Viewing and Ray Tracing

CS 4620 Lecture 2
Parallel projection

• To render an image of a 3D scene, we *project* it onto a plane
• Simplest kind of projection is *parallel projection*
Two approaches to rendering
Two approaches to rendering

for each object in the scene {
    for each pixel in the image {
        if (object affects pixel) {
            do something
        }
    }
}

object order
or
rasterization
Two approaches to rendering

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    for each pixel in the image {
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    }
}

object order
or
rasterization

for each pixel in the image {
    for each object in the scene {
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}

image order
or
ray tracing
Two approaches to rendering

object order
or
rasterization

image order
or
ray tracing

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}

We will do this first
Ray tracing idea

- Start with a pixel—what belongs at that pixel?
- Set of points that project to a point in the image: a ray
Ray tracing idea

- Start with a pixel—what belongs at that pixel?
- Set of points that project to a point in the image: a **ray**

![Diagram showing ray tracing process](image)
Ray tracing idea
Ray tracing idea

viewer (eye)

light source

objects in scene
Ray tracing idea

viewer (eye) → viewing ray → visible point → objects in scene
Ray tracing idea
Ray tracing algorithm

for each pixel {
    compute viewing ray
    intersect ray with scene
    compute illumination at visible point
    put result into image
}
Generating viewing rays

• For a given pixel in the image, what is the corresponding ray?
  – this ray contains all the points that project to a single point in the image

• To answer it, we need an exact specification of the view
Classical projections—parallel

- Emphasis on cube-like objects
  - traditional in mechanical and architectural drawing

Planar Geometric Projections

Parallel

Orthographic

Oblique

Multiview Orthographic

Axonometric

Perspective

One-point

Two-point

Three-point

[after Carlbom & Paciorek 78]
Orthographic

Figure 2-1. Multiview orthographic projection: plan, elevations, and section of a building.
Orthographic

- projection plane parallel to a coordinate plane
- projection direction perpendicular to projection plane
Off-axis parallel

**axonometric**: projection plane perpendicular to projection direction but not parallel to coordinate planes

**oblique**: projection plane parallel to a coordinate plane but not perpendicular to projection direction.

[Carlson & Paciorek 78]
“Orthographic” projection

- In graphics usually we lump axonometric with orthographic
  - projection plane perpendicular to projection direction
  - image height determines size of objects in image
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Oblique projection

- View direction no longer coincides with projection plane normal (one more parameter)
  - objects at different distances still same size
  - objects are shifted in the image depending on their depth
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Vector math review

• Vectors and points
• Vector operations
  – addition
  – scalar product
• More products
  – dot product
  – cross product
• Bases and coordinates
• Orthogonality and orthonormal bases
Generating eye rays—orthographic

• Ray origin (varying): pixel position on viewing window
• Ray direction (constant): view direction

– but where exactly is the view rectangle?
Generating eye rays—parallel

- Positioning the view rectangle
  - establish three vectors to be camera basis: \( \mathbf{u}, \mathbf{v}, \mathbf{w} \)
  - view rectangle is in \( \mathbf{u}–\mathbf{v} \) plane, specified by \( l, r, t, b \)
    (often \( l = -r \) and \( b = -t \))
- Generating rays
  - for \((u, v)\) in \([l, r] \times [b, t]\)
  - \(\text{ray.origin} = e + u \mathbf{u} + v \mathbf{v}\)
  - \(\text{ray.direction} = -\mathbf{w}\)
Oblique parallel views

• View rectangle is the same
  – ray origins identical to orthographic
  – view direction \( \mathbf{d} \) differs from \(-\mathbf{w}\)

• Generating rays
  – for \((u, v)\) in \([l, r] \times [b, t]\)
  – ray.origin = \(e + u \mathbf{u} + v \mathbf{v}\)
  – ray.direction = \(\mathbf{d}\)
Establishing the camera basis

• Could require user to provide \( \mathbf{e}, \mathbf{u}, \mathbf{v}, \) and \( \mathbf{w} \)
  – but this is error prone and unintuitive
• Instead, calculate basis from things the user cares about
  – viewpoint: where the camera is \( \rightarrow \mathbf{e} \)
  – view direction: which way the camera is looking \( \rightarrow \mathbf{d} \)
  – view plane normal (by default, same as view direction)
  – up vector: how the camera is oriented
• This is enough to calculate \( \mathbf{u}, \mathbf{v}, \) and \( \mathbf{w} \)
  – set \( \mathbf{w} \) parallel to v.p. normal, facing away from \( \mathbf{d} \)
  – set \( \mathbf{u} \) perpendicular to \( \mathbf{w} \) and perpendicular to up-vector
  – set \( \mathbf{v} \) perpendicular to \( \mathbf{w} \) and \( \mathbf{u} \) to form a right-handed ONB
Pixel-to-image mapping

- One last detail: \((u, v)\) coords of a pixel

\[
\begin{align*}
  u &= l + (r - l)(i + 0.5)/n_x \\
  v &= b + (t - b)(j + 0.5)/n_y
\end{align*}
\]
Specifying views in Ray 1

```xml
<camera type="ParallelCamera">
  <viewPoint>2.0 4.0 7.0</viewPoint>
  <viewDir>-2.0 -4.0 -7.0</viewDir>
  <viewUp>0.0 1.0 0.0</viewUp>
  <viewWidth>8.0</viewWidth>
  <viewHeight>4.5</viewHeight>
</camera>

<camera type="ParallelCamera">
  <viewPoint>2.0 4.0 7.0</viewPoint>
  <viewDir>-2.0 -4.0 -7.0</viewDir>
  <projNormal>0.0 0.0 1.0</projNormal>
  <viewUp>0.0 1.0 0.0</viewUp>
  <viewWidth>8.0</viewWidth>
  <viewHeight>4.5</viewHeight>
</camera>
```
History of projection

- Ancient times: Greeks wrote about laws of perspective
- Renaissance: perspective is adopted by artists

Duccio c. 1308
History of projection

• Later Renaissance: perspective formalized precisely

(da Vinci c. 1498)
Plane projection in drawing
Plane projection in drawing

The concept of the picture plane may be better understood by looking through a window or other transparent plane from a fixed viewpoint. Your lines of sight, the multitude of straight lines leading from your eye to the subject, will all intersect this plane. Therefore, if you were to reach out with a grease pencil and draw the image of the subject on this plane you would be "tracing out" the infinite number of points of intersection of sight rays and plane. The result would be that you would have "transferred" a real three-dimensional object to a two-dimensional plane.
Plane projection in photography

- This is another model for what we are doing
  - applies more directly in realistic rendering
Plane projection in photography
Classical projections—perspective

- Emphasis on cube-like objects
  - traditional in mechanical and architectural drawing
**Perspective**

**one-point**: projection plane parallel to a coordinate plane (to two coordinate axes)

**two-point**: projection plane parallel to one coordinate axis

**three-point**: projection plane not parallel to a coordinate axis
Perspective projection (normal)

• Perspective is projection by lines through a point; “normal” = plane perpendicular to view direction
  – magnification determined by:
    • image height
    • object depth
    • image plane distance
  – f.o.v. $\alpha = 2 \ \text{atan}(h/(2d))$
  – $y' = d \ y / z$
  – “normal” case corresponds to common types of cameras
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    - image height
    - object depth
    - image plane distance
  - f.o.v. $\alpha = 2 \tan \left( \frac{h}{2d} \right)$
  - $y' = \frac{dy}{z}$
- “normal” case corresponds to common types of cameras
Shifted perspective projection

- Perspective but with projection plane not perpendicular to view direction
  - additional parameter: projection plane normal
  - exactly equivalent to cropping out an off-center rectangle from a larger “normal” perspective
  - corresponds to view camera in photography
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Generating eye rays—perspective

- Use window analogy directly
- Ray origin (constant): viewpoint
- Ray direction (varying): toward pixel position on viewing window
Generating eye rays—perspective

• Positioning the view rectangle
  – establish three vectors to be camera basis: \( \mathbf{u}, \mathbf{v}, \mathbf{w} \)
  – view rectangle is parallel to \( \mathbf{u} - \mathbf{v} \) plane, at \( w = -d \), specified by \( l, r, t, b \)

• Generating rays
  – for \((u, v)\) in \([l, r] \times [b, t]\)
  – ray.orientation = \(e\)
  – ray.direction = \(-d \mathbf{w} + u \mathbf{u} + v \mathbf{v}\)
Oblique perspective views

• Positioning the view rectangle
  – establish three vectors to be
    *camera basis*: $\mathbf{u}, \mathbf{v}, \mathbf{w}$
  – view rectangle is the same, but shifted so that the center is in the direction $\mathbf{d}$ from $\mathbf{e}$

• Generating rays
  – for $(u, v)$ in $[l, r] \times [b, t]$  
  – ray.origin = $\mathbf{e}$
  – ray.direction = $\mathbf{d} \mathbf{d} + u \mathbf{u} + v \mathbf{v}$
Perspective views in Ray 1

```xml
<camera type="PerspectiveCamera">
  <viewPoint>3.0 6.0 10.5</viewPoint>
  <viewDir>–3.0 –6.0 –10.5</viewDir>
  <viewUp>0.0 1.0 0.0</viewUp>
  <projDistance>13.0</projDistance>
  <viewWidth>8.0</viewWidth>
  <viewHeight>4.5</viewHeight>
</camera>

<camera type="PerspectiveCamera">
  <viewPoint>3.0 6.0 10.5</viewPoint>
  <viewDir>–3.0 –6.0 –10.5</viewDir>
  <projNormal>0.0 0.0 1.0</projNormal>
  <viewUp>0.0 1.0 0.0</viewUp>
  <projDistance>11.0</projDistance>
  <viewWidth>8.0</viewWidth>
  <viewHeight>4.5</viewHeight>
</camera>
```
Field of view (or f.o.v.)

• The angle between the rays corresponding to opposite edges of a perspective image
  – simpler to compute for “normal” perspective
  – have to decide to measure vert., horiz., or diag.
• In cameras, determined by focal length
  – confusing because of many image sizes
  – for 35mm format (36mm by 24mm image)
    • 18mm = 67° v.f.o.v. — super-wide angle
    • 28mm = 46° v.f.o.v. — wide angle
    • 50mm = 27° v.f.o.v. — “normal”
    • 100mm = 14° v.f.o.v. — narrow angle (“telephoto”)
Field of view

- Determines “strength” of perspective effects

close viewpoint
- wide angle
- prominent foreshortening

far viewpoint
- narrow angle
- little foreshortening
Choice of field of view

• In photography, wide angle lenses are specialty tools
  – “hard to work with”
  – easy to create weird-looking perspective effects
• In graphics, you can type in whatever f.o.v. you want
  – and people often type in big numbers!
Perspective distortions

- Lengths, length ratios
Why shifted perspective?

• Control convergence of parallel lines
• Standard example: architecture
  – buildings are taller than you, so you look up
  – top of building is farther away, so it looks smaller
• Solution: make projection plane parallel to facade
  – top of building is the same distance from the projection plane
• Same perspective effects can be achieved using post-processing
  – (though not the focus effects)
  – choice of which rays vs. arrangement of rays in image
camera tilted up: converging vertical lines
lens shifted up: parallel vertical lines
Specifying perspective projections

• Many ways to do this
  – common: from, at, up, v.f.o.v. (but not for shifted)
• One way (used in ray tracer):
  – viewpoint, view direction, up
    • establishes location and orientation of viewer
    • view direction is the direction of the center ray
  – image width, image height, projection distance
    • establishes size and location of image rectangle
  – image plane normal
    • can be different from view direction to get shifted perspective