RGB monitor
  - "match" means it looks the same
  - any spectrum that projects to the same point in the visual color space is a good reproduction
- Must find a spectrum that the monitor can produce that is a metamer of s



#### **Additive Color**

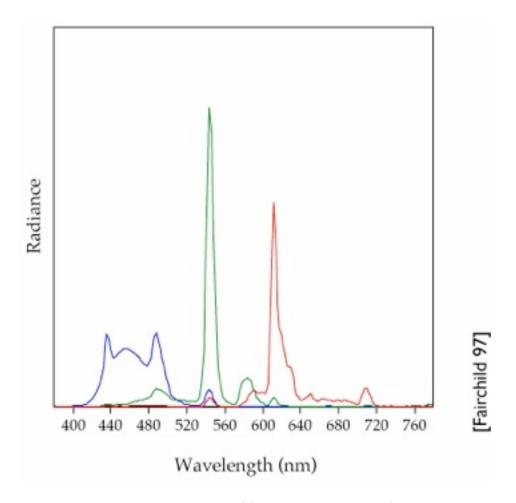


# **CRT** display primaries



- Curves determined by phosphor emission properties

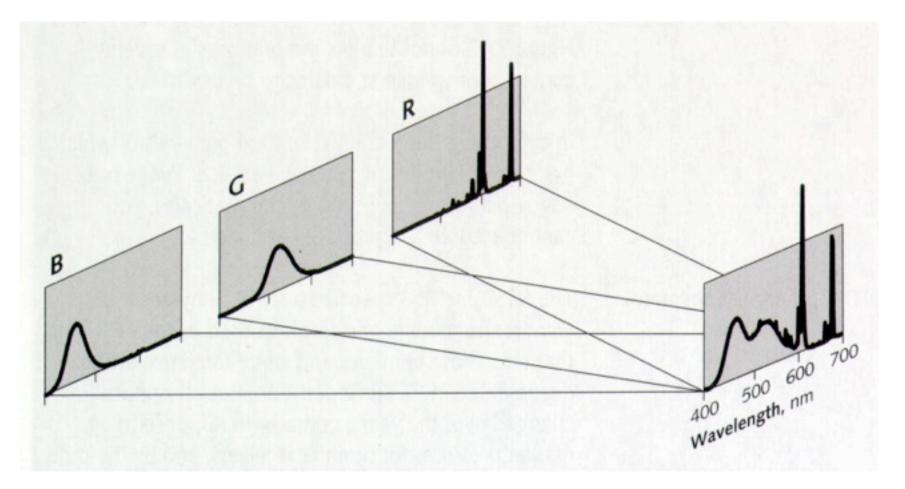
# LCD display primaries



- Curves determined by (fluorescent) backlight and filters

# [source unknown]

# Combining Monitor Phosphors with Spatial Integration

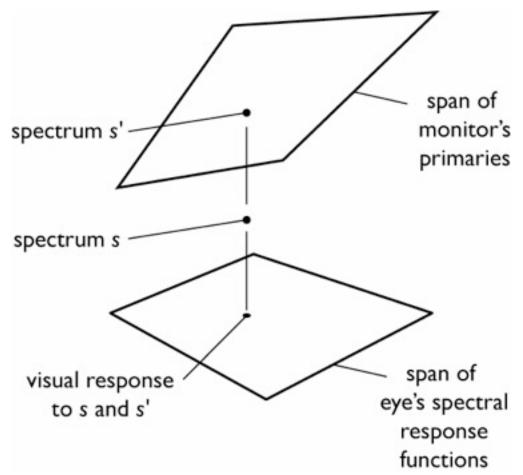


# **Color reproduction**

- Say we have a spectrum s we want to match on an RGB monitor
  - "match" means it looks the same
  - any spectrum that projects to the same point in the visual color space is a good reproduction
- So, we want to find a spectrum that the monitor can produce that matches s
  - that is, we want to display a metamer of s on the screen

# **Color reproduction**

 We want to compute the combination of r, g, b that will project to the same visual response as s.



 The projection onto the three response functions can be written in matrix form:

$$\begin{bmatrix} S \\ M \\ L \end{bmatrix} = \begin{bmatrix} -r_S - \\ -r_M - \\ -r_L - \end{bmatrix} \begin{bmatrix} | \\ s \\ | \end{bmatrix}$$

or,

$$V = M_{SML} s$$
.

• The spectrum that is produced by the monitor for the color signals R, G, and B is:

$$s_a(\lambda) = Rs_r(\lambda) + Gs_g(\lambda) + Bs_b(\lambda).$$

Again the discrete form can be written as a matrix:

$$\begin{bmatrix} | \\ s_a \\ | \end{bmatrix} = \begin{bmatrix} | & | & | \\ s_R & s_G & s_B \\ | & | & | \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix} =$$

or,

$$s_a = M_{RGB} C$$
.

- What color do we see when we look at the display?
  - Feed C to display
  - Display produces s<sub>a</sub>
  - Eye looks at s<sub>a</sub> and produces V

$$V = M_{SML} M_{RGB} C$$

$$\begin{bmatrix} S \\ M \\ L \end{bmatrix} = \begin{bmatrix} r_S \cdot s_R & r_S \cdot s_G & r_S \cdot s_B \\ r_M \cdot s_R & r_M \cdot s_G & r_M \cdot s_B \\ r_L \cdot s_R & r_L \cdot s_G & r_L \cdot s_B \end{bmatrix} \begin{bmatrix} R \\ G \\ B \end{bmatrix}$$

• Goal of reproduction: visual response to s and  $s_a$  is the same:

$$M_{SML}\,\tilde{s} = M_{SML}\,\tilde{s_a}.$$

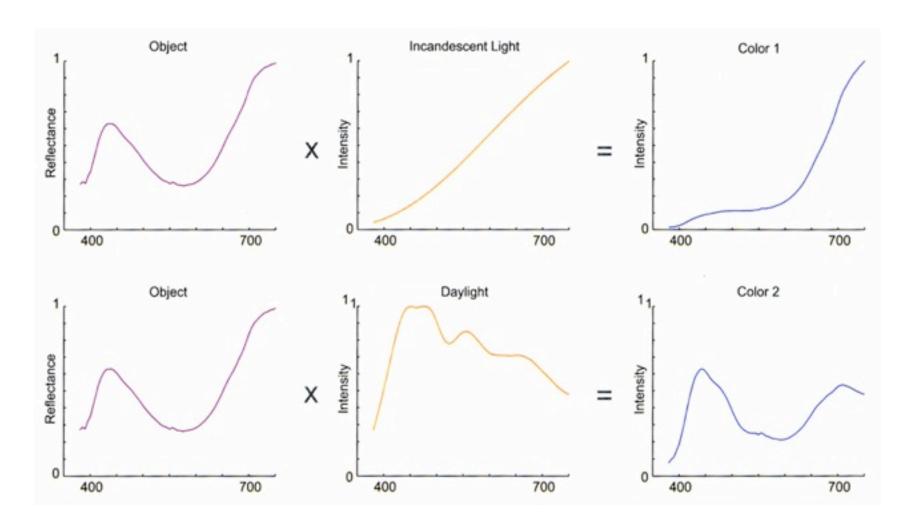
Substituting in the expression for s<sub>a</sub>

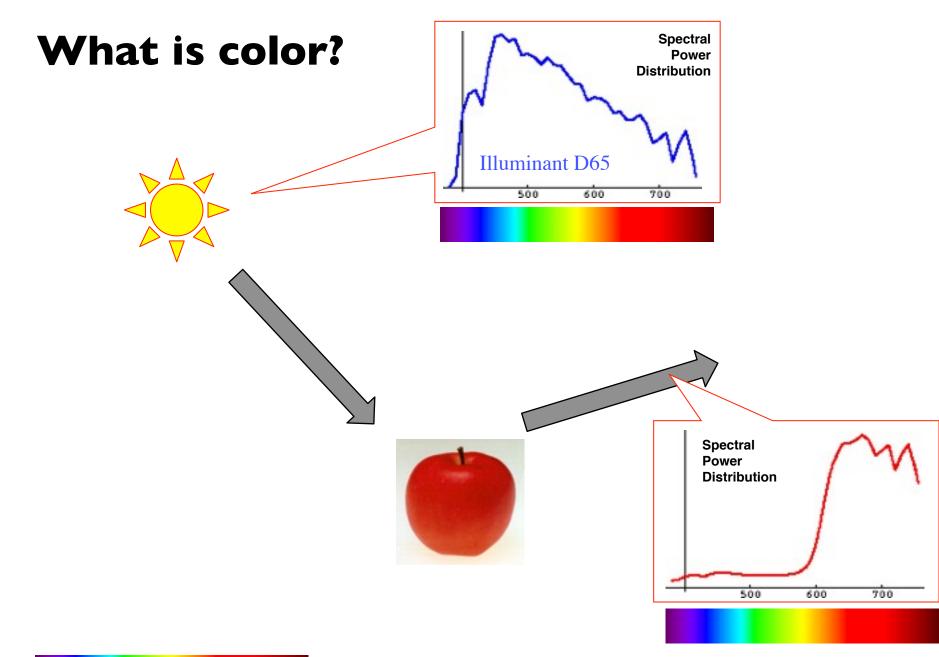
$$M_{SML}\, \tilde{s} = M_{SML} M_{RGB}\, C$$
 
$$C = (M_{SML} M_{RGB})^{-1} M_{SML}\, \tilde{s}$$
 color matching matrix for RGB

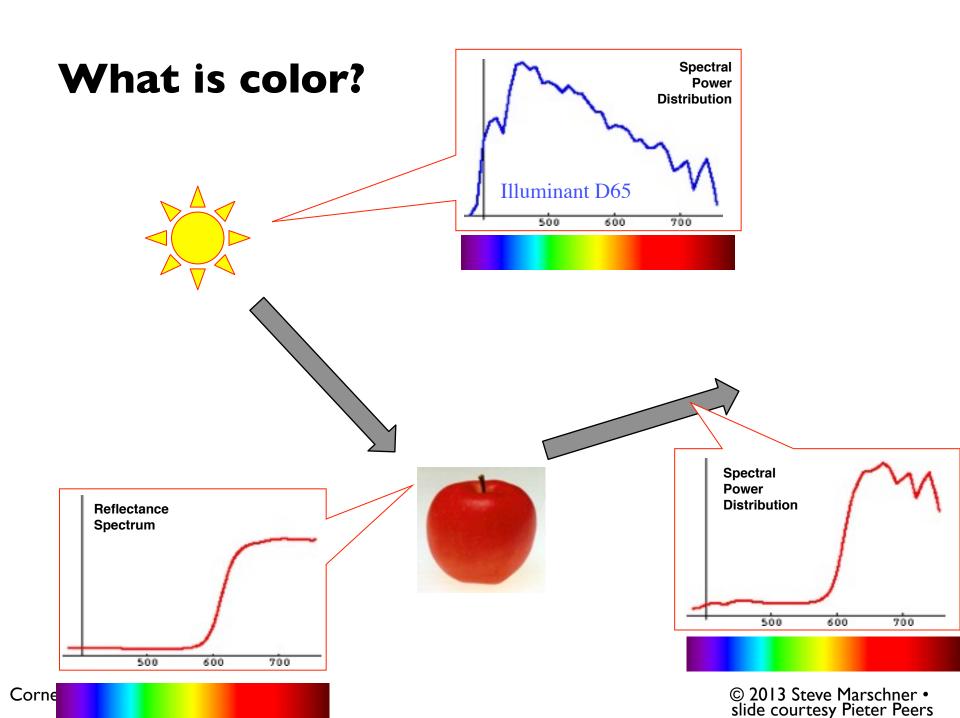
# **Subtractive Color**

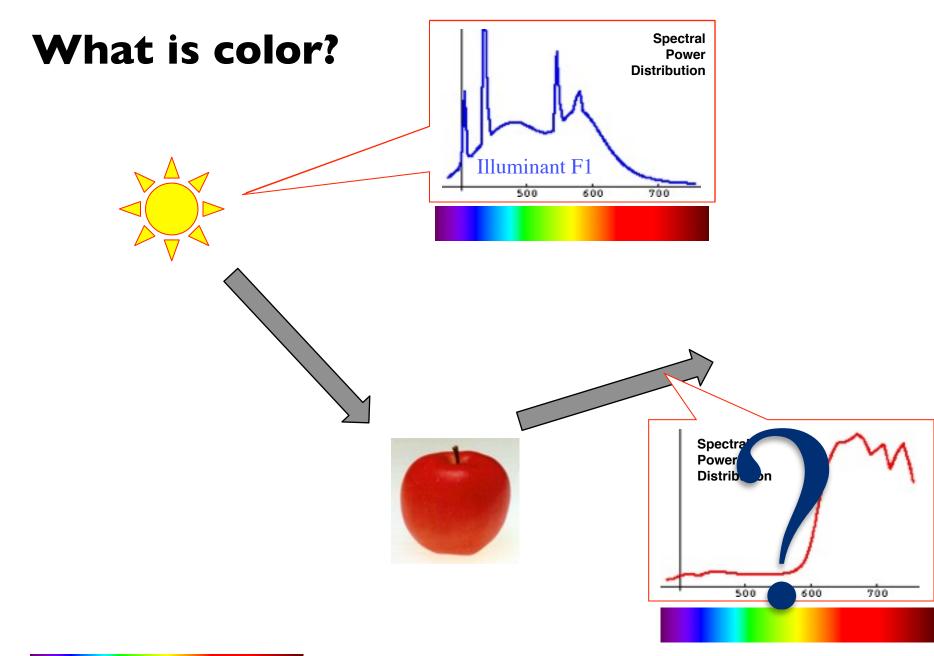


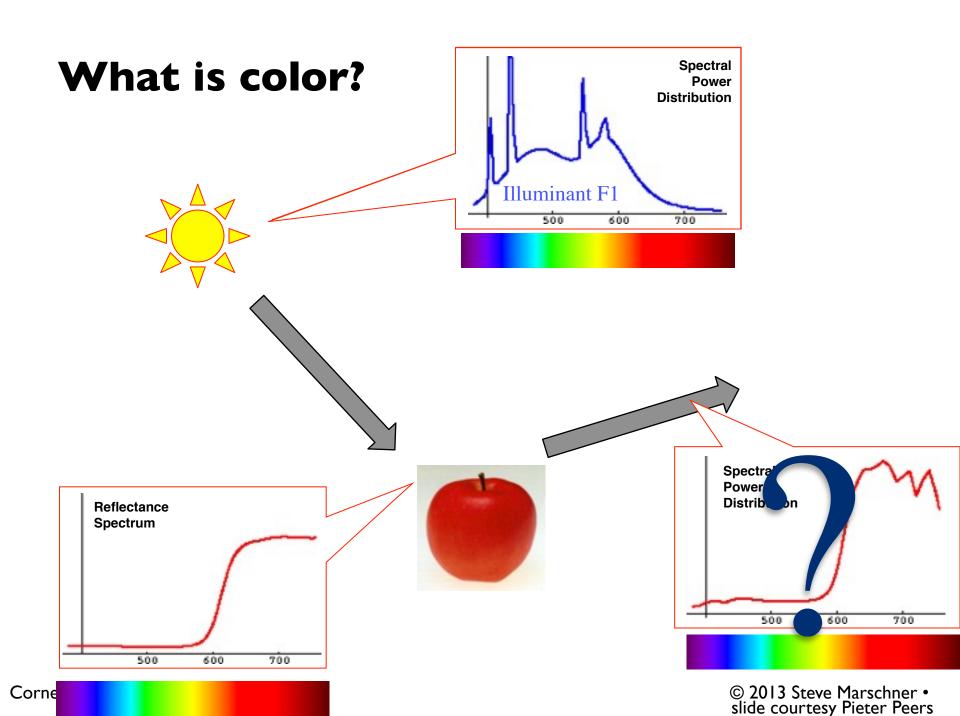
#### Reflection from colored surface

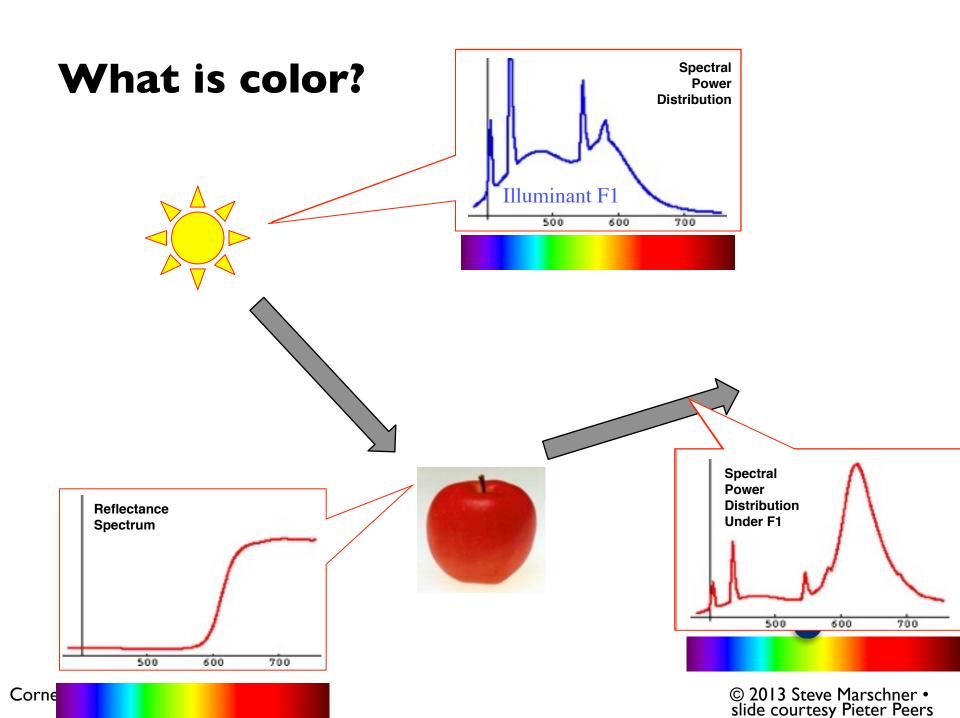












#### **Subtractive color**

- Produce desired spectrum by subtracting from white light (usually via absorption by pigments)
- Photographic media (slides, prints) work this way
- Leads to C, M,Y as primaries
- Approximately, I R, I G, I B

### **Color spaces**

- Need three numbers to specify a color
  - but what three numbers?
  - a color space is an answer to this question
- Common example: monitor RGB
  - define colors by what R, G, B signals will produce them on your monitor

```
(in math, s = RR + GG + BB for some spectra R, G, B)
```

- device dependent (depends on gamma, phosphors, gains, ...)
  - therefore if I choose RGB by looking at my monitor and send it to you, you may not see the same color
- also leaves out some colors (limited gamut), e.g. vivid yellow

# **Standard color spaces**

- Standardized RGB (sRGB)
  - makes a particular monitor RGB standard
  - other color devices simulate that monitor by calibration
  - sRGB is usable as an interchange space; widely adopted today
  - gamut is still limited

# A universal color space: XYZ

- Standardized by CIE (Commission Internationale de l'Eclairage, the standards organization for color science)
- Based on three "imaginary" primaries X, Y, and Z
   (in math, s = XX + YY + ZZ)
  - imaginary = only realizable by spectra that are negative at some wavelengths
  - key properties
    - any stimulus can be matched with positive X, Y, and Z
    - separates out luminance: X, Z have zero luminance, so Y tells you the luminance by itself

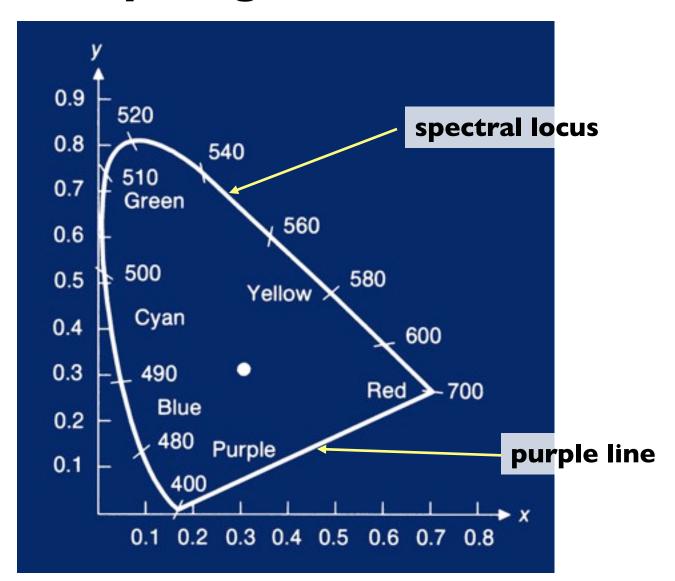
# Separating luminance, chromaticity

- Luminance: Y
- Chromaticity: x, y, z, defined as

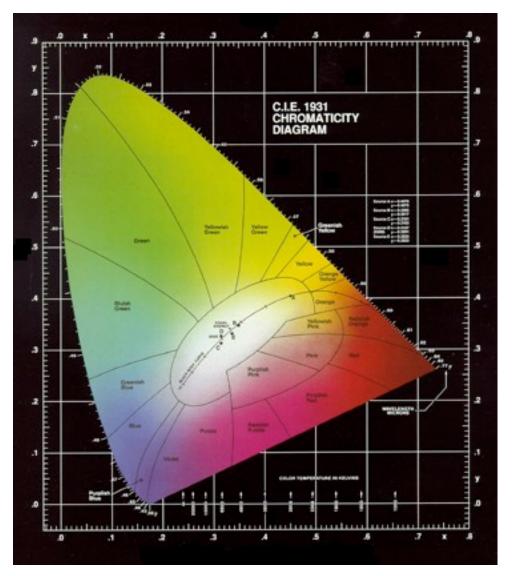
$$x = \frac{X}{X + Y + Z}$$
$$y = \frac{Y}{X + Y + Z}$$
$$z = \frac{Z}{X + Y + Z}$$

- since x + y + z = 1, we only need to record two of the three
  - usually choose x and y, leading to (x, y, Y) coords

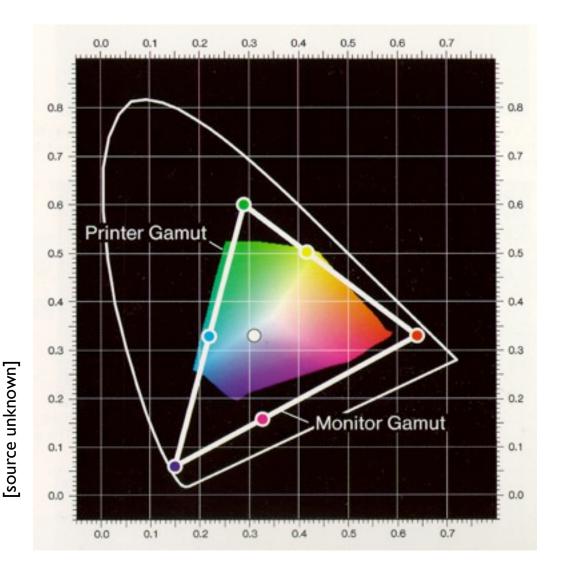
# **Chromaticity Diagram**



# **Chromaticity Diagram**



#### **Color Gamuts**



Monitors/printers can't produce all visible colors

Reproduction is limited to a particular domain

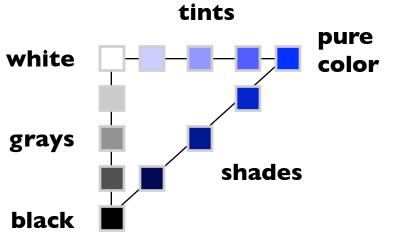
For additive color (e.g. monitor) gamut is the triangle defined by the chromaticities of the three primaries.

# Perceptually organized color spaces

- Artists often refer to colors as tints, shades, and tones of pure pigments
  - tint: mixture with white
  - shade: mixture with black
  - tones: mixture with black and white
  - gray: no color at all (aka. neutral)
- This seems intuitive



• "same" color but lighter, darker, paler, etc.



# Perceptual dimensions of color

#### Hue

- the "kind" of color, regardless of attributes
- colorimetric correlate: dominant wavelength
- artist's correlate: the chosen pigment color

#### Saturation

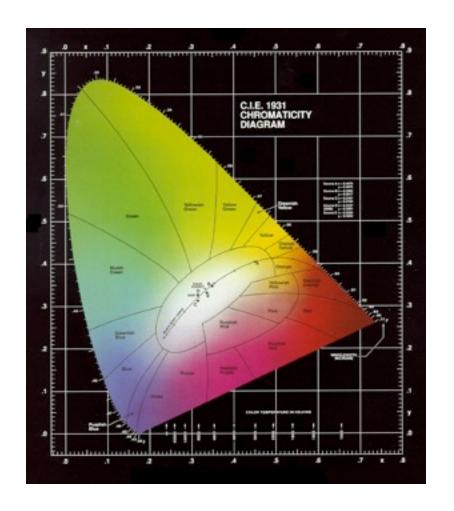
- the "colorfulness"
- colorimetric correlate: purity
- artist's correlate: fraction of paint from the colored tube

#### Lightness (or value)

- the overall amount of light
- colorimetric correlate: luminance
- artist's correlate: tints are lighter, shades are darker

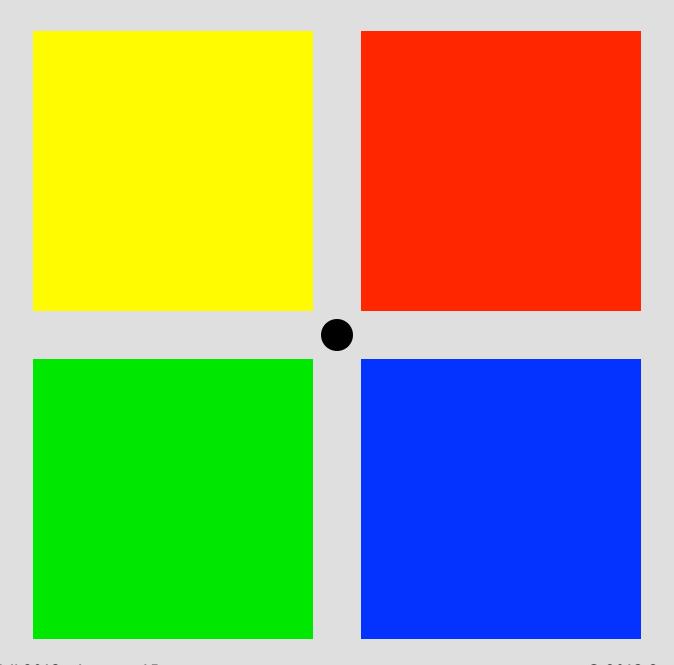
# Perceptual dimensions: chromaticity

- In x, y, Y (or another luminance/chromaticity space), Y corresponds to lightness
- hue and saturation are then like polar coordinates for chromaticity (starting at white, which way did you go and how far?)



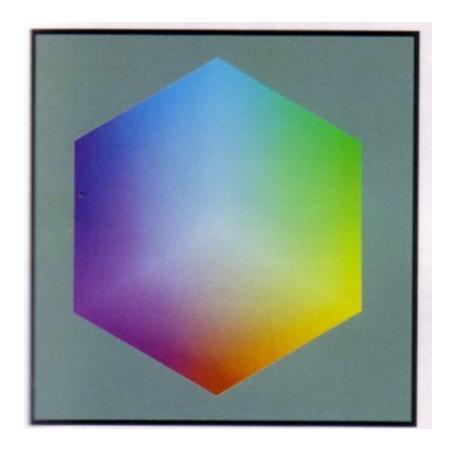
### Perceptual dimensions of color

- There's good evidence ("opponent color theory") for a neurological basis for these dimensions
  - the brain seems to encode color early on using three axes:
     white black, red green, yellow blue
  - the white—black axis is lightness; the others determine hue and saturation
  - one piece of evidence: you can have a light green, a dark green, a yellow-green, or a blue-green, but you can't have a reddish green (just doesn't make sense)
    - thus red is the opponent to green
  - another piece of evidence: afterimages (next slide)



# RGB as a 3D space

• A cube:

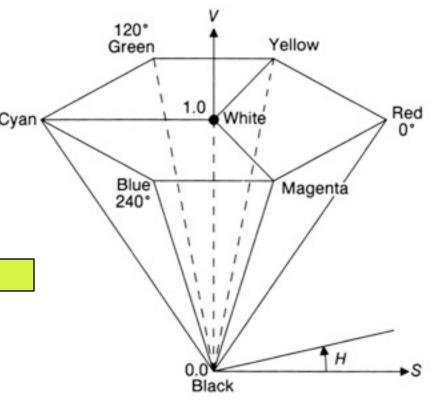


(demo of RGB cube)

# Perceptual organization for RGB: HSV

- Uses hue (an angle, 0 to 360), saturation (0 to 1), and value (0 to 1) as the three coordinates for a color
  - the brightest available
     RGB colors are those
     with one of R,G,B
     equal to I (top surface)
  - each horizontal slice is the surface of a sub-cube of the RGB cube

(demo of HSV color pickers)



# Perceptually uniform spaces

- Two major spaces standardized by CIE
  - designed so that equal differences in coordinates produce equally visible differences in color
  - LUV: earlier, simpler space; L\*, u\*, v\*
  - LAB: more complex but more uniform:  $L^*$ ,  $a^*$ ,  $b^*$
  - both separate luminance from chromaticity
  - including a gamma-like nonlinear component is important