Consider the (real) inner product on $P_2$ defined by

$$\langle p, q \rangle = \int_{-1}^{1} p(x)q(x) \, dx.$$

A real inner product is a symmetric positive bilinear form, so in any given basis it is represented by some symmetric positive definite matrix $A$. What is the matrix for this inner product for the power basis?