

CS 381 Assignment 1 due Friday, Sept. 1, 2006

1. a) Prove that  $\{0,1\}^*$  is countably infinite.  
b) Prove that the set of all subsets of  $\{0,1\}^*$  is not countably infinite.  
c) Can we assign a unique name to each subset of  $\{0,1\}^*$ ? Explain your answer.
  
2. a) List the three shortest strings in  $\{0^n 10^{2^n} 1 \mid n \geq 1\}$ .  
b) Describe the set of strings denoted by  $\{0^n 10^{2^n} 1 \mid n \geq 1\}^*$ . How many strings are there of length less than or equal to 15?
  
3. 2.2.4
  
4. 2.2.5a and d