

CS412 Homework 4

1. Consider a `switch` construct with the following syntax:

```
switch(E) {
  case v1: S1;
  ...
  case vn: Sn;
  default: Sd;
}
```

where `E` is an expression, `v1`, ..., `vn` are constants, and `S1`, ..., `Sn`, `Sd` are statements in the program. When the value of `E` matches the constant `vk`, the program executes statement `Sk`; if the program doesn't match any case, it executes the default statement `Sd`. The execution of each case doesn't fall through to the next case. One way to implement this construct in low IR is by testing each case sequentially. However, for constructs with a large number of cases, this implementation can be slow for those cases listed at the end.

- (a) If the listed cases represent a dense set in some range of values $[l,u]$, a better implementation is to use a jump table containing case labels and have a single table lookup to figure out the matching case. Give a precise description of the table contents and show a translation of the switch statement to low-level IR that implements this approach.
 - (b) The solution proposed above has the drawback that the jump table may be too large if the set of case values is sparse. Propose two different approaches that find, in average, the matching case faster than the sequential search, but use data structures that are linear in the number of cases in the switch.
 - (c) Explain what complication do all of the new approaches bring in the process of building the internal representation of the program for optimizations, and propose solutions to address this problem.
 - (d) Explain why are switch constructs are less frequent in object-oriented languages than in non-object oriented languages.
2. The compiler for an object-oriented language has generated the following x86 code for a method:

```
_foo:
  push %ebp
  mov %esp, %ebp
  add $-4, %esp
  mov 12(%ebp), %eax
  add 16(%ebp), %eax
  mov %eax, -4(%ebp)
  cmp $2, -4(%ebp)
  jle L2
  mov -4(%ebp), %eax
  push %edx
  mov 8(%ebp), %edx
  sub 20(%ebp), %eax
  mov %eax, 8(%edx)
  pop %edx
  jmp L3
L2:  mov 8(%ebp), %ebx
     mov -4(%ebp), %eax
     add 20(%ebp), %eax
     mov %eax, 8(%ebx)
L3:  mov 8(%ebp), %eax
     mov %ebp, %esp
     pop %ebp
     ret
```

Assume that the language supports both static and virtual methods. Also assume that the stack grows downward.

- (a) Show the layout for all of the pieces of memory that the execution of this method accesses. Leave blank entries for the pieces that cannot be inferred from this code alone.
- (b) Show a possible input program that this code may have been generated from.
- (c) Is it possible to identify whether this method is static or virtual by inspecting its generated code? Explain.
- (d) Can the instruction “add \$-4, %esp” be optimized away in this example? Precisely in what situations is it safe to discard this instruction?

3. Consider the following function which implements the insertion sort algorithm.

```
void sort(int[] v, int n) {
    int i = 1;
    while (i < n) {
        int k = v[i];
        int j = i-1;
        while(j >= 0 && v[j] > k) {
            v[j+1] = v[j];
            j = j-1;
        }
        v[j+1] = k;
        i = i+1;
    }
}
```

In this program, the test condition in the inner while loop uses a short-circuit “and” operation `&&`. At the end of the function, no variable is live.

- (a) Write the three-address code (low IR) for this program. In the generated code, array indices must represent byte offsets (not element offsets). This means that you have to translate statements such as `k = v[i]` into sequences `t = i*4; k = v[t]`. Also, when short-circuit boolean expressions occur in the conditions of while loops, your code must efficiently combine the control-flow in these two constructs as discussed in class.
 - (b) Construct the control flow graph from the low IR code.
 - (c) Show the dominator tree, the back edges, and the natural loops for the program in part (b).
 - (d) Optimize the program. Perform common subexpression elimination, dead code elimination, strength reduction, and elimination of induction variables. Indicate the changes in the code for each optimization and show the final, optimized program.
4. We want to design a dataflow analysis which compute ranges for integer variables in the program. For this, we extend the set \mathbb{N} of integer numbers with plus and minus infinity: $\mathbb{N}^* = \mathbb{N} \cup \{+\infty, -\infty\}$, such that $-\infty < n$, and $n < +\infty$ for any integer number n . We then use a lattice over the set $L = \{[l, u] \mid l, u \in \mathbb{N}^* \wedge l \leq u\} \cup \{\top\}$.
- (a) Explain what does the element \top represent and why we need it. Define the partial order and the meet operator for elements in this lattice (including \top).
 - (b) Using this lattice to compute ranges of variables will fail. Explain why.
 - (c) To solve the problems from part (b), we define a lattice $L' = \{[l, u] \mid l, u \in \{-\infty, -1, 0, 1, +\infty\} \wedge l \leq u\} \cup \{\top\}$ (with the same partial order as before) and build a dataflow analysis that computes ranges in L' . Show the transfer functions for assignments of constants `x = n` and arithmetic operations `x = y + z` and `x = y * z`, where `x`, `y`, and `z` are program variables and `n` is an integer constant.
 - (d) Assuming programs that consist only of the three kinds of statements shown above, does this analysis from part (c) always yield the same result as the Meet-Over-Paths solution? If yes, show why. If not, show a counter-example program and indicate the MOP and dataflow solutions.