gamedesigninitiative at cornell university

Lecture 17

Physics in Games

The Pedagogical Problem

- Physics simulation is a very complex topic
 - No way I can address this in a few lectures
 - Could spend an entire course talking about it
 - CS 5643: Physically Based Animation
- This is why we have physics engines
 - Libraries that handle most of the dirty work
 - But you have to understand how they work
 - Examples: Box2D, Bullet, PhysX



Approaching the Problem

- Want to start with the problem description
 - Squirrel Eiserloh's Problem Overview slides
 - http://www.essentialmath.com/tutorial.htm
- Will help you understand the Engine APIs
 - Understand the limitations of physics engines
 - Learn where to go for other solutions
- Will cover box2d API next time in depth



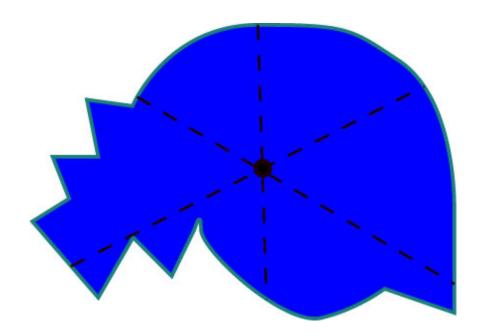
Physics in Games

- Moving objects about the screen
 - Kinematics: Motion ignoring external forces (Only consider position, velocity, acceleration)
 - Dynamics: The effect of forces on the screen
- Collisions between objects
 - Collision Detection: Did a collision occur?
 - Collision Resolution: What do we do?



Motion: Modeling Objects

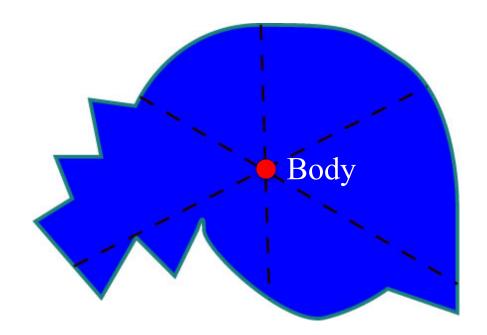
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 - Don't worry about shape
 - Only needed for collisions
- Every object is a point
 - *Centroid*: average of points
 - Also called: *center of mass*
 - Same if density uniform
- Use rigid body if needed
 - Multiple points together
 - Moving one moves them all





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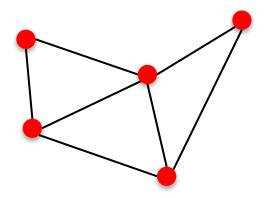




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Rigid Body





- Physics is time-stepped
 - Assume velocity is constant (or the acceleration is)
 - Compute the position
 - Move for next frame



- Movement is very linear
 - Piecewise approximations
 - Remember your calculus
- Smooth = smaller steps
 - More frames a second?



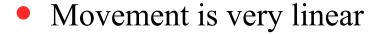
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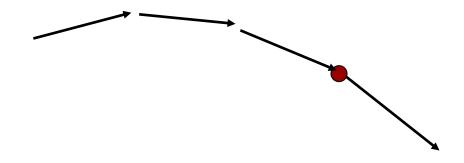
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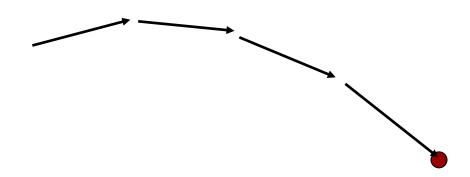


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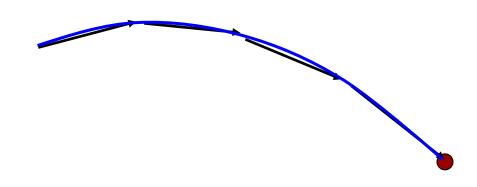


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Kinematics

- Goal: determine an object position p at time t
 - Typically know it from a previous time
- **Assume**: constant velocity *v*
 - $p(t+\Delta t) = p(t) + v\Delta t$
 - Or $\Delta p = p(t + \Delta t) p(t) = v \Delta t$
- Alternatively: constant acceleration a
 - $v(t+\Delta t) = v(t) + a\Delta t$ (or $\Delta v = a\Delta t$)
 - $p(t+\Delta t) = p(t) + v(t)\Delta t + \frac{1}{2}a(\Delta t)^2$
 - Or $\Delta p = v_0 \Delta t + \frac{1}{2} a(\Delta t)^2$

Formulas commonly in use



Kinematics

- Goal: determine an object position p at time t
 - Typically know it from a previous time
- **Assume**: constant velocity v
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 - High School Physics w/o Calculus
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Formulas commonly in use



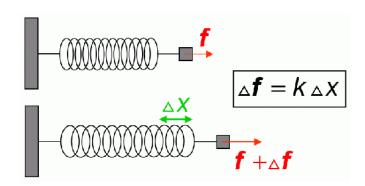
Linear Dynamics

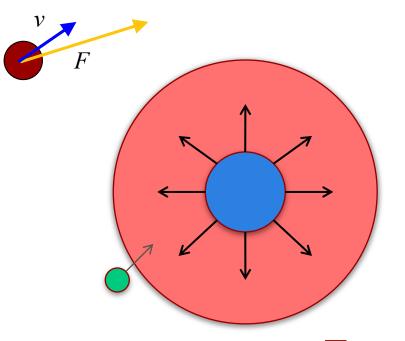
- Forces affect movement
 - Springs, joints, connections
 - Gravity, repulsion
- Get velocity from forces
 - Compute current force *F*
 - F constant entire frame
 - Formulas:

$$\Delta a = F/m$$

$$\Delta v = F\Delta t/m$$

$$\Delta p = F(\Delta t)^2/m$$

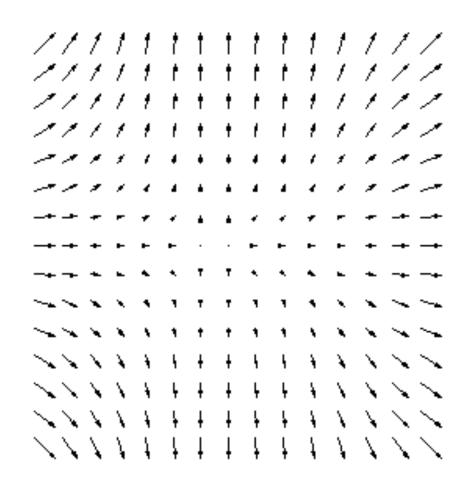






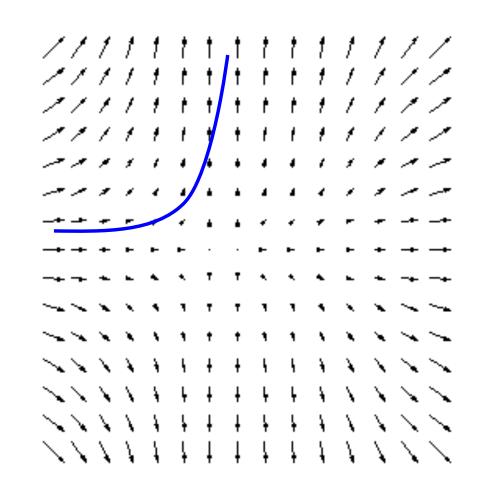
Linear Dynamics

- Force: F(p,t)
 - p: current position
 - t: current time
- Creates a vector field
 - Movement should follow field direction
- Update formulas
 - $a_i = F(p_i, i\Delta t)/m$
 - $v_{i+1} = v_i + a_i \Delta t$
 - $\bullet \quad p_{i+1} = p_i + v_i \Delta t$



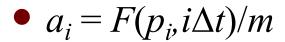
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- Differential Equation
 - \bullet $F(p,t) = m \ a(t)$
 - $F(p,t) = m \underline{p}''(t)$
- Euler's method:



•
$$v_{i+1} = v_i + a_i \Delta t$$

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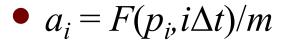


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- But heavily optimized



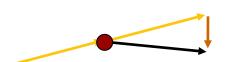
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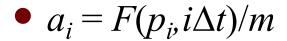


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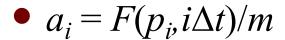


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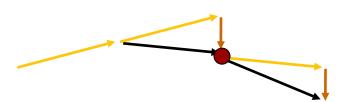


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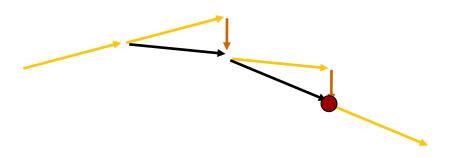


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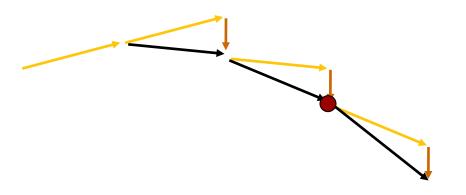
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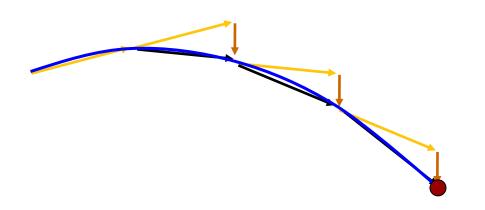
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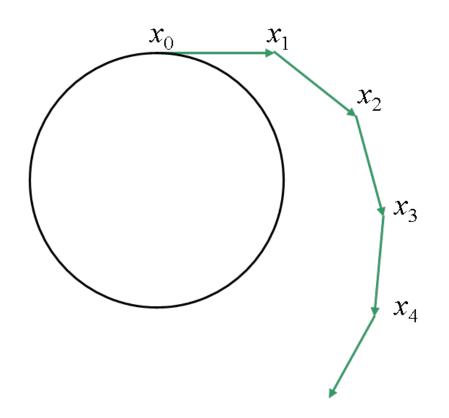
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Problem with DE Solvers

Errors accumulate

- Side effect of techniques
- Stepwise approximations
- Major problem with orbits
 - Move along tangent vector
 - Vector takes out of orbit
 - Gets worse over time
- Must constrain behavior
 - Keep movement in orbit





Dealing with Error Creep

- Classic solution: reduce the time step Δt
 - Up the frame rate (not necessarily good)
 - Perform more than one step per frame
 - Each Euler step is called an *iteration*
- Multiple iterations per frame
 - Let *h* be the length of the frame
 - Let *n* be the number of iterations

$$\Delta t = h/n$$

Typically a parameter in your physics engine



Dealing with Error Creep

- Classic solution: reduce the time step Δt
 - Up the frame rate (not necessarily good)
 - Perform more than one step per frame
 - Still does not solve orbit problem • Each Euler ata
- - Let ... the length of the frame
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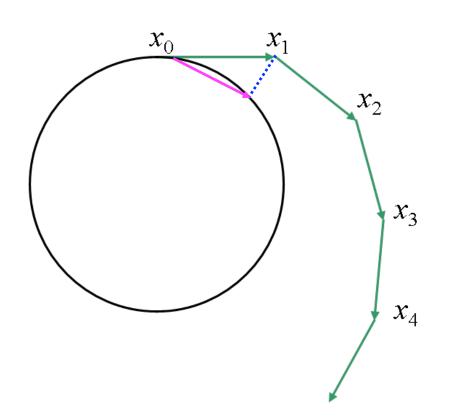
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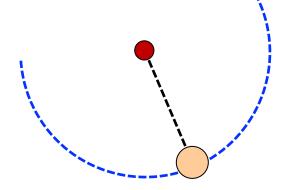




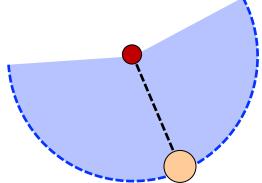
Constraint Solvers

- Limit object movement
 - Pos must satisfy constraint
 - Correct position if does not
- Example: Distance
 - Hard: Dist must be exact
 - Soft: Dist must be no more
- Other constraints
 - Contact: non-penetration
 - Restitution: bouncing
 - Friction: sliding, sticking





Soft Constraint

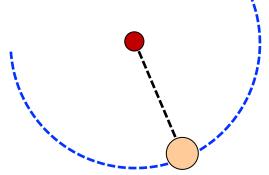




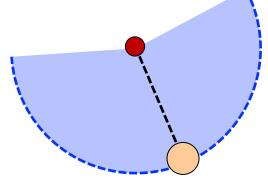
Constraint Solvers

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- Example: Distance
 - Focus of Lab 4
- Other constraints
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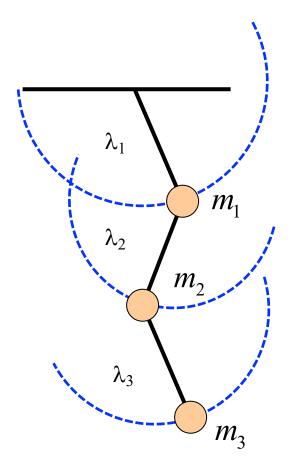






Challenge: Interconnected Constraints

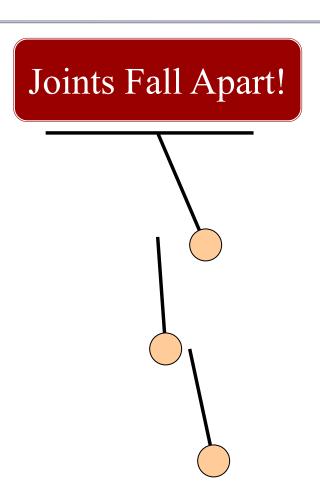
- Not hard if one object
 - Just move it and correct
- How about *relationships*?
 - Correct an object
 - But it constrained another
 - So have to correct it and...
- When does this happen?
 - Ropes, chains
 - Box stacking





Challenge: Interconnected Constraints

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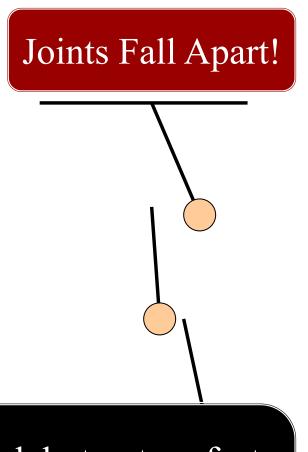




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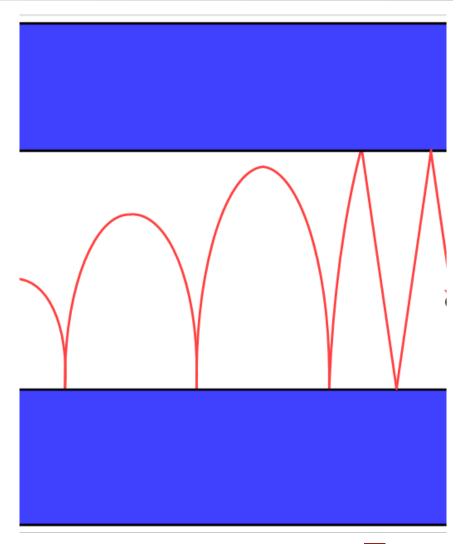
box2d is good, but not perfect





Error Accumulation: Energy

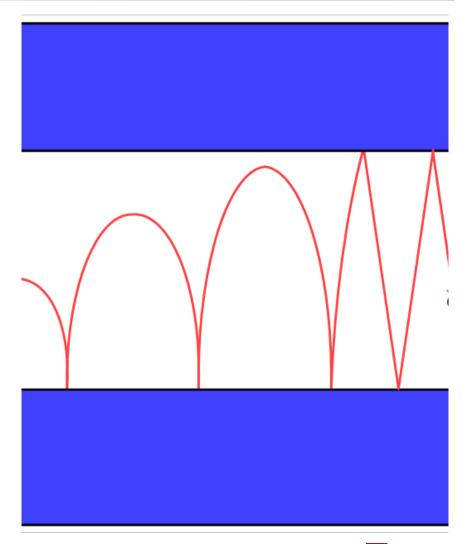
- Want energy conserved
 - Energy loss undesirable
 - Energy gain is evil
 - Simulations explode!
- Not always possible
 - Error accumulation!
- Need *ad hoc* solutions
 - Clamping (max values)
 - Manual dampening





Error Accumulation: Energy

- Want energy conserved
 - Energy loss undesirable
 - Energy gain is evil
 - Simulations explode!
- High Energy is where joints fail
- Need *ad hoc* solutions
 - Clamping (max values)
 - Manual dampening





Kinematics vs. Dynamics

Kinematics

Dynamics

- Advantages
 - Very simple to use
 - Non-calculus physics
- Disadvantages
 - Only simple physics
 - All bodies are rigid
- Old school games

- Advantages
 - Complex physics
 - Non-rigid bodies
- Disadvantages
 - Beyond scope of course
 - Need a physics engine
- Neo-retro games



Physics in Games

- Moving objects about the screen
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Collisions and Geometry

- Collisions need geometry
 - Points are not enough
 - Find where objects meet
- Often use convex shapes
 - Lines always remain inside
 - If not convex, is *concave*
- What if is not convex?
 - Break into components
 - Triangles always convex!



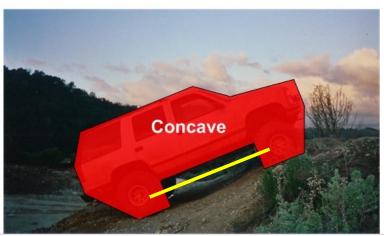




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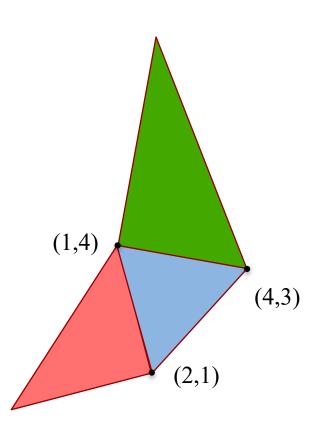






Recall: Triangles in Computer Graphics

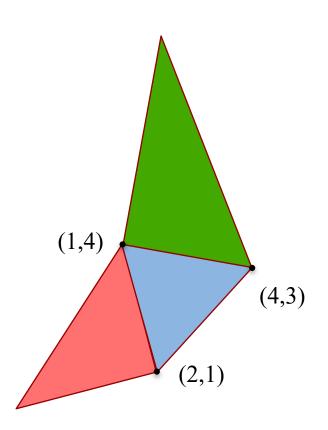
- Everything made of triangles
 - Mathematically "nice"
 - Hardware support (GPUs)
- Specify with three vertices
 - Coordinates of corners
- Composite for complex shapes
 - Array of vertex objects
 - Each 3 vertices = triangle





Recall: Triangles in Computer Graphics

- Everything made of triangles
 - Guaranteed to be convex
 - Hardware support (GPUs)
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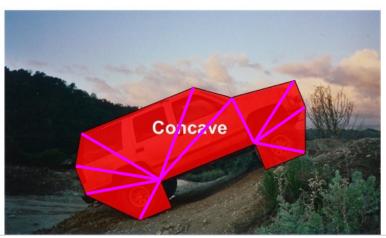




Collisions and Geometry

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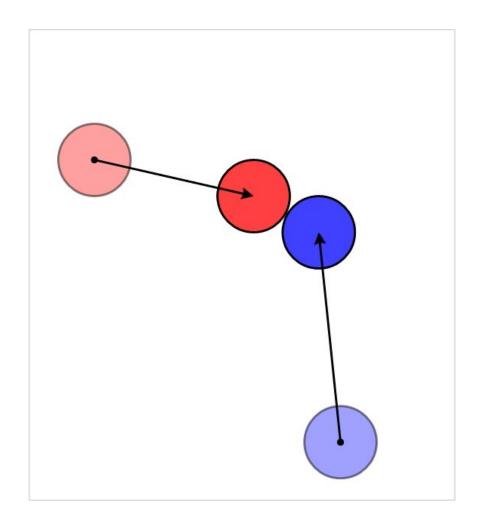
Collision Types

Inelastic Collisions

- No energy preserved
- Stop in place (v = 0)
- "Back-out" so no overlap
- Very easy to implement

Elastic Collisions

- 100% energy preserved
- Think billiard balls
- Classic physics problem

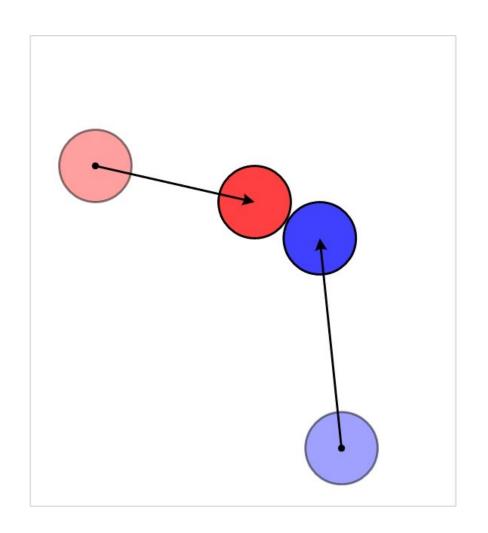




Something In-Between?

Partially Elastic

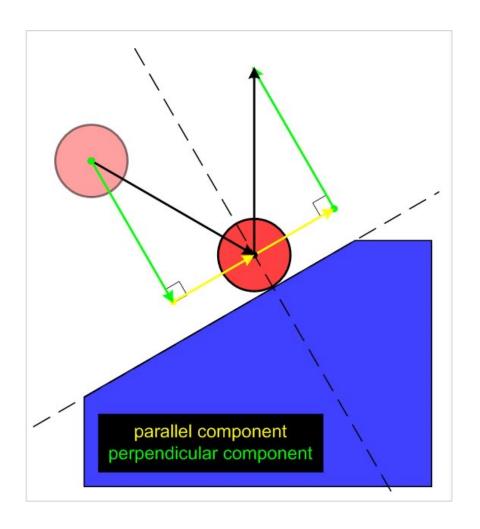
- x% energy preserved
- Different each object
- Like elastic, but harder
- Issue: object "material"
 - What is object made of?
 - **Example**: Rubber? Steel?
- Another parameter!
 - Technical prototype?





Collision Resolution: Circles

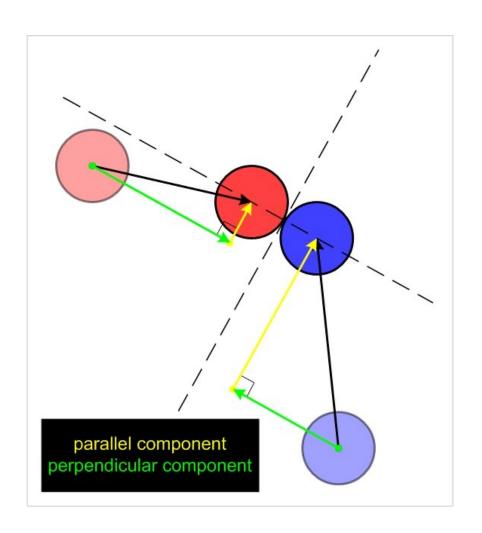
- Single point of contact!
 - Energy transferred at point
 - Not true in complex shapes
- Use relative coordinates
 - Point of contact is origin
 - **Perpendicular component**: Line through origin, center
 - Parallel component:
 Axis of collision "surface"
- Reverse object motion on the perpendicular comp





Collision Resolution: Circles

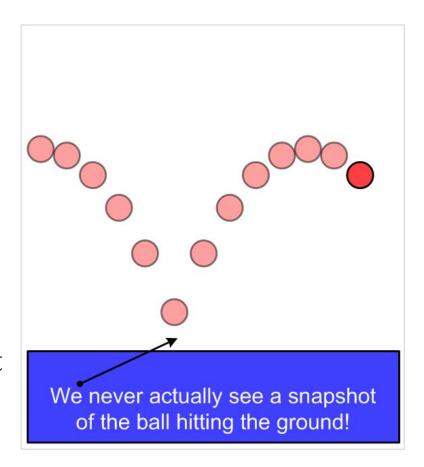
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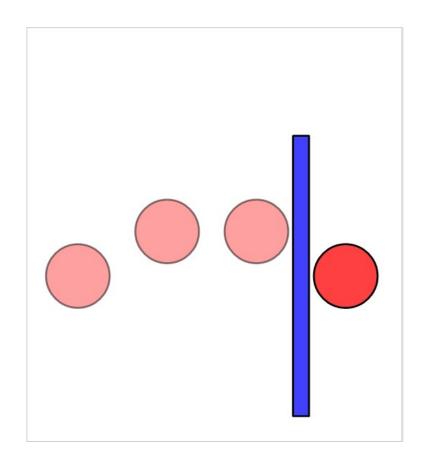
Issues with Collisions: Tunneling

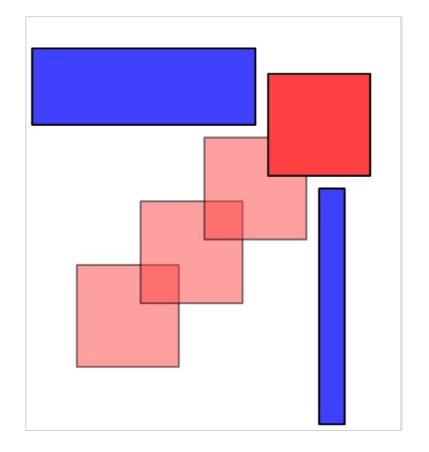
- Games act like flip-books
 - Sequence of snapshots
 - Collisions mid-snapshot?
 - Could *miss* the collision
- Example of false negative
- This is a serious problem
 - Players going where shouldn't
 - Players missing event trigger
 - Cannot ignore tunneling





Tunneling

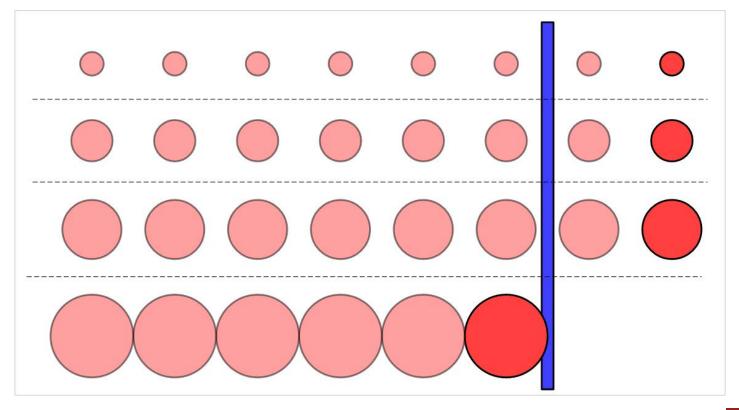






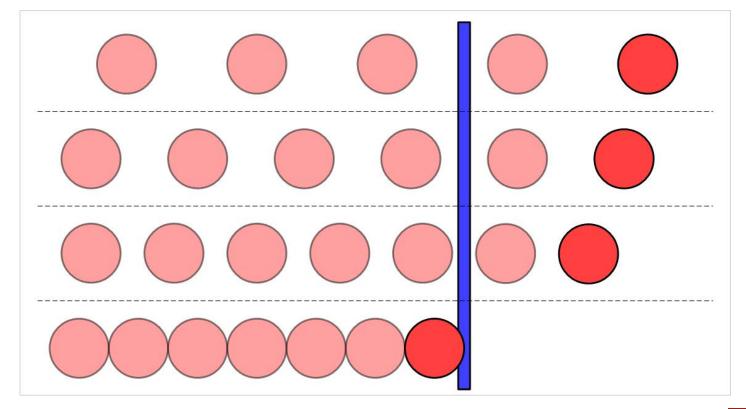
Tunneling: Observations

Small objects tunnel more easily



Tunneling: Observations

- Small objects tunnel more easily
- Fast-moving objects tunnel more easily



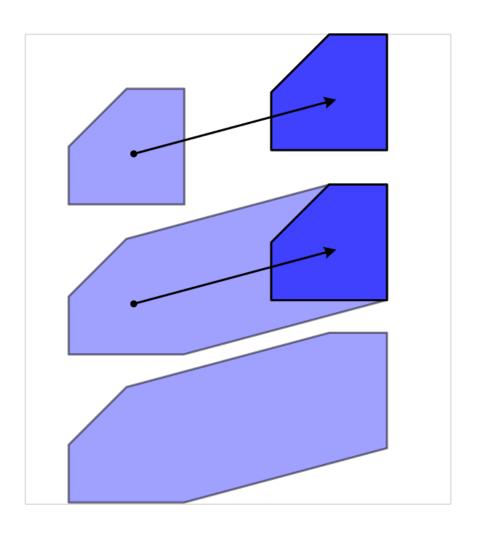
Possible Solutions to Tunnelling

- Minimum size requirement?
 - Fast objects still tunnel
- Maximum speed limit?
 - Speed limit is a function of object size
 - So small & fast objects (bullets) not allowed
- Smaller time step?
 - Essentially the same as a speed limit
- All of these solutions are inadequate



Swept Shapes

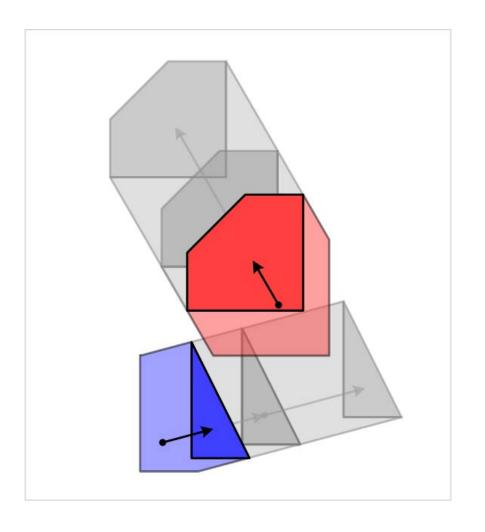
- Bounds contain motion
 - "Cylinder" w/ shape at ends
 - Object always in bounds
 - Convex if shape is convex
- New collision checking
 - Put shapes at start and end
 - Create swept shape for pair
 - Check for collisions
- Can have false positives
 - Swept shape ignores time





Swept Shapes

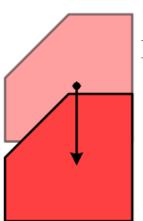
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 - Swept shape ignores time



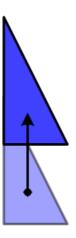


Swept Shapes & Relative Coordinates

- False positives happen if:
 - Two objects are moving
 - Swept shapes intersect at different intersection times
- What if only one moving?
 - Swept intersects stationary
 - So no false positives
- Change reference frames
 - Keep one shape still
 - Move other in new coords



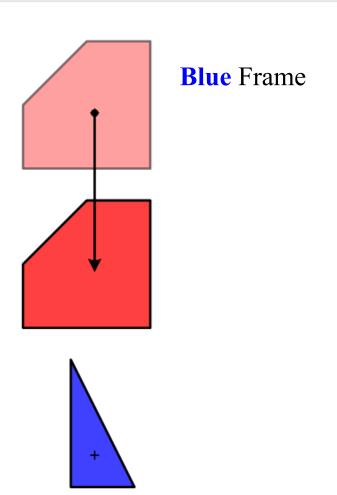
Inertial Frame





Swept Shapes & Relative Coordinates

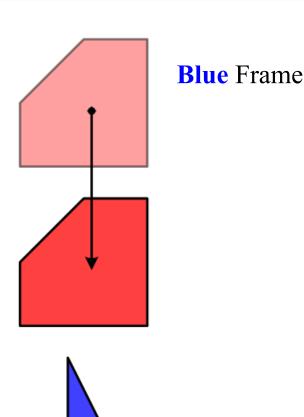
- False positives happen if:
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Swept Shapes & Relative Coordinates

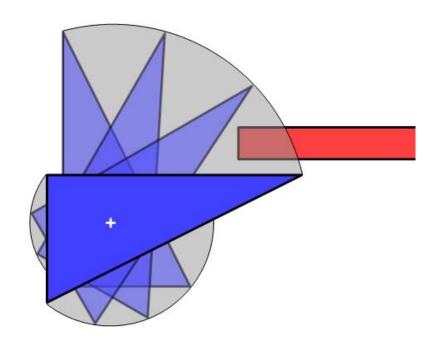
- False positives happen if:
 - Two objects are moving
 - Swept shapes intersect at different intersection times
- What if only one moving?
 - Swept intersects stationary
 - So no false positives
- Change reference frames
 - Expensive!





Rotations Suck

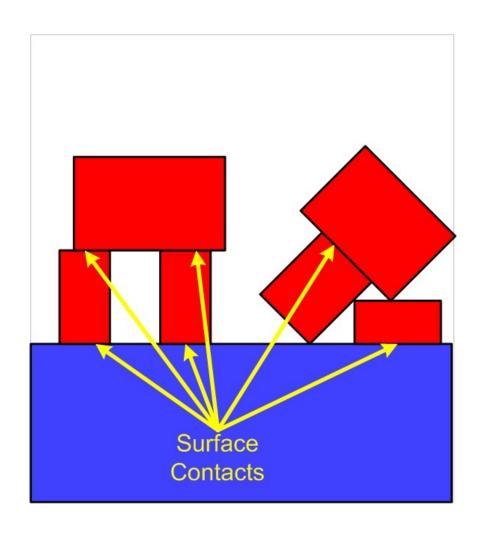
- Relative coordinates no help
 - Cannot use swept shapes
 - Actual solution is hard!
- But not so bad…
 - Angular tunneling looks ok
 - Speed limits are feasible
 - Do linear approximations
- Many physics systems
 never handle this well





More Complex Shapes

- Point of contact harder
 - Could just be a point
 - Or it could be an edge
- Model w/ rigid bodies
 - Break object into points
 - Connect with constraints
 - Force at point of contact
 - Transfers to other points
- Needs constraint solver





Summary

- Object representation depends on goals
 - For motion, represent object as a single point
 - For collision, objects must have geometry
- Dynamics is use of forces to move objects
 - Solve differential equations for position
 - Need constraint solvers to overcome error creep
- Collisions are broken up into two steps
 - Collision detection checks for intersections
 - Collision resolution is hard if not a circle

