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CS4620 Fall 2011  
HW4 - Curves and Animation

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Due: Nov 22 2011

## 1 B-Spline and Bezier Curves

Consider the B-spline to Bezier conversion algorithm covered in Lecture 28, Slide 20 (Boehms conversion). Prove that the corresponding Bezier curves rendered, in fact, are the same as the originally intended B-spline curve.

We will simplify this problem, by not worrying about the end cases. Further, in the slide, we create 3 new Bezier curves; you will only derive the equivalence of the middle Bezier curve (shown by the thick green curve in the figure, reproduced here for your convenience).

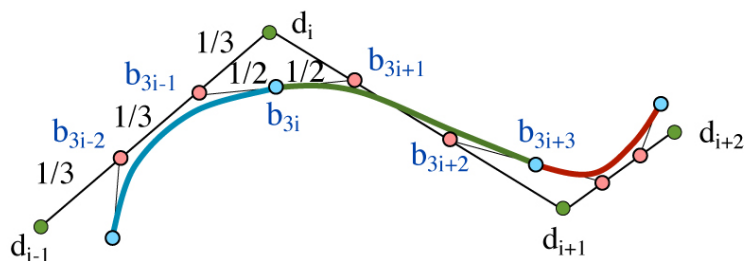


Figure 1: Bspline to Bezier conversion.

Hint: to solve this problem you will need to do the following. Derive the Bezier points,  $b$ , for the green curve in terms of the associated B-spline points,  $d$ . Given the matrices of Bezier and Bspline curves prove that the green curve is the "right" curve.

## 2 Quaternions

### 2.1

Let  $q_0 = \frac{1}{2} + \frac{\sqrt{3}}{2}\mathbf{k}$ . What rotation does  $q_0$  represent? That is,  $q_0$  represents the rotation around which vector and by what angle?

### 2.2

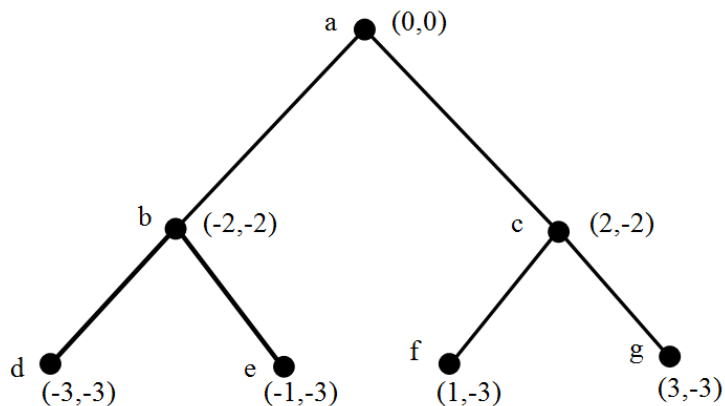
Let  $q_1 = \frac{\sqrt{3}}{2} + \frac{1}{2}\mathbf{k}$ . Compute  $\text{slerp}(q_0, q_1, 0.5)$ .

### 2.3

Let  $q$  be a unit quaternion. Show that  $q$  and  $-q$  represent the same rotation.

## 3 Forward Kinematics

Consider the following articulated rigid body in its rest pose. Here,  $a$  is the



root joint. All the positions are *world positions* of the joints/end effectors. They are not relative positions to the joints'/end effectors' parents.

Draw the rigid body when it is in the following pose:

$$\theta_a = 45^\circ, \theta_b = -45^\circ, \theta_c = 45^\circ.$$

Also, specify the positions of all the joints and end effectors.