# the gamedesigninitiative at cornell university 

## Lecture 13

## Sprite Graphics

## Graphics Lectures

- Drawing Images
- SpriteBatch interface
- Coordinates and Transforms
- Drawing Perspective
- Camera
- Projections
- Drawing Primitives
- Color and Textures
- Polygons


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## Graphics Lectures

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Animation is part of AI Lectures

- Drawing Primitives
- Color and Textures
- Polygons


## Graphics Lectures

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## Take Away for Today

- Coordinate Spaces and drawing
- What is screen space? Object space?
- How do we use the two to draw objects?
- Do we need any other spaces as well?
- Drawing Transforms
- What is a drawing transform?
- Describe the classic types of transforms.
- List how to use transforms in a game.


## The SpriteBatch Interface

- In this class we restrict you to 2D graphics
- 3D graphics are much more complicated
- Covered in much more detail in other classes
- Art 1701: Artist tools for 3D Models
- CS 5625: Programming with 3D models
- In LibGDX, use the class SpriteBatch
- Sprite: Pre-rendered 2D (or even 3D) image
- All you do is composite the sprites together


## Drawing in 2 Dimensions

- Use coordinate systems
- Each pixel has a coordinate
- Draw something at a pixel by
- Specifying what to draw
- Specifying where to draw
- Do we draw each pixel?

- What LibGDX gives us


## Sprite Coordinate Systems

- Screen coordinates: where to paint the image
- Think screen pixels as a coordinate system
- Very important for object transformations
- Example: scale, rotate, translate
- In 2D, LibGDX origin is bottom left of screen
- Object coordinate: location of pixels in object
- Think of sprite as an image file (it often is)
- Coordinates are location of pixels in this file
- Unchanged when object moves about screen


## Sprite Coordinate Systems



## Historical Coordinate Systems



## Historical Coordinate Systems



## Drawing Sprites

## - Basic instructions:

- Set origin for the image in object coordinates
- Give the SpriteBatch a point to draw at
- Screen places origin of image at that point
- What about the other pixels?
- Depends on transformations (rotated? scaled?)
- But these (almost) never affect the origin
- Sometimes we can reset the object origin


## Sprite Coordinate Systems



## Sprite Coordinate Systems



## Sprite Coordinate Systems



## Sprite Coordinate Systems



## Drawing with SpriteBatch

## public void draw(float dt) \{

## spriteBatch.begin();

 spriteBatch.draw(image0); spriteBatch.draw(imagel, $\underbrace{\text { pos.x, pos.y) }}$; spriteBatch.end();screen
coordinates

## 2D Transforms

- A function $T: \mathbb{R}^{2} \rightarrow \mathbb{R}^{2}$
- "Moves" one set of points to another set of points
- Transforms one "coordinate system" to another
- The new coordinate system is the distortion
- Idea: Draw on paper and then "distort" it
- Examples: Stretching, rotating, reflecting
- Determines placement of "other" pixels
- Also allows us to get multiple images for free


## The "Drawing Transform"

- $T$ : object coords $\rightarrow$ screen coords
- Assume pixel $(a, b)$ in art file is blue
- Then screen pixel $T(a, b)$ is blue
- We call $T$ the object map
- By default, object space = screen space
- Color of image at $(a, b)=$ color of screen at $(a, b)$
- By drawing an image, you are transforming it
- S an image; transformed image is $T(\mathbf{S})$


## Example: Translation

- Simplest transformation: $T(\mathbf{v})=\mathbf{v}+\mathbf{u}$
- Shifts object in direction u
- Distance shifted is magnitude of $\mathbf{u}$
- Used to place objects on screen
- By default, object origin is screen origin
- $T(\mathbf{v})=\mathbf{v}+\mathbf{u}$ places object origin at $\mathbf{u}$




## Aside: Matching Your Translation

- Movement is two things
- Animation of the filmstrip
- Translation of the image
- These two must align
- Example: Walking
- Foot is point of contact
- "Stays in place" as move
- This constrains translation

- Make movement regular
- Measure distance per frame
- Keep same across frames


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## Composing Transforms

- Example: $T: \mathbb{R}^{2} \rightarrow \mathbb{R}^{2}, S: \mathbb{R}^{2} \rightarrow \mathbb{R}^{2}$
- Assume pixel $(a, b)$ in art file is blue
- Transform $T$ makes pixel $T(a, b)$ blue
- Transform $S \circ T$ makes pixel $S(T(a, b))$ blue
- Strategy: use transforms as building blocks
- Think about what you want to do visually
- Break it into a sequence of transforms
- Compose the transforms together


## Application: Scrolling



## Application: Scrolling



## Application: Scrolling



## Scrolling: Two Translations

- Place object in the World at point $\mathbf{p}=(x, y)$
- Basic drawing transform is $T(\mathbf{v})=\mathbf{v}+\mathbf{p}$
- Suppose Screen origin is at $\mathbf{q}=\left(x^{\prime}, y^{\prime}\right)$
- Then object is on the Screen at point $\mathbf{p - q}$
- $S(\mathbf{v})=\mathbf{v}-\mathbf{q}$ transforms World coords to Screen
- $S \circ T(\mathbf{v})$ transforms the Object to the Screen
- This separation makes scrolling easy
- To move the object, change $T$ but leave $S$ same
- To scroll the screen, change $S$ but leave $T$ same


## Scrolling: Practical Concerns

- Many objects will exists outside screen
- Can draw if want; graphics card will drop them
- It is expensive to keep track of them all
- But is also unrealistic to always ignore them
- In graphics, drawing transform = matrix
- Hence composition = matrix multiplication
- Details beyond the scope of this course
- LibGDX handles all of this for you (sort of)


## Using Transforms in LibGDX

- LibGDX has methods for creating transforms
- Two types depending on application
- AffineZ for transforming 2D sprites
- Matrix4 for transforming 3D object
- But also for transforming fonts
- Parameters fill in details about transform
- Example: Position $(x, y)$ if a translation
- The most math you will ever need for this


## Transforms in SpriteBatch

## Affine2

## Matrix4

- Pass it to a draw command
- Applies only to that image
- Adds to CPU power
- Handles everything
- Location is in transform
- Transform to object position
- sb.draw(image,wd,ht,affine);
- Pass to setTransformMatrix
- Applies to all images!
- Handled by the GPU but...
- Change causes GPU stall
- Only use this if you must
- e.g. Transforming fonts
- See GameCanvas in Lab1


## Transforms in SpriteBatch

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Only supports a TextureRegion??

- Pass to setTransformMatrix
- Applies to all images!
- Handled by the GPU but...
- Change causes GPU stall
- Only use this if you must
- e.g. Transforming fonts
- See GameCanvas in Lab1


## Positioning in LibGDX

public void draw(float dt) \{

Vector2 pos = object.getPosition();
spriteBatch.begin(); spriteBatch.draw(image,pos.x,pos.y); spriteBatch.end();

## Positioning in LibGDX



## Positioning in LibGDX

```
public void draw(float dt) {
    Affine% oTran = new Affine2();
    oTran.setToTranslation(object.getPosition());
    Affine2 wtran = new Affine2();
    Vector2 wPos = viewWindow.getPosition();
    wTran.setToTranslation(-wPos.X.-wPos.y);
```



```
wTran.setToTranslation(-wPos.x.-wPos.y);
oTran.mul(wTran);
spriteBatch.begin(); spriteBatch.draw(image,width,height,oTran); spriteBatch.end();

\section*{Transform Gallery}
- Uniform Scale: \(\left[\begin{array}{ll}s & 0 \\ 0 & s\end{array}\right]\left[\begin{array}{l}x \\ y\end{array}\right]=\left[\begin{array}{l}s x \\ s y\end{array}\right]\)
\[
\left[\begin{array}{cc}
1.5 & 0 \\
0 & 1.5
\end{array}\right]
\]


\section*{Transform Gallery}
- Uniform Scale: \(\left[\begin{array}{ll}s & 0 \\ 0 & s\end{array}\right]\left[\begin{array}{l}x \\ y\end{array}\right]=\left[\begin{array}{l}s x \\ s y\end{array}\right]\)
\(\left.\begin{array}{c}\text { Represent as } \\ 2 \times 2 \text { matrix }\end{array}\right]\left[\begin{array}{cc}1.5 & 0 \\ 0 & 1.5\end{array}\right]\)


\section*{Matrix Transform Gallery}
\(\begin{aligned} \text { - Nonuniform Scale: } & {\left[\begin{array}{cc}s_{x} & 0 \\ 0 & s_{y}\end{array}\right]\left[\begin{array}{l}x \\ y\end{array}\right]=\left[\begin{array}{l}s_{x} x \\ s_{y} y\end{array}\right] } \\ & {\left[\begin{array}{cc}1.5 & 0 \\ 0 & 0.8\end{array}\right] }\end{aligned}\)



\section*{Matrix Transform Gallery}
- Rotation:
\[
\begin{aligned}
& {\left[\begin{array}{cc}
\cos \theta & -\sin \theta \\
\sin \theta & \cos \theta
\end{array}\right]\left[\begin{array}{l}
x \\
y
\end{array}\right]=\left[\begin{array}{l}
x \cos \theta-y \sin \theta \\
x \sin \theta+y \cos \theta
\end{array}\right]} \\
& {\left[\begin{array}{cc}
0.866 & -0.5 \\
0.5 & 0.866
\end{array}\right]}
\end{aligned}
\]

affine.setToRotationRad(angle);

\section*{Matrix Transform Gallery}
- Reflection: \(\left[\begin{array}{cc}-1 & 0 \\ 0 & 1\end{array}\right]\left[\begin{array}{l}x \\ y\end{array}\right]=\left[\begin{array}{c}-x \\ y\end{array}\right]\)
- View as special case of Scale \(\left[\begin{array}{cc}-1 & 0 \\ 0 & 1\end{array}\right]\)



\section*{Matrix Transform Gallery}
- Shear: \(\left[\begin{array}{ll}1 & a \\ 0 & 1\end{array}\right]\left[\begin{array}{l}x \\ y\end{array}\right]=\left[\begin{array}{c}x+a y \\ y\end{array}\right]\)
\[
\left[\begin{array}{cc}
1 & 0.5 \\
0 & 1
\end{array}\right]
\]


affine.setToShearing(a,1);

\section*{Translation Revisited}
- Translation is not a linear transform
- To be linear, \(\mathrm{T}(\mathbf{v}+\mathbf{w})=\mathrm{T}(\mathbf{v})+\mathrm{T}(\mathbf{w})\)
- Translation transform is \(T(\mathbf{v})=\mathbf{v}+\mathbf{u}\)
- \(\mathrm{T}(\mathbf{v})+\mathrm{T}(\mathbf{w})=(\mathbf{v}+\mathbf{u})+(\mathbf{w}+\mathbf{u})=\mathbf{v}+\mathbf{w}+2 \mathbf{u} \neq \mathrm{T}(\mathbf{v}+\mathbf{w})\)
- But LibGDX treats it like one
- Affine2 transforms support translation
- Matrix4 supports matrix.set(affine)
- What is going on here?

\section*{Homogenous Coordinates}
- Add an extra dimension to the calculation.
- An extra component \(w\) for vectors
- For affine transformations, can keep \(w=1\)
- Add extra row, column to matrices (so \(3 \times 3\) )
- Dimension is for calculation only
- We are not in 3D-space yet
- 3D transforms need 4D vectors, \(4 \times 4\) matrices
- Matrix4 because LibGDX supports 3D

\section*{Homogenous Coordinates}
- Linear transforms have dummy row and column
\[
\left[\begin{array}{ccc}
a & b & 0 \\
c & d & 0 \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{l}
x \\
y \\
1
\end{array}\right]=\left[\begin{array}{c}
a x+b y \\
c x+d y \\
1
\end{array}\right]
\]
- Translation uses extra column
\[
\left[\begin{array}{lll}
1 & 0 & t \\
0 & 1 & s \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{l}
x \\
y \\
1
\end{array}\right]=\left[\begin{array}{c}
x+t \\
y+s \\
1
\end{array}\right]
\]

\section*{Affine Transforms Revisited}
- Affine: Linear on homogenous coords
- Equal to all transforms \(T(\mathbf{v})=\mathrm{Mv}+\mathbf{p}\)
- Treat everything as matrix multiplication
- Why does this work?
- Area of mathematics called projective geometry
- Far beyond the scope of this class
- LibGDX hides all the messy details
- Just stick with AffineZ class for now

\section*{Affine Transform Gallery}
- Translation:
\[
\left[\begin{array}{ccc}
{\left[\begin{array}{ccc}
1 & 0 & t_{x} \\
0 & 1 & t_{y} \\
0 & 0 & 1
\end{array}\right]} \\
\hline & \\
\hline
\end{array}\right.
\]

\section*{Affine Transform Gallery}
- Uniform Scale:


2D Sprite Graphics

\section*{Affine Transform Gallery}
- Nonuniform Scale:
\[
\left[\begin{array}{ccc}
s_{x} & 0 & 0 \\
0 & s_{y} & 0 \\
0 & 0 & 1
\end{array}\right]
\]

\section*{Affine Transform Gallery}
- Rotation:
\[
\left[\begin{array}{ccc}
\cos \theta & -\sin \theta & 0 \\
\sin \theta & \cos \theta & 0 \\
0 & 0 & 1
\end{array}\right]\left[\begin{array}{ccc}
0.866 & -0.5 & 0 \\
0.5 & 0.866 & 0 \\
0 & 0 & 1
\end{array}\right]
\]

\section*{Affine Transform Gallery}
- Reflection:
- Special case of Scale
\[
\left[\begin{array}{ccc}
-1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right]
\]



\section*{Affine Transform Gallery}
- Shear:


\section*{Compositing Transforms}
- In general not commutative: order matters!

rotate, then translate

translate, then rotate

\section*{Compositing Transforms}
- In general not commutative: order matters!

scale, then rotate

rotate, then scale

\section*{Rotating Object About Center}


\section*{Rotating Object About Center}


\section*{Rotating Object About Center}


\section*{Rotating Object About Center}


\section*{Rotating Object About Center}


\section*{A Word About Scaling}
- If making smaller, it drops out pixels
- Suppose \(T(\mathbf{v})=0.5 \mathbf{v}\)
- \((0,0)=T(0,0)\); pixel \((0,0)\) colored from \((0,0)\) in file
- \((0,1)=T(0,2)\); pixel \((0,1)\) colored from \((0,2)\) in file
- But if making larger, it duplicates pixels
- Suppose \(T(\mathbf{v})=2 \mathbf{v}\)
- \((0,1)=T(0,0.5)\); pixel \((0,1)\) colored from \((0,1)\) in file
- \((0,1)=T(0,1)\); pixel \((0,2)\) colored from \((0,1)\) in file
- This can lead to jaggies

\section*{Scaling and Jaggies}
- Jaggies: Image is blocky
- Possible to smooth image
- Done through blurring

- In addition to transform
- Some graphic card support
- Solution for games
- Shrinking is okay
- Enlarging not (always) okay
- Make sprite large as needed

\section*{Summary}
- Drawing is all about coordinate systems
- Object coords: Coordinates of pixels in image file
- Screen coords: Coordinates of screen pixels
- Transforms alter coordinate systems
- "Multiply" image by matrix to distort them
- Multiply transforms together to combine them
- Matrices are not commutative
- Later transforms go on "the right"```

