1 Introduction

In this assignment you will build an interpreter for a functional language called CL, with concurrency and imperative features. A CL program has multiple processes executing at the same time. Each process executes its own CL code, and has its own local memory. Processes can communicate to each other through a global shared memory. They can also start off other processes, or wait for the spawned processes to finish. Finally, there is an outside world that provides additional functionality (for instance, I/O support), and processes can request services from this outside world.

For this part of the project, you will implement an interpreter for programs written in CL. More precisely, you will implement the evaluation of CL expressions, including the concurrent constructs. You will also implement a garbage collector to manage your local and global memories.

2 Instructions

You will do this part of the project by modifying the source files provided in CMS, and submitting the program that results. As before, your programs must compile without any warnings. Programs that do not compile or compile with warnings will receive an automatic zero. All files submitted should not have any lines longer than 80 characters, and ideally all lines should be less than 78 characters long.

We will be evaluating your project on several different criteria: the specifications you write (where appropriate), the correctness of your implementation, code style, efficiency, and validation strategy. Correctness is worth about two thirds of the total score, and the importance of the other criteria varies from part to part.

Note that you will be building on your solution for the second part of the project, so we strongly recommend you to start early on Part I and understand the code given to you early. Part I and II are also partner assignments. You are expected to find a partner to do this assignment with by November 4. You can continue working with the partner from PS4, or find somebody else. In either case, you must sign up in CMS with that partner. If CMS shows that you don’t have a partner by November 4, we will automatically pair you up with someone else in the class at that time.

3 The CL language

The CL language has some interesting features. First, it is a concurrent language in which multiple processes can be executing simultaneously. Second, it has imperative features that allow updating memory locations. Third, processes can get additional services (including input/output operations) from an external world.
A process can launch another process using the expression `spawn e`. The expression `e` provides the program that the newly created process is supposed to execute. A process can then wait for all its spawned children to finish using `sync`.

There are two different kinds of memories that the processes can read or write. Each process has its own `local memory`, which can only be used by that process. Local memory is allocated with `lref e` expressions. In addition, there is a `global memory` that is global and shared by all the processes. Processes can communicate with each other by modifying locations in the global memory. Global memory is allocated with `gref e` expressions.

Processes can request the external world to perform actions, usually using an expression of the form `do e`. This expression is evaluated by sending the result of `e` to the external world. Different possible values of `e` are interpreted as requests to perform different actions. In this project, the `do e` expression will be used for I/O operations. For example, the expression `do 0` causes the external world to ask the user to input a number, which is returned as a result of the expression.

The behavior of the external world is not specified by the CL language. We have given you one possible implementation of the external world, but it will be modified in Part II to allow processes to sense and interact with the environment in many more ways.

3.1 Expressions

A CL program for a single process can contain the following expressions:

- `n` An integer constant, as in SML. Examples: `~3, 0, 2.`
- `(e_1, e_2)` A pair. Evaluates to the value `(v_1, v_2)` where `v_1` and `v_2` are the respective results of evaluating the expressions `e_1` and `e_2`.
- `unop e` Returns `unop` applied to the result of evaluation of `e`. `unop` is one of the following unary operators: `~` (negates an integer), and `rand` (returns a random number between 1 and `n` where `n` is the result of evaluation of `e`).
- `e_1 binop e_2` Applies binary operator `binop` to the results of evaluations of the two expressions. Both `e_1` and `e_2` must evaluate to an integer. `binop` is one of the following operators: `+`, `-`, `*`, `/`, `mod`, `<`, `=`. For the last two operators the result will be 1 if the comparison is true, and 0 otherwise.
- `e_1 ; e_2` A sequence of expressions. It is evaluated similarly to an ML sequence. First expression `e_1` is evaluated, possibly creating side effects (modifying memories). After that the result of `e_1` is thrown away and expression `e_2` is evaluated.
- `let id = e_1 in e_2` Binds the result of evaluating `e_1` to the identifier `id` and uses the binding to evaluate `e_2`. Identifiers start with a letter and consist of letters, underscores, and primes.
- `fn id => e` Anonymous function with the argument `id` and the body `e`. Note that functions are values, so the body `e` is not evaluated until an argument is supplied to the function.
- `id` Identifier. Must be contained inside a `let` or `fn` expression with the same identifier name, otherwise unbound identifier error will occur.
Function application. Evaluates expression $e_1$ to a function $\text{fn } id \Rightarrow e$, expression $e_2$ to a value $v_2$, binds $v_2$ to the identifier $id$ and uses the binding to evaluate $e$.

**if** $e$ **then** $e_1$ **else** $e_2$

Similar to the ML if/then/else expression except that the result of expression $e$ is tested for being greater than 0 (there are no booleans in CL).

Examples: if 1 then 1 else 2 returns 1, if 4<3 then 1 else 2 returns 2.

**typecase** $e$ **of**

- $(id, id') \Rightarrow e_1$
- int $id \Rightarrow e_2$
- loc $id \Rightarrow e_3$
- fun $id \Rightarrow e_4$
- any $id \Rightarrow e_5$

First evaluates expression $e$ to a value. If the result is a pair, it binds the elements of the pair to $id$ and $id'$ in the case for pairs. Otherwise, it binds the the result to $id$ in the appropriate case. The case any matches any value. It then evaluates the expression $e_i$ of the matched case.

Each of the cases is optional and can occur at most once. The case for any is allowed only if at least two of the other cases are missing. As in ML, all cases must be covered. The expression “typecase $e_1$ of any $id \Rightarrow e_2$” is equivalent to “let $id = e_1$ in $e_2$”.

Note that lists can be emulated in CL using pairs of pairs. Like pattern matching in ML, the typecase construct gives the ability to distinguish between the head and the tail of a list.

**delay** $e$ **by** $n$

Delays the evaluation of $e$ by $n$ evaluation steps. The number $n$ must be an integer constant greater or equal to 1. At each evaluation step, $n$ is decreased; when it reaches 1, the expression reduces to $e$.

**lref** $e$

Similar to the ML operation ref. First expression $e$ is evaluated to a value $v$. After that a new location loc is allocated in the process’s local memory and value $v$ is stored at this location. The return result of the expression is location loc which can be viewed as a memory address.

**gref** $e$

Similar to lref except that the new location is allocated in the global shared memory. Before allocating the location the result of $e$ is checked to ensure that it satisfies the “global memory invariant” (see section 3.3).

**!** $e$

Evaluates expression $e$ to location loc and returns the value stored at this location.

$e_1 := e_2$

Evaluates expression $e_1$ to a location loc\(_1\) and expression $e_2$ to a value $v_2$. After that replaces the value at the location loc\(_1\) with $v_2$. The return result of this expression is $v_2$. If loc\(_1\) is a location in the global memory, then the value $v_2$ is checked for the “global memory invariant” before assigning (see section 3.3).

**lock** $e_1$ $e_2$

This expression evaluates $e_1$ to a location, loc. If loc is in local memory, the program proceeds with the evaluation of $e_2$. If loc is in global memory and is not already locked, then the current process acquires a lock for loc. If any other process already has the lock, the process will continue to attempt the operation until the old lock is removed. All other cases are runtime errors.

Once the current process has grabbed the lock, the expression reduces to a new expression of the form locked loc $e_2$. Then it evaluates $e_2$, while
maintaining the lock. When the evaluation of \( e_2 \) finishes with a value \( v \), the lock is released and the value \( v \) is returned.

**do** \( e \) This allows a process to interact with the external world. First expression \( e \) is evaluated to a value \( v \) which is then sent to the external world. The return result of this expression can be arbitrary (it is specified by the external world). The list of actions currently recognized by the external world is given in section 3.6.

**spawn** \( e \) This launches a new process. The code of the spawned process is \( e \).

**sync** The current process waits (i.e., does nothing) until all of its spawned children have finished executing. Once that happens, if \( v_1, \ldots, v_n \) are the result values of the children (in the order they have been spawned), then \( \text{sync} \) evaluates to \((v_1, (v_2, (...(v_n, 0))))\).

There are two expressions that never appear in the source of a CL program, but can occur during the evaluation:

- **loc**, a memory location. A location can be viewed as a pair \((\text{scope}, \text{addr})\) where \text{scope} identifies whether it is in the local or global memory and \text{addr} is a memory address. A location can only be generated using \text{lref} and \text{gref} expressions.

- **locked loc e**. This occurs during the evaluation of a \text{lock} expression, after the lock for \text{loc} has been acquired.

We have provided for you an implementation of the expression type as \text{AbSyn.exp} in the file \text{absyn/absyn.sml}.

### 3.2 Values

Some of the expressions described above are values (i.e., they cannot be evaluated any further). Here is the list of possible values:

- Integer constants \( n \);
- Locations \( \text{loc} \);
- Functions \( \text{fn id => e} \);
- Pairs \((v_1, v_2)\), provided that \( v_1 \) and \( v_2 \) are values.

Note that there is no special type for values in our implementation; it is up to the programmer to identify which expressions are values.

### 3.3 Local and global memories

A memory \( \sigma \) can be viewed as a mapping from locations (or addresses) to values. Each process has its own local memory that cannot be accessed by other processes. In addition, there is a global memory shared among all processes.
A difference between a local and the global memories can be illustrated with the following example:

```
let
  r = lref 0
in
  spawn (fn x => (r := 1));
!r
```

This process (let’s call it “A”) allocates a location (call it \( \text{loc} \)) for an integer 0 and then launches another process (let’s call it “B”). The local memory of A is copied to the local memory of B, so local memories of A and B will contain two different locations storing value 0.

After some reductions process A evaluates to expression \(!\text{loc}\) and process B to expression \((\text{loc} := 1)\). Process B then modifies its own copy of location \(\text{loc}\) to 1; memory of process A is unchanged. Thus, process A will return 0.

Now consider the same code where \(\text{lref}\) is replaced with \(\text{gref}\). Then location \(\text{loc}\) will be allocated in the global memory, so after launching B locations \(\text{loc}\) in both processes will point to the same place. Therefore, depending on the order of executions of A and B, process A will return either 0 (if A is executed before B) or 1 (if A is executed after B).

To make sure that the local memory of a process cannot be accessed by other processes we need to maintain the following global memory invariant: values stored in the global memory do not contain locations from local memories. Thus, each modification of the global memory (i.e. expressions \(\text{gref } v\) and \(\text{loc} := v\) where \(\text{loc}\) is a location in the global memory) must be checked before evaluation: if value \(v\) contains references to local memories, then a run-time error will occur. An example of an invalid expression is \(\text{gref } (\text{lref } 0, 0)\). A process trying to execute such an expression should be terminated.

### 3.4 Evaluation

A process is represented by a unique process identifier \(\text{pid}\), local memory \(M\) and expression \(e\). A current state of the interpreter is described by a queue of processes, as well as a global memory \(M_g\), and a tree \(T\) of spawned processes. A process \(p\) is the child of \(p'\) in the spawn tree \(T\) if \(p\) has been directly spawned by \(p'\).

The interpreter repeatedly performs the following operation: it takes the process at the head of the queue, performs a single evaluation step on its expression (possibly modifying the process local and global memory or the spawn tree), and places the modified process at the end of the queue. A single step is illustrated in Figure [1](#).

It is important that each process is executed one step at a time. If we evaluated a program down to a value all at once, the system would not be concurrent because only that process would be able to run. Therefore, we must evaluate in steps.

Given an expression, the evaluator finds the leftmost subexpression that can be reduced, and reduces this subexpression.

Note that just as in ML, some expressions do not evaluate some of their subexpressions before doing a reduction. These expressions are \(\text{let } id = v \text{ in } e, \text{if } v \text{ then } e_1 \text{ else } e_2, \text{fn } id \Rightarrow e, \text{delay } e \text{ by } n, \text{typecase } v \text{ of } \langle id, id' \rangle \Rightarrow e_1 \mid \ldots, \text{spawn } e, \text{lock } \text{loc} \text{ e, and } v \text{ ; } e\). The \(v\)’s indicate
subexpressions that must be fully evaluated before the expression can be reduced, and the e’s indicate subexpressions that are not evaluated until after the reduction of the whole expression.

3.5 Reductions

The list of possible reductions that can be performed during evaluation is given below. First we consider reductions that do not change local or global memories. Letters v stand for values, and letters e for expressions which may or may not be values.

\[
\begin{align*}
\text{unop } v & \rightarrow v' & \text{where } v' = \text{unop } v \\
\text{v}_0 \text{ binop } v_1 & \rightarrow v' & \text{where } v' = \text{v}_0 \text{ binop } v_1 \\
\text{v; } e & \rightarrow e \\
\text{let } id = v \text{ in } e & \rightarrow e\{v/id\} \\
\text{(fn } id =\rightarrow e) \text{ v} & \rightarrow e\{v/id\} \\
\text{if } v \text{ then } e_1 \text{ else } e_2 & \rightarrow e_1 & v \in \{1, 2, 3 \ldots \} \\
\text{if } v \text{ then } e_1 \text{ else } e_2 & \rightarrow e_2 & \text{all other } v \\
\text{delay } e \text{ by } n & \rightarrow \text{delay } e \text{ by } n' & \text{where } n' = n - 1, \text{if } n > 1 \\
\text{delay } e \text{ by } 1 & \rightarrow e \\
\text{typecase } (v, v') \text{ of } ... (id, id') \Rightarrow e ... & \rightarrow e\{v/id, v'/id'\} \\
\text{typecase } v \text{ of } \text{lab } id \Rightarrow e ... & \rightarrow e\{v/id\} & \text{where } \text{lab} \text{ is one one the cases int, loc, fun, or any, which matches } v
\end{align*}
\]

e\{v/id\} stands for the result of substitution of value v for all occurrences of identifier id in expression e. These reductions are similar to the reductions you have learned for SML. The rules for the memory accesses are as follows:
where $loc$ is a location in the process local memory or in the global memory, and $v$ is the value stored at this location

$\text{lref } v \rightarrow loc$

where $loc$ is a new location in the process local memory

Side effect: a location $loc$ is allocated in the memory, its content is initialized with $v$

$\text{gref } v \rightarrow loc$

where $loc$ is a new location in the global memory

Checks: $v$ satisfies the global memory invariant (Section 3.3)

Side effect: a location $loc$ is allocated in the memory, with its contents initialized to $v$

$loc := v \rightarrow v$

where $loc$ is a location in the process local memory or in the global memory

Checks: $v$ satisfies global memory invariant (if $loc$ is global)

Side effect: content of the location $loc$ is replaced with $v$

Finally, the reductions for concurrent constructs are:

$\text{lock } loc \ e \rightarrow e$

where $loc$ is a location in local memory

$\text{lock } loc \ e \rightarrow \text{lock } loc \ e$

where $loc$ is a location in global memory that is currently locked by another process

$\text{lock } loc \ e \rightarrow \text{locked } loc \ e$

where $loc$ is a location in global memory and is not currently locked. Effects: location $loc$ is locked by the current process

$\text{do } v \rightarrow e$

where $e$ is the expression returned by the external world

Side effect: send $\text{doAction} (\text{pid}, v)$ to the external world (which will return an expression $e$) where $\text{pid}$ is the process identifier (see Figure 2)

$\text{spawn } e \rightarrow 0$

Side effects: (1) select a fresh process identifier $\text{pid}'$

(2) update the spawn tree $T$; and (3) launch a new process with the process identifier $\text{pid}'$ expression $e$, and a copy of the memory of the current process. (see Figure 3)

$\text{sync} \rightarrow \text{sync}$

where not all the spawned children have finished

$\text{sync} \rightarrow (v_1,..(v_n, 0))$

where $v_1, ..., v_n$ are the values that each of the spawned children have evaluated to, in the order in which the kid processes were launched.

Notice that because expressions may have side effects, it is critical that expressions are evaluated left to right. For example, $e_1 \ \text{binop } e_2$ must be evaluated as

$$e_1 \ \text{binop } e_2 \rightarrow v_1 \ \text{binop } e_2 \rightarrow v_1 \ \text{binop } v_2 \rightarrow v$$
3.6 The external world

Currently the do action performs simple I/O operations, though in Part II it will be a general mechanism for interacting with the world. The following actions are currently provided:

- **do 0**: reads a number from the input, returns it to the interpreter
- **do (1, v)**: prints the value $v$ to the output and returns $v$.
- **do (2, (c_1, (c_2, (c_3, (... (c_n, 0))))))**: prints the characters $c_1, \ldots, c_n$. Returns 1 if well-formatted, 0 otherwise.
- **do (3, v)**: if value $v$ is well formed, prints $v$ and returns 1, otherwise prints undefined text and returns 0. Here $v$ is considered well formed if it only contains pair and integer expressions.
3.7 Configurations

A configuration is the state of the entire interpreter at a particular point during execution. The configuration consists of a set of processes, each of which has a currently executing expression and local memory, a global memory that is shared by all the processes, and a spawn tree.

We can describe a single process as a triple \( \langle \text{pid}, M, e \rangle \). The entire interpreter configuration is a tuple containing the global memory \( M_g \) and the current queue of processes:

\[
\langle T, M_g, \langle \text{pid}_1, M_1, e_1 \rangle, \ldots, \langle \text{pid}_n, M_n, e_n \rangle \rangle
\]

The process at the head of the queue, process 1, is the one that will take the next evaluation step and be pushed to the end of the queue. Suppose that this process takes the evaluation step \( e_1 \longrightarrow e'_1 \), with side effects that change the local memory \( M_1 \) to \( M'_1 \), the global memory \( M_g \) to \( M'_g \), and the spawn tree from \( T \) to \( T' \). Then the effect of this step on the configuration as a whole is this:

\[
\langle T, M'_g, \langle \text{pid}_2, M_2, e_2 \rangle, \ldots, \langle \text{pid}_n, M_n, e_n \rangle, \langle \text{pid}_1, M'_1, e'_1 \rangle \rangle
\]

The type for configurations Configuration.configuration is implemented in eval/configuration.sml. A single step of the interpreter is performed by the function Evaluation.stepConfig in eval/evaluation.sml.

3.8 Creating and terminating processes

Processes can create other processes by calling \texttt{spawn e}. As a result, a new process will be added to the list of processes. The new process will have a copy of the old process local memory. The two processes will be able to communicate with each other if the old process had allocated locations in the global memory before spawning.

If a process has evaluated to a value, then it terminates—it is deleted from the list of processes. Thus, we have the following evaluation rule:

\[
\langle T, M'_g, \langle \text{pid}_2, M_2, e_2 \rangle, \ldots, \langle \text{pid}_n, M_n, e_n \rangle, \langle \text{pid}_1, M_1, v_1 \rangle \rangle
\]

Here, \( M'_g \) is the global memory with all locks belonging to \texttt{pid}_1 released. The updated spawn tree \( T' \), is the same as \( T \), but records the result value \( v_1 \) for terminated process \texttt{pid}_1.

A process should also be terminated if it causes a run-time error such as a type error (e.g. \texttt{!0}) or a violation of the global memory invariant (e.g. \texttt{gref (lref 0)}). A process that is terminated due to a run-time error yields a result of -1. These run-time errors correspond to processes for which there is no legal reduction. Note that such errors should terminate the process encountering an error but should not affect other running processes.

4 Using the interpreter

4.1 File structure

The code is structured as follows:
• absyn/absyn.sml: definitions of basic types (AbSyn.exp, AbSyn.pid, AbSyn.action)
• eval/memory.sig, memory.sml: definition of the memory type ('a Memory.memory) and associated operations
• eval/spawntree.sig, spawntree.sml: the spawn tree structure
• eval/configuration.sml: definition of the configuration type
• eval/evaluation.sml: a single step of the main interpreter loop
• eval/gc.sig, gc.sml: garbage collector
• world/action.sig: interface for interaction with the external world
• debug/debug-loop.sml: interface for debugging
• eval/check.sig, check.sml: well-formedness and consistency checking for expressions, processes and memories. Useful when debugging.
• cl/*.cl, a few sample CL programs

4.2 Running CL code

After compiling the code (CM.make()) you can enter the debugging mode using the command

```
Debug.debug "a string representing a CL program"
```

You will see a prompt (>). You can get the list of available commands by typing “help”. These are some commands for quick start:

• step: steps one step and shows the new stepped expression
• run: runs until the end
• l file: resets the interpreter and loads a file with a CL program
• h: gives you the help message and shows you many more commands
• q: quits the debugger

There are many other helpful functions and debugger commands; see debug/debug-loop.sml for more details. If you feel that the debugging tools implemented are inadequate, feel free to modify them.

4.3 String Literals

Although strings are not part of CL the parser will convert string literals into lists of integers. For example, "hello" parses as (104, (101, (108, (108, (111, 0))))).
5 Your task

Part 1: Evaluator

Parts of the single-step evaluator are currently written, but there are holes in the implementation. Also, the implementation has not been tested fully, so it is your job to fix any problems you may encounter.

Your task is to finish the single-step evaluator. You will have to make changes to the following files:

- `eval/evaluation.sml`
- `eval/reductions.sml`

To help in your task, we have also implemented some functions in `eval/check.sml` that can be used to check whether expression, processes, and memories are well formed. These functions will be useful in checking that your interpreter is implemented correctly.

To Submit: Completed versions of `eval/evaluation.sml` and `eval/reductions.sml`. Also submit a summary of your changes in an ASCII file `eval.txt`, so that we know where to look when we are grading.

Part 2: Memory Locks and The Spawn Tree

Finish the implementation of memory synchronization operations, and provide an implementation for spawn trees. You must modify the following files:

- In `eval/memory.sml`, provide implementations for `acquire`, `release` and `releaseAll`;
- In `eval/spawntree.sml`, provide an implementation for the spawn tree abstraction. Provide a concrete type `tree`, and fill in the all of the functions in this file.

To Submit: Completed copies of `memory.sml` and `spawntree.sml`.

Part 3: The garbage collector

Garbage is data in local or global memory that is not reachable by following any chain of references from a running process. These locations should be periodically reclaimed and used for subsequent allocation requests. The process of reclaiming unreachable locations is known as garbage collection.

The signature `gc.sig` describes an automatic garbage collector for the CL language. Occasionally the garbage collector will be used to clean up memory. For the purpose of CL, two kinds of garbage collection are defined: local garbage collection and global garbage collection. Local garbage collection cleans up the local memory of a particular process. Global garbage collection cleans the local memory of all processes as well as the shared global memory in a configuration.
Implement global and local garbage collection using the copy-collection algorithm described in class. As implied by gc.sig, the malloc function should try to reuse locations that the garbage collector has reclaimed.

To help you test your garbage collector, the localGC and globalGC commands in debug mode will force garbage collections to take place immediately.

**To Submit:** An implementation of the signature gc.sig (do not change the signature) in the file gc.sml.