Say we are using Newton’s method to minimize a function $g(x)$. Assuming $g'(x_k) \neq 0$ and $g''(x_k) > 0$ (and that the third derivatives exist and are bounded), argue that there is some sufficiently small $\alpha_k > 0$ such that $g(x_{k+1}) < g(x_k)$.