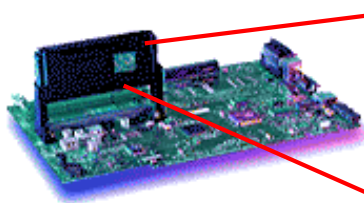


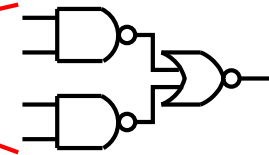
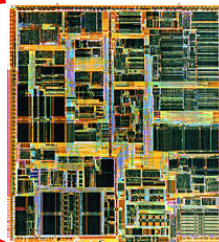
# What 314 Is About

---

System  
Architecture



Processor  
Design



Logic Design

```
jal _getnext  
ori $a0,$0,0  
lw $t0,8($v0)  
lw $t0,12($t0)  
beq $t0,0,0x401834  
li $t1,4  
beq $t0,$t1,0x4018a0
```

Assembly  
Language

```
0x0c004841  
0x00000000  
0x34040000  
0x8c480008  
0x00000000  
0x8d08000c  
0x10001834  
0x00000000  
0x24090004  
0x11090002  
...
```

Machine  
Instructions



# Building A Computer

---

Information is encoded with bits: 0's and 1's.  
(we've already seen 2's complement numbers)

These are encoded using *voltages*...

- + well understood
- + easy to generate, detect
- affected by environment

But why 1's and 0's only?



# Digital Representation

---

Example: representing a B&W picture:

- Black = 0 V
- White = 1 V
- 80% grey = 0.8 V
- ...

Represent by scanning picture in fixed order.

Let's try doing some computation with the voltages...

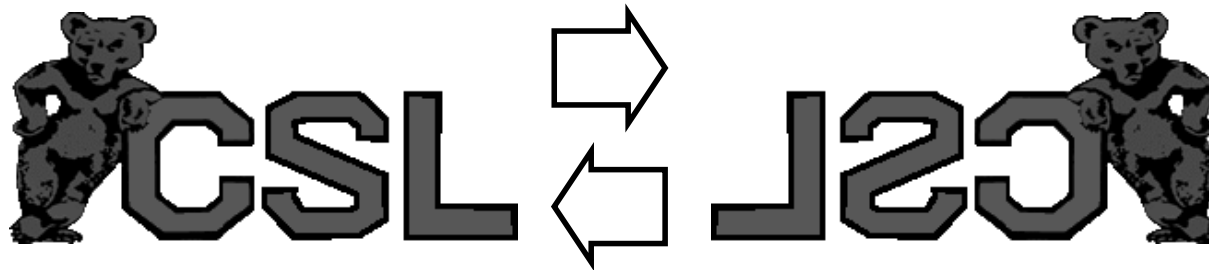


# Digital Representation

---

Flip image:

Flip back and forth...



What really happens...



Have to build system to tolerate some error (noise).



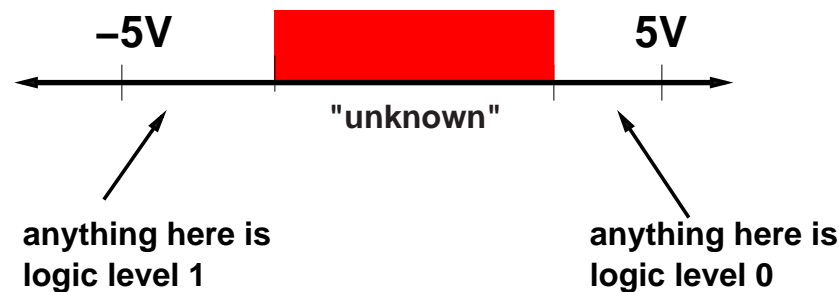
# Logic Levels

---

- Store just one bit on a wire...
- Gain reliability



Different conventions are possible



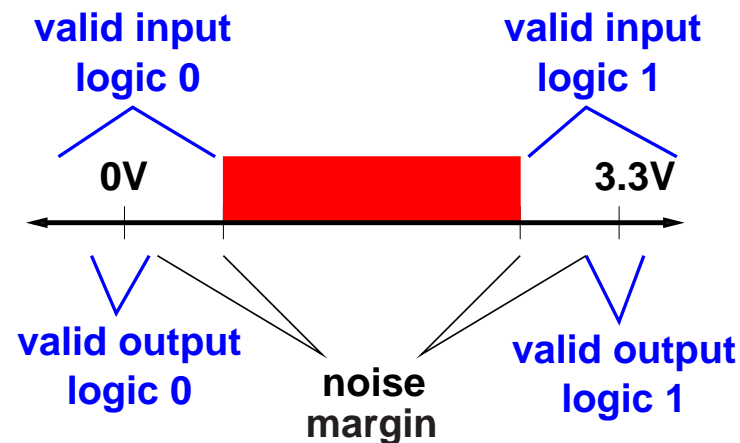
# Combinational Devices

---

A **combinational device**:

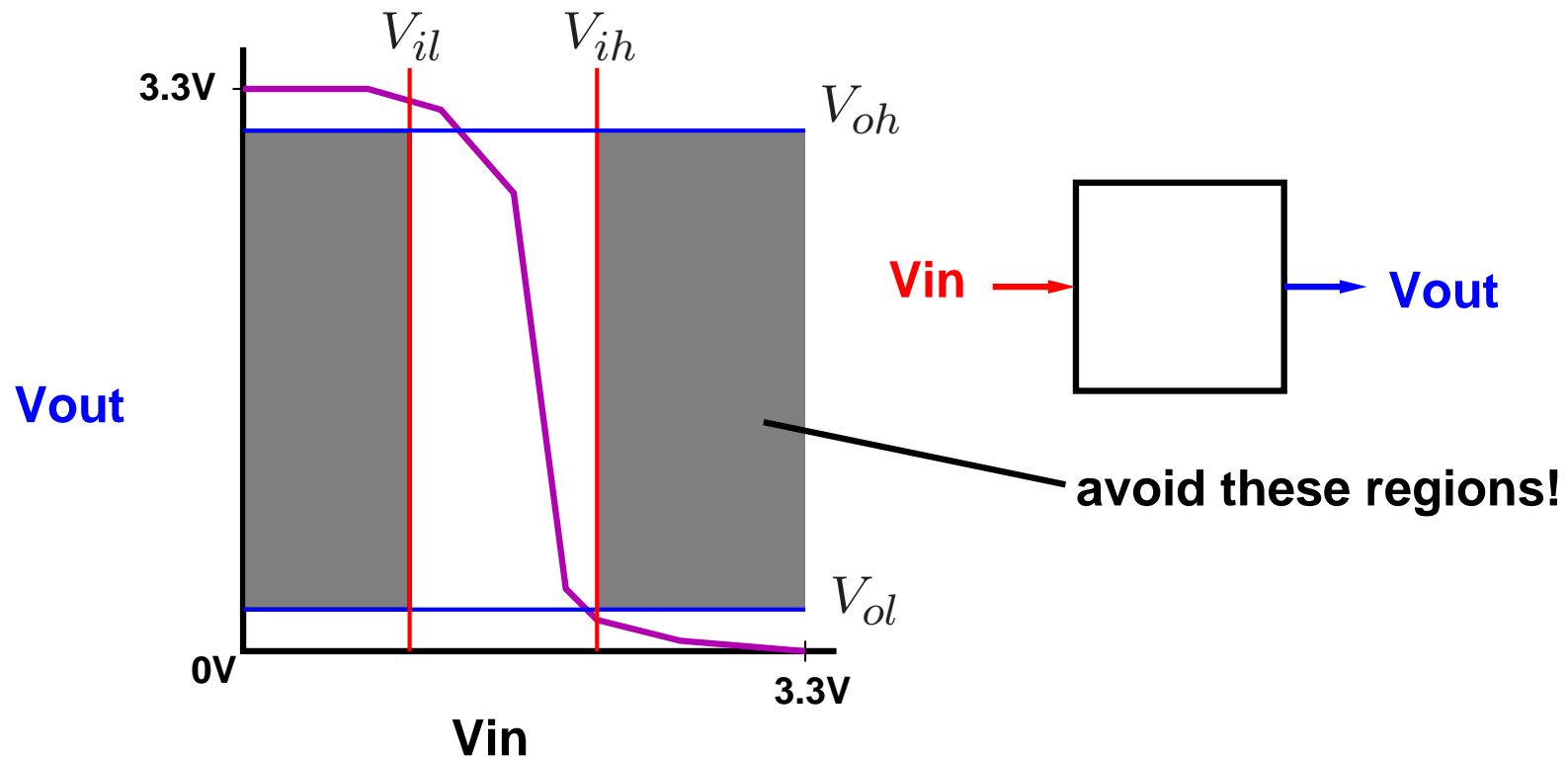
- Output is a function of inputs only ("memoryless")
- Takes input to valid, stable outputs

Combinational devices **restore** marginally valid signals!



# Example

- Input: logic 0 if  $< V_{il}$ , logic 1 if  $> V_{ih}$
- Output logic 0 if  $< V_{ol}$ , logic 1 if  $> V_{oh}$



# Digital View

---

- If input is 0, output is 1
- If input is 1, output is 0

Normally written in a table, like this:

In	Out
0	1
1	0

Called a "truth-table".





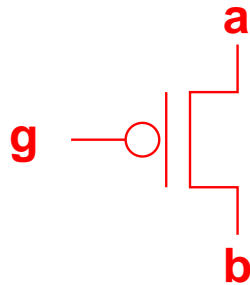
# Implementation: Switching Networks

---

Lots of ways to build switches...

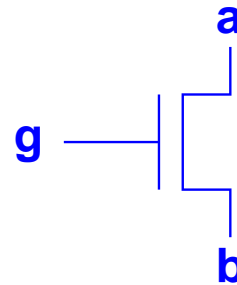
- relays
- vacuum tubes
- transistors
- ...

**P-transistor**



**Connect a and b  
if  $g = 0$ .**

**N-transistor**

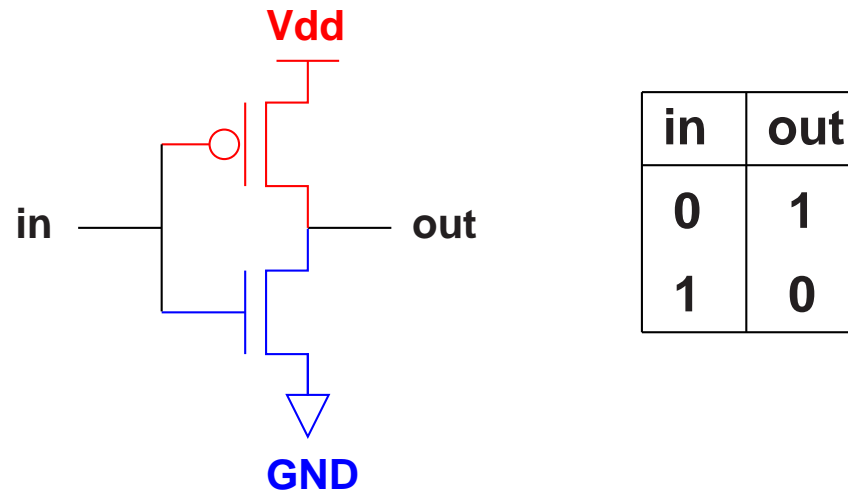


**Connect a and b  
if  $g = 1$ .**

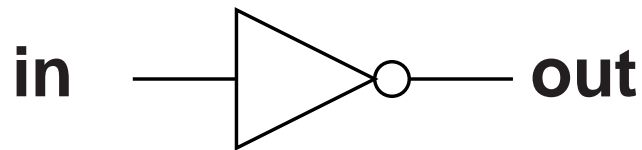


# Switching Networks: Inverter

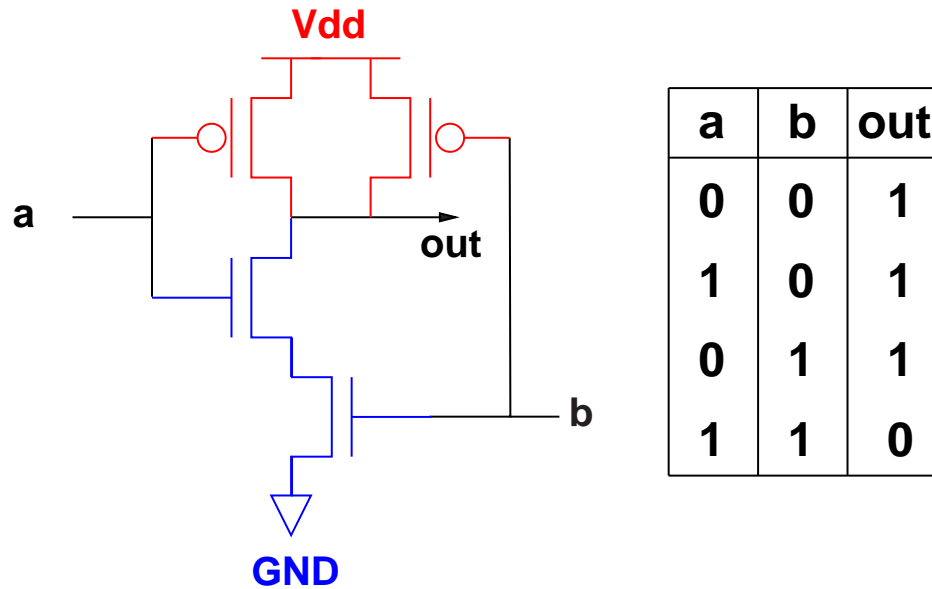
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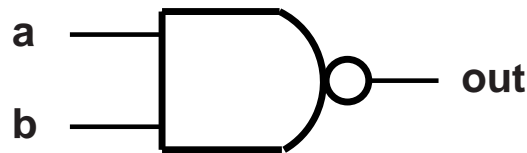
- Function: NOT
- Called an inverter
- Symbol:



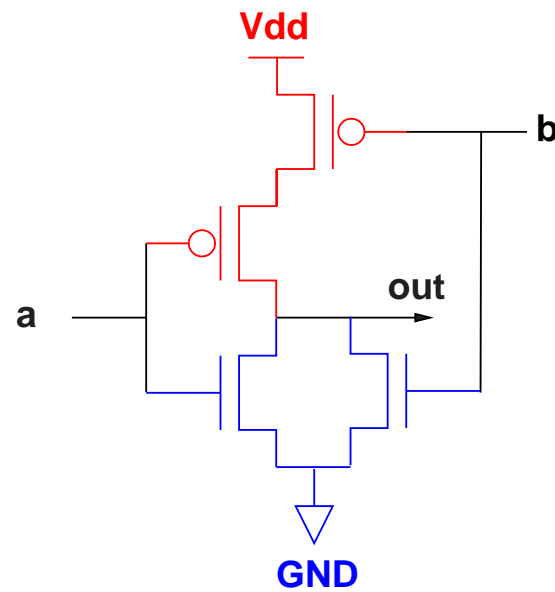
# Switching Networks: NAND



- Function: NAND
- Symbol:

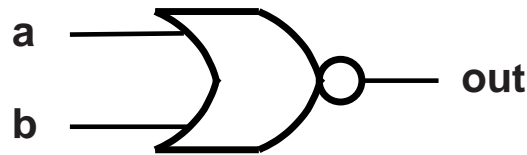


# Switching Networks: NOR



a	b	out
0	0	1
1	0	0
0	1	0
1	1	0

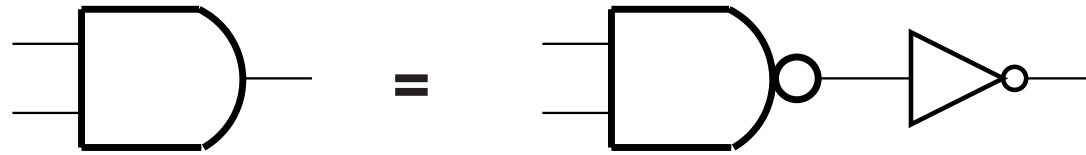
- Function: NOR
- Symbol:



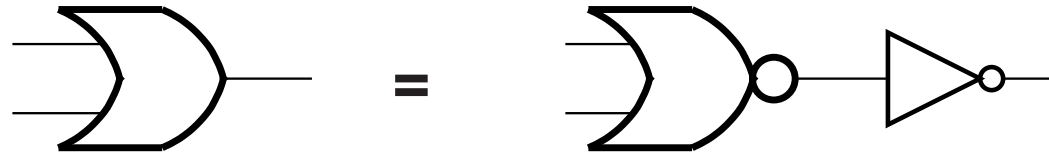
# Building Functions From Gates

---

- AND:



- OR:



Can specify function by describing gates, truth table, or **logic equations**.



# Logic Equations

---

AND:

$$out = a \cdot b$$

$$out = ab$$

$$out = a \wedge b$$

OR:

$$out = a + b$$

$$out = a \vee b$$

NOT:

$$out = \neg in$$

$$out = \overline{in}$$



# Logic Equations

---

Fun with identities:

$$a + \bar{a} = 1$$

$$a + 0 = a$$

$$a + 1 = 1$$

$$a\bar{a} = 0$$

$$a \cdot 0 = 0$$

$$a \cdot 1 = a$$

$$a(b + c) = ab + ac$$

$$\overline{(a + b)} = \bar{a} \cdot \bar{b}$$

$$\overline{(a \cdot b)} = \bar{a} + \bar{b}$$

$$a + \bar{a}b = a + b$$

Check by writing truth tables, or by manipulating logic equations.



# Let's Build An Adder

---

Write down function:

- Two 1-bit inputs,  $a$  and  $b$
- Two 1-bit outputs,  $sum$  and  $carry$

Truth-table:

$a$	$b$	$carry$	$sum$
0	0	0	0
1	0	0	1
0	1	0	1
1	1	1	0





# Let's Build An Adder

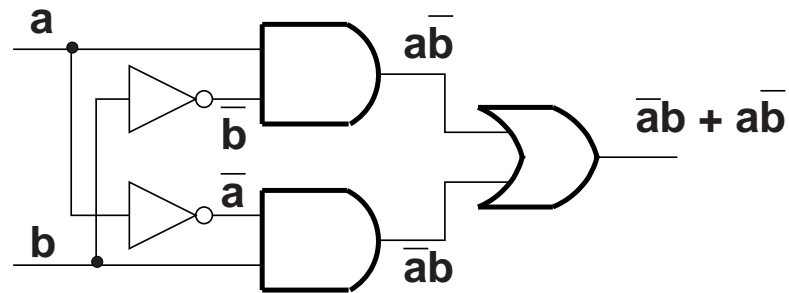
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Sum output:

a	b	sum	Logic term
0	0	0	$\bar{a} \cdot \bar{b}$
1	0	1	$a \cdot \bar{b}$
0	1	1	$\bar{a} \cdot b$
1	1	0	$a \cdot b$

Logic equation:  $a \cdot \bar{b} + \bar{a} \cdot b$

Circuit:



# Let's Build An Adder

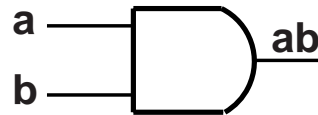
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Carry output:

a	b	carry	Logic term
0	0	0	$\bar{a} \cdot \bar{b}$
1	0	0	$a \cdot \bar{b}$
0	1	0	$\bar{a} \cdot b$
1	1	1	$a \cdot b$

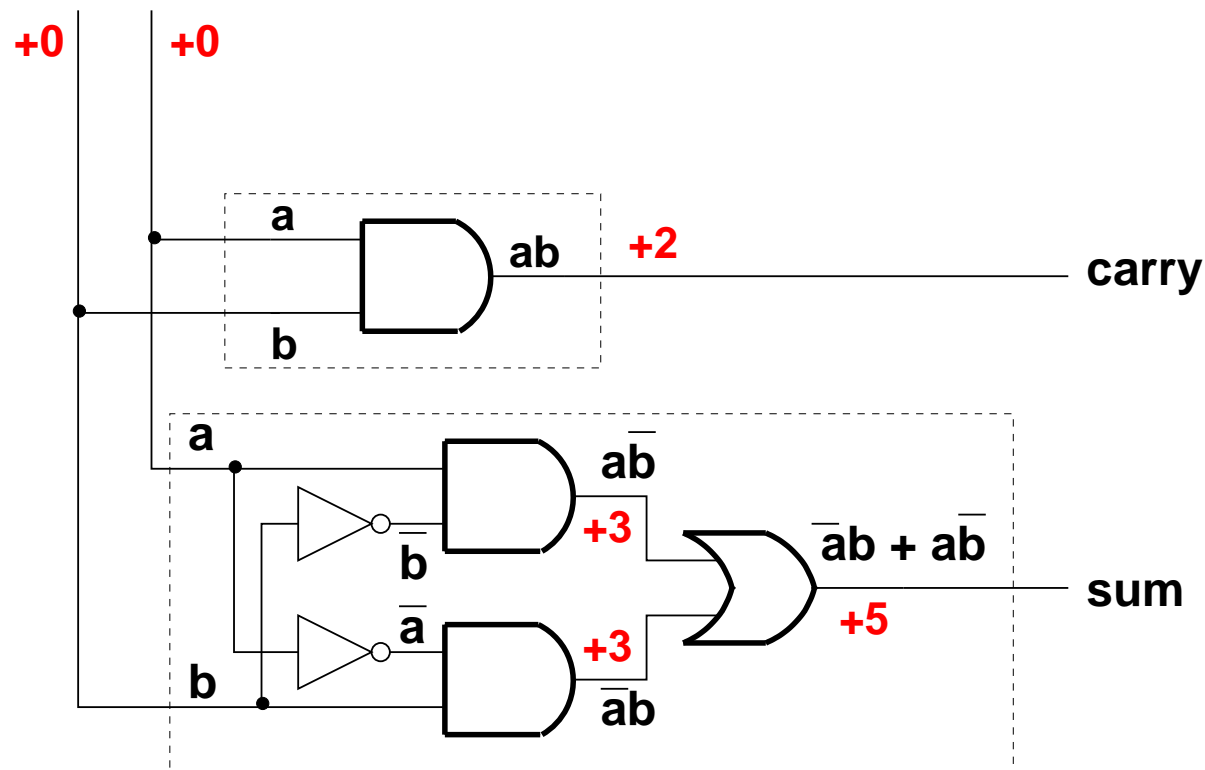
Logic equation:  $a \cdot b$

Circuit:



# Let's Build An Adder

Final Circuit:



Numbers indicate the number of sequential steps from input to output (worst-case).

