

# **CS4620/5620: Lecture 24**

## **Texture Mapping**

## **Announcements**

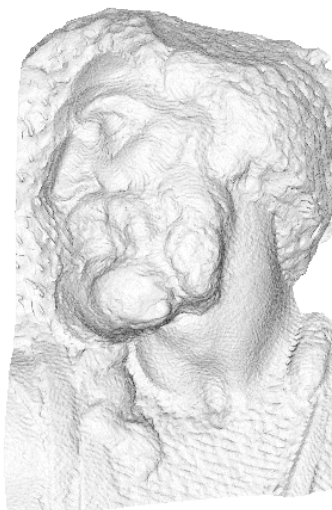
- PA2B out today
  - Material will be covered today and Wed
- Plan for next few lectures
  - Texturing
  - Wed: Perlin noise, Sampling and anti-aliasing
  - Friday onwards: Splines

## Other uses of texture mapping

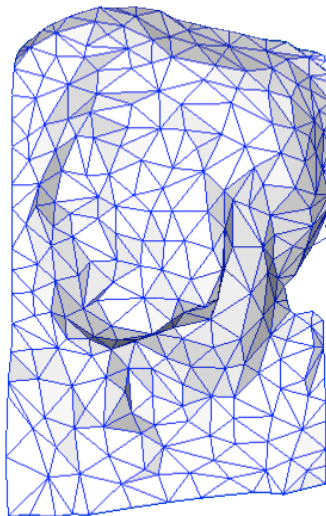
- Reflection maps
- Environment maps
- Normal maps
- Bump maps
- Displacement maps
- Shadow maps
- Irradiance maps
- ...

## Normal mapping

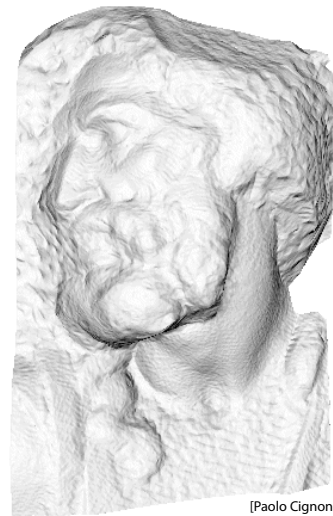
- Stores normals as texture map over coarse geometry



original mesh  
4M triangles



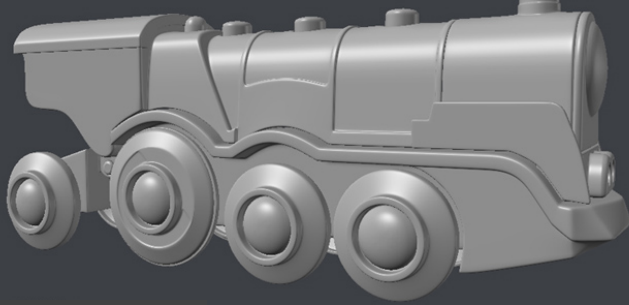
simplified mesh  
500 triangles



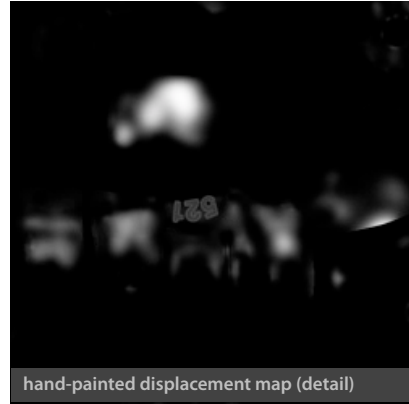
[Paolo Cignoni]

simplified mesh  
and normal mapping  
500 triangles

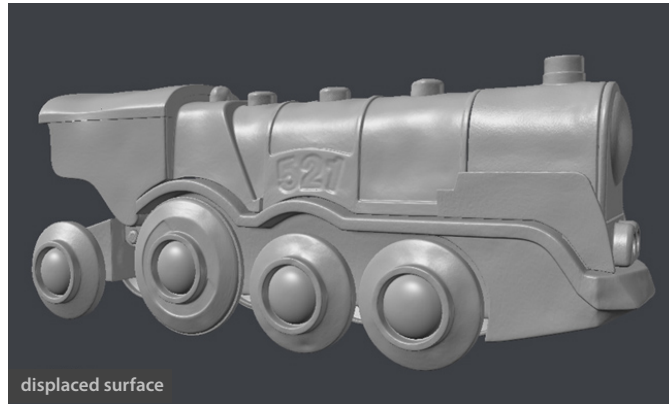
# Displacement mapping



base subdivision surface

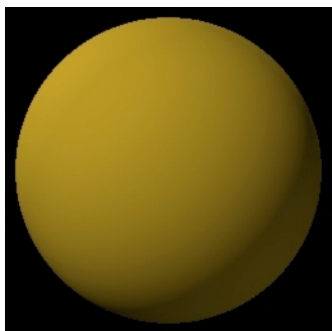


hand-painted displacement map (detail)

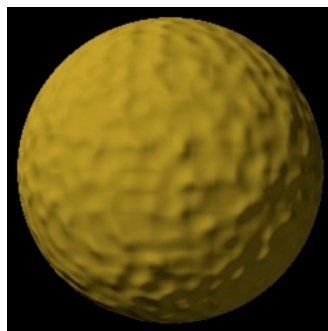


displaced surface

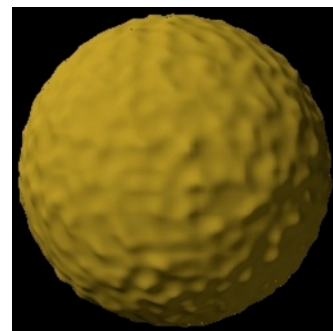
Pawel Filip  
tolas.wordpress.com



no map



normal map

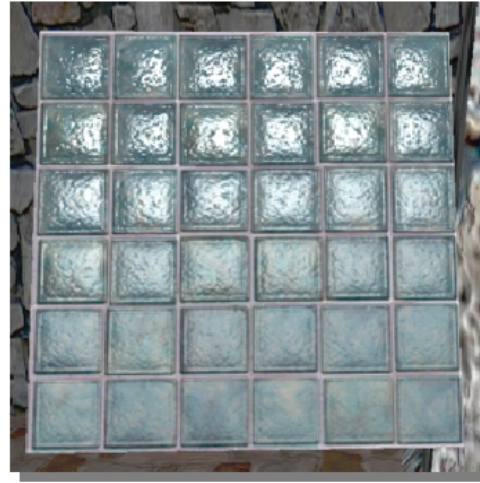


displacement map

# Altogether: Gloss Maps/Normal Maps

$$n \cdot l \cdot d + (n \cdot h)^m \cdot g$$

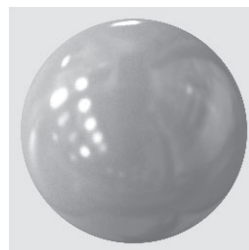
ATI Technologies, Inc.



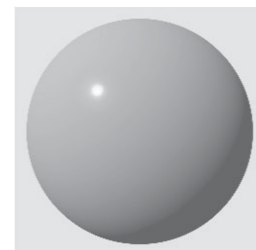
- Normal maps, diffuse map, gloss map, shininess maps

## Reflection mapping

- Early (earliest?) non-decal use of textures
- Appearance of shiny objects
  - Phong highlights produce blurry highlights for glossy surfaces.
  - A polished (shiny) object reflects a sharp image of its environment.
- The whole key to a shiny-looking material is providing something for it to reflect.



(a)



(b)

[Dror, Willsky, & Adelson 2004]

Figure 2. (a). A shiny sphere rendered under photographically acquired real-world illumination. (b). The same sphere rendered under illumination by a point light source.

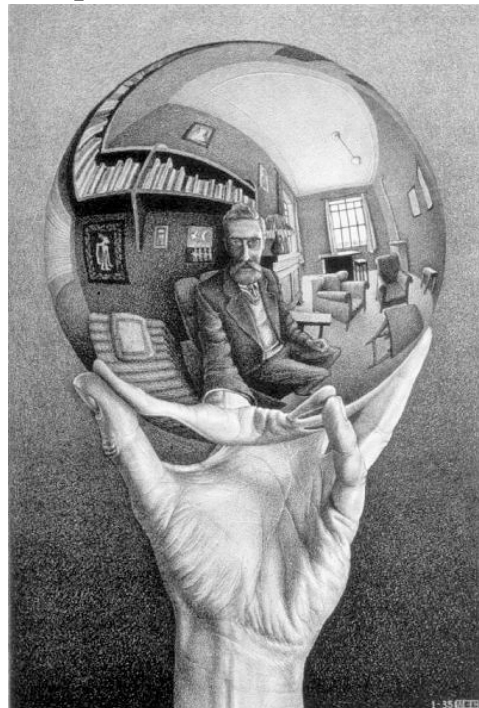
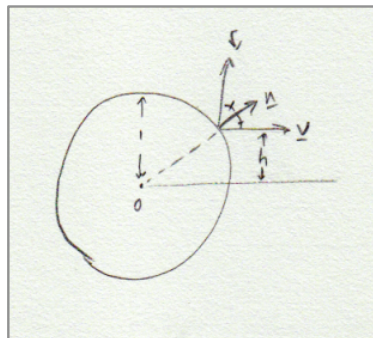
# Environment map

- A function from the sphere to colors, stored as a texture.



[Blinn & Newell 1976]

# Spherical environment map



Hand with Reflecting Sphere. M. C. Escher, 1935. lithograph

# Spherical environment maps



[Paul Debevec]

## Types of Mappings: Cube Mapping



Cube mapping



# Sphere Mapping Example



## Other uses of texture mapping

- Reflection maps
- Environment maps
- Normal maps
- Bump maps
- Displacement maps
- Shadow maps
- Irradiance maps
- ...

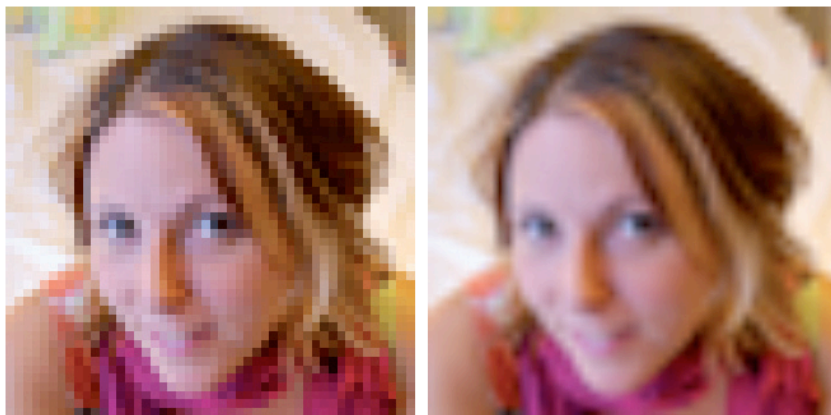
## Another definition

**Texture mapping:** a general technique for storing and evaluating functions.

- They're not just for shading parameters any more!

## Texture mapping from 0 to infinity

- When you go close...





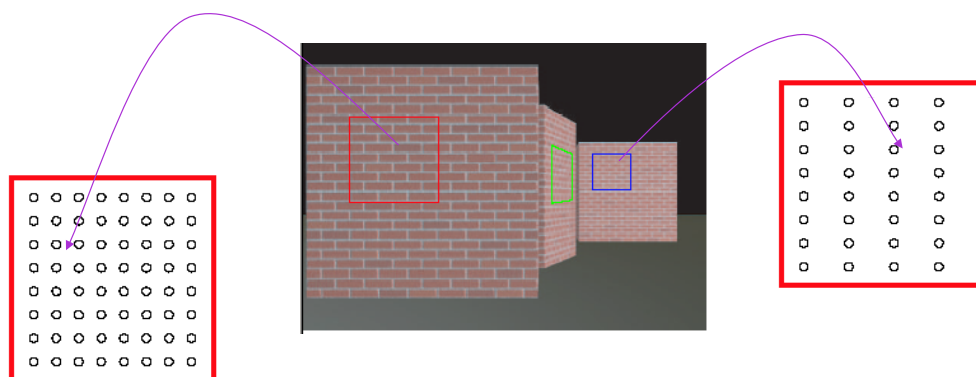
## When viewed from a distance

- Aliasing!
- Also, minification

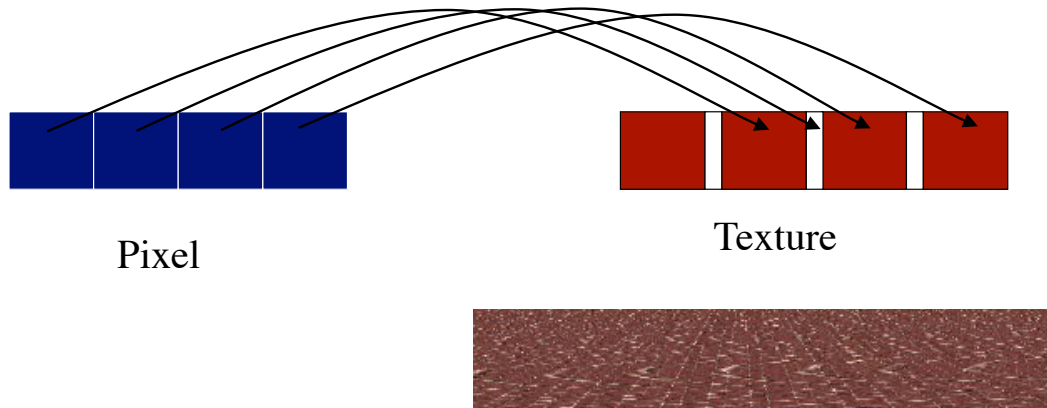


## What is going on?

- Image-based texture mapping is resolution dependent



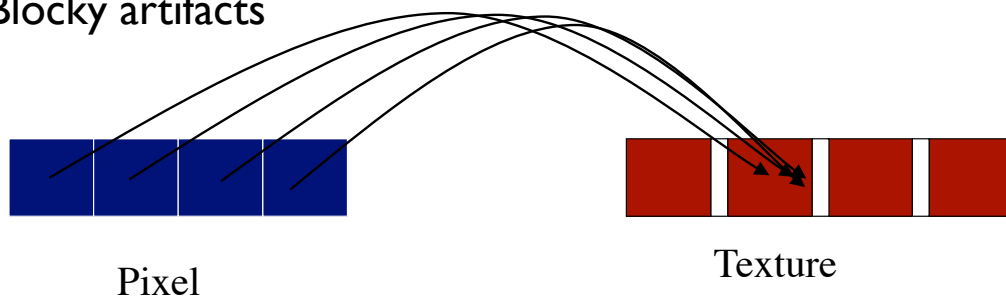
## What is texture lookup doing? Sampling a single point



- From far away
- Scintillating artifacts over multiple frames

## When viewed closer...

- Nearby pixels all lie in same texel
- Blocky artifacts

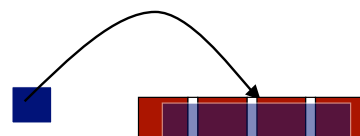
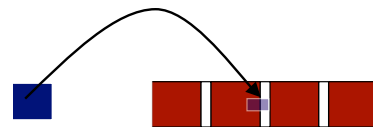
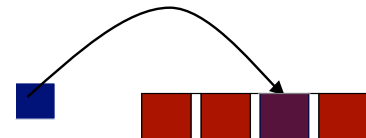


## What is really the issue?

- A pixel is not a point
  - It is an area!
- Each pixel maps to some region of texture space
- Ideally, we want to integrate over mapped area

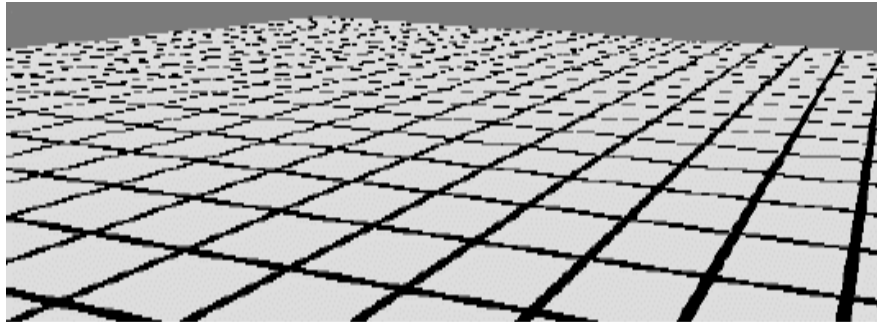
## How does area map over distance?

- At optimal viewing distance:
  - One-to-one mapping between pixel area and texel area
- When closer
  - Each pixel is a small part of the texel
- When farther
  - Each pixel could include many texels



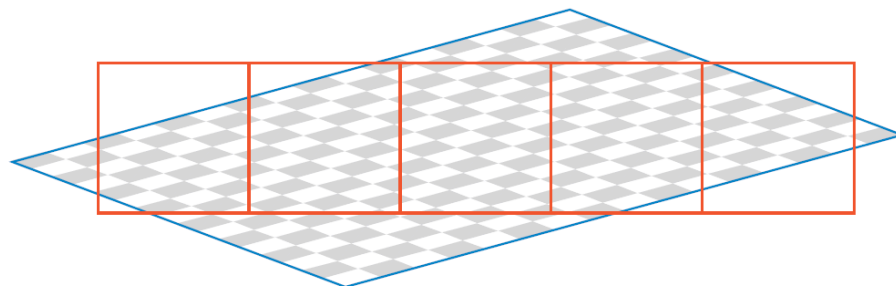
## Solution: Antialiasing in textures

- Problem: Perspective produces very high image frequencies
- Solution
  - Would like to render textures with one (few) samples/pixel
  - Need to filter first!



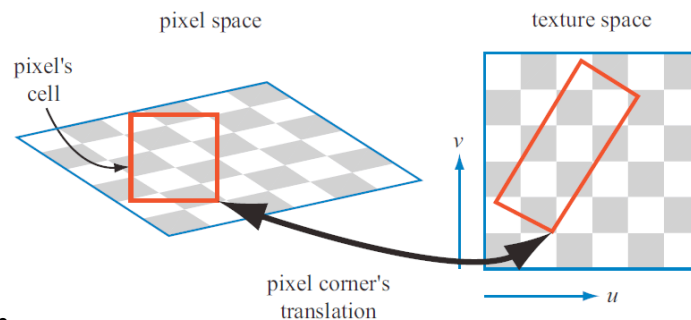
## Theoretical Solution

- Find the area of pixel in texture space
- “Filter” the area to compute “average” texture color
  - Filtering eliminates high frequency artifacts



## Theoretical Solution

- Find the area of pixel in texture space
- “Filter” the area to compute “average” texture color
  - Filtering eliminates high frequency artifacts
- How to filter?
  - Analytically compute area
  - But too expensive



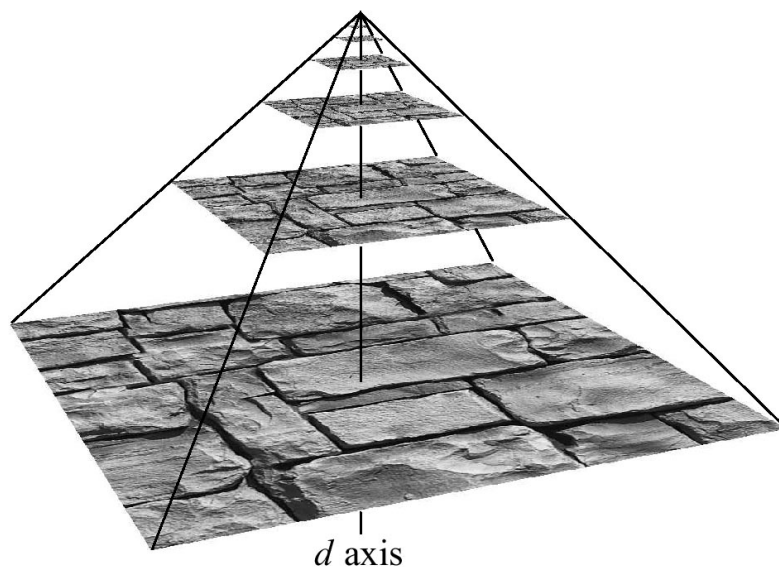
## Solutions for Minification

- Need some way to access pre-filtered (precomputed) regions of the texture
- MIP Maps
- RIP Maps
- Summed Area Tables
- Clip Maps

# MIP Maps

- MIP Maps
  - Multum in Parvo: Much in little, many in small places
  - Proposed by Lance Williams
- Stores pre-filtered versions of texture
- Supports very fast lookup

## Mipmap image pyramid



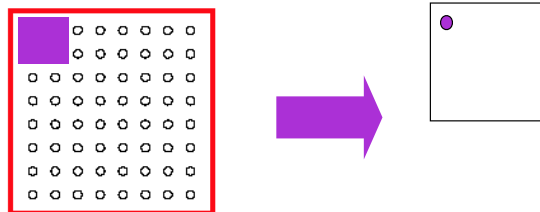
[Akenine-Möller & Haines 2002]



## Some basic assumptions

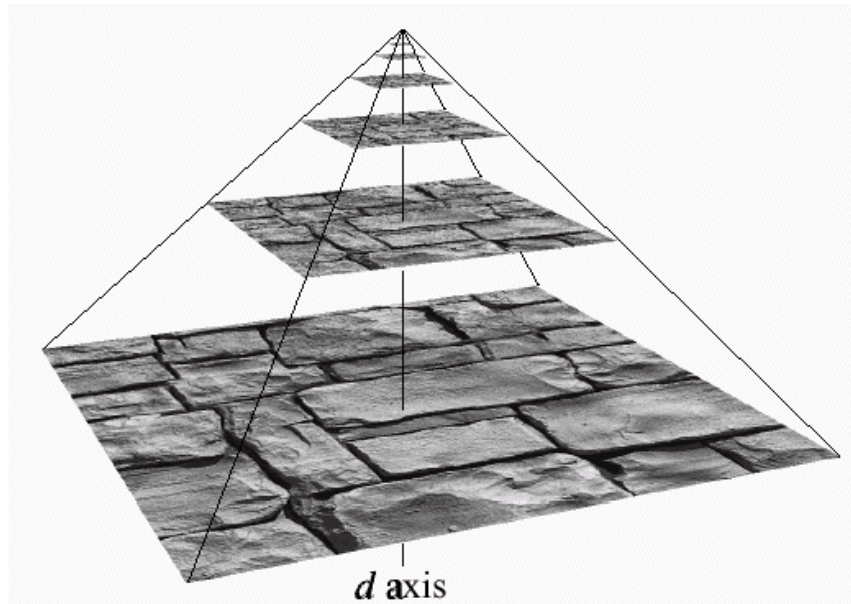
- Can't really precompute every possible required area
- But can precompute some areas

## Filtering by Averaging



- Each pixel in a level corresponds to 4 pixels in lower level
  - Average
  - Gaussian filtering (more on this next lecture)

# Image Pyramid



## Using the MIP Map

- Find the MIP Map level where the pixel has a 1-to-1 mapping
- How?
  - Find largest side of pixel footprint in texture space
    - Pick level where that side corresponds to a texel
  - Compute derivatives to find pixel footprint
    - Intuition for derivatives

## Using the MIP Map

- Find the MIP Map level where the pixel has a 1-to-1 mapping
- How?
  - Find largest side of pixel footprint in texture space
    - Pick level where that side corresponds to a texel
  - Compute derivatives to find pixel footprint
    - x derivative:  $\frac{\partial u}{\partial x} \quad \frac{\partial v}{\partial x}$
    - y derivative:  $\frac{\partial u}{\partial y} \quad \frac{\partial v}{\partial y}$

## Given derivatives: what is level?

$$level = \log[\max(\frac{du}{dx}, \frac{dv}{dx}, \frac{du}{dy}, \frac{dv}{dy})]$$

$$level = \log \sqrt{(\frac{du}{dx})^2 + (\frac{dv}{dx})^2 + (\frac{du}{dy})^2 + (\frac{dv}{dy})^2}$$

- Gradients
  - Available in pixel shader (except where there is dynamic branching)