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Types

top_level = Exp_t of exp
           | Decl_t of decl list

5 funrec = {name: id, args: (id * typ) list, ret_typ: typ}

(* Declarations *)
decl = Val_d of (id * typ * exp)
      | Fun_d of (funrec * exp)

10 (* Types *)
typ = Int_t
     | Real_t
     | Bool_t
     | Char_t
     | String_t
     | Tuple_t of typ list
     | List_t of typ
     | Fn_t of (typ * typ)
     | Ref_t of typ
     | Undef_t

15 (* Expressions *)
25 exp = Int_c of int
        | Real_c of real
        | Bool_c of bool
        | Char_c of char
        | String_c of string
        | Id_e of id
        | If_e of (exp * exp * exp)
        | Let_e of (decl list * exp)
        | Fn_e of ((id*typ)list * typ * exp)
        | Apply_e of (exp * exp)
        | Unop_e of (unop * exp)
        | Binop_e of (exp * binop * exp)
        | Tuple_e of (exp list)
        | Ith_e of (int * exp)
        | List_e of (exp list)

30 (* Values *)
40 value = Int_v of int
          | Real_v of real
          | Bool_v of bool
          | Char_v of char
          | String_v of string
          | Tuple_v of value list
          | List_v of value list
          | Fn_v of (string list * env * exp * string option)
          | Predef_v of string
          | SpecForm_v of string
          | Thunk_v of exp * env
          | Dyn_v of exp

45 and env = Env of (string * value * typ) list

Structures

50 structure AbstractSyntax = struct
  type id = string
  datatype typ = ...
  datatype binop = ...
  datatype unop = ...
  datatype exp = ...
  and decl = ...
  datatype top_level = ...

  exception TypeUnification

70 fun unifyTypes (t: typ, t': typ): typ = ...
end

structure Interpreter =
struct
75 ...
  fun loop (en: env, prenv: bool):unit =
  ...
  let
    val t = (parseString:string→AbstractSyntax.top_level option)inLine

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80 in
  (case t of
    NONE ⇒ loop(en, prenv)
    | SOME(Exp_t ex) ⇒ (print(printValue(
85 forceValue(evaluate (ex, en)),
0));
loop(en, prenv))
    | SOME(Decl_t dlist) ⇒ let
      val en = evaluateDeclare(dlist, en)
      in
90 (if prenv then print(printEnv(en, 0))
      else ())
      loop(en, prenv))
      end)
  handle Error.Error ⇒ loop(en, prenv)
95 end
...
end

structure Environment = struct
100 datatype value = ...
and env = Env of (string * value * typ) list

val top_level = Env([
  ("stmtlst", Predef_v("stmtlst"), Fn_t(Undef_t, Undef_t)),
105 ("ncat", Predef_v("ncat"), Fn_t(Undef_t, String_t)),
...
])

fun lookupBinding (id: string, Env(en)): (value * typ) option = ...
110 fun insertBinding (id: string, (v, t): value * typ, Env(en)): env = ...
end

structure Evaluator =

115 (* Variables that control the evaluator. *)
val debug: bool = false
datatype scoping_style = STATIC | DYNAMIC
val scoping: scoping_style = STATIC
datatype evaluation_style = LAZY | EAGER
120 val evaluation: evaluation_style = LAZY

fun predefined (name: string, (arg, argt): value * typ): value * typ =
(
125 ...
| ("ncat", Tuple_v sl, Tuple_t tl ) ⇒
if List.all (fn t ⇒ case t of String_t ⇒ true | _ ⇒ false) tl
then
(String_v (foldl (fn (sv, cs) ⇒ case sv of
String_v s ⇒ cs ^ s
| _ ⇒ err "internal error [10]"
130 ""
sl),
String_t)
else
err "'ncat' takes only strings"
(* If a function has a single argument, that is transmitted as such,
not as a tuple. Zero or more than one argument results in tuples. *)
| ("ncat", String_v _, String_t _) ⇒ (arg, argt)
| ("ncat", _, _ ) ⇒ err "ncat needs strings"
140 ...
)

fun specialForm (name: string, expr: exp, en: env): value * typ =
(
145 ...
case name of
"if3" ⇒
(case expr of
Tuple_e([cond, thenE, elseE]) ⇒
150 (case evaluate(cond, en) of
(Bool_v true, Bool_t) ⇒ (* evaluate 'then' branch *)
evaluate(thenE, en)
| (Bool_v false, Bool_t) ⇒ (* evaluate 'else' branch *)
evaluate(elseE, en)
| _ ⇒ err "first argument of if3 must be boolean")
155 | _ ⇒ err "incorrect argument number for if3; should be 3")
...
)

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160 (* Computes a value from expressions that might contain thunks. *)
and forceValue (v1: value, t1: typ): value * typ = ...

and evaluate (ex: exp, en: env): value * typ =
(
  ...
  case ex of
    Int_c i          => (Int_v i,   Int_t)
    ...
    | Id_e id        => (case lookupBinding (id, en) of
      NONE           => err ("unbound variable "^id)
      | SOME((Dyn_v ex, _))
                    => evaluate(ex, en)
      | SOME v       => v)
    | If_e (test, e1, e2) =>
      (case forceValue (evaluate(test, en)) of
        (Bool_v b, Bool_t) => evaluate(if b then e1 else e2, en)
        | _                => err ("if condition must be boolean"))
    | Let_e (dlist, ex)   => evaluate(ex, evaluateDeclare (dlist, en))
    | Apply_e (e1, e2)   => evaluateApply(e1, e2, en)
    | Unop_e (uop, ex)   => evaluateUnop (uop,
      forceValue(evaluate(ex, en)))
    ...
)

185 and evaluateApply (e1: exp, e2: exp, encrt: env): value * typ =
(
  ...
  let
    (*fc = function, fa = formal arg, a = actual arg, t = type, l = list*)
    val (fc, fct) = forceValue (evaluate(e1, encrt))
  in
    case fc of
      SpecForm_v name          => specialForm(name, e2, encrt)
      | Predef_v name         => predefined (name,
        evaluate (e2, encrt))
      | Fn_v (fal, env, body, name) =>
        let
          (* Are we using static or dynamic scoping? *)
          val en = case scoping of
            STATIC => env
            | DYNAMIC => encrt
          (* Evaluate (maybe now, maybe later) the function's arguments *)
          val (a, at) =
            (case evaluation of
              EAGER => evaluate (e2, encrt)
              | LAZY =>
                (case e2 of
                  Tuple_e a2 =>
                    (Tuple_v (map (fn a3 => Thunk_v(a3, encrt)) a2),
                     Tuple_t (map (fn a3 => Undef_t) a2))
                  | _ => (Thunk_v(e2, encrt), Undef_t)))
            (* Transfer values & types of actual parameters into lists. *)
          val (al, atl) = case (a, at) of
            (Tuple_v al, Tuple_t atl) => (al, atl)
            | (_, _) => ([a], [at])
          (* First, retrieve the types of the formal arguments. *)
          val (fat1, frt) = case fct of
            Fn_t(Tuple_t fat1, frt) => (fat1, frt)
            | _ => err "internal err, bad function type"
          (*
            Are there too many, too few, or just enough args?
            (Length atl = Length al) & (Length fal = Length fat)
            1 = set of matched args
            2 = supplementary or missing args
          *)
          val (fall, fat11, all, atl1, fal2, fat12, a2, atl2) =
            let
              let len = Int.min(List.length atl, List.length fal)
            in
              (List.take(fal, len), List.take(fat1, len),
               List.take(al, len), List.take(atl, len),
               List.drop(fal, len), List.drop(fat1, len),
               List.drop(al, len), List.drop(atl, len))
            end
          (*
            Are there too many arguments? That would be bad...

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*)
val _ = if List.length al2 > 0
  then err "too many arguments provided in function call"
  else ()

(*
  Do types match for the available actual arguments?
  u = unified
*)
val ut1 = ListPair.map (fn (f, a) => unifyTypes(f, a))
  (fat11, atl1)
  handle TypeUnification =>
    err "argument types don't match in function call"

250 in
  (*
    Are there too few arguments?
  *)
  if List.length fal2 > 0
  then (* this is a curried function => return closure *)
    ( Fn_v(fal2,
      ListPair.foldl (fn ((fa, a), ut, en') =>
        insertBinding(fa, (a, ut), en'))
        en
        (ListPair.zip(fall, all), ut1),
      body,
      NONE),
      Fn_t(Tuple_t fat12, frt))
    else
      (case evaluation of
        EAGER =>
          (*evaluate function, check returned type (r = returned)*)
          let
            val (rv, rt) = evaluate(
              body,
              ListPair.foldl
                (fn ((fa, a), ut, en') =>
                  insertBinding(fa, (a, ut), en'))
                (case name of
                  NONE => en
                  | SOME(s) => insertBinding(s, (fc, fct), en))
                (ListPair.zip(fall, all), ut1))
            val urt = unifyTypes(frt, rt)
            handle TypeUnification =>
              err ("actual return type does not" ^
                "match declared type")
          in
            (rv, urt)
          end
        | LAZY =>
          (* create thunk for fct body and unevaluated arguments *)
          (Thunk_v(
            body,
            ListPair.foldl
              (fn ((fa, a), ut, en') =>
                insertBinding(fa, (a, ut), en'))
              (case name of
                NONE => en
                | SOME(s) => insertBinding(s, (fc, fct), en))
              (ListPair.zip(fall, all), ut1)),
            frt))
          end
        | _ => err "attempt to evaluate non-function"
      )
    end
  )

and evaluateUnop (uop: unop, (v, t): value * typ): value * typ = ...

and evaluateBinop (bop: binop,
  (v1, t1): value * typ,
  (v2, t2): value * typ): value * typ =
(
  case (bop, v1, v2) of
    (Plus, Int_v a, Int_v b)      => (Int_v (a+b),   Int_t )
    | (Plus, Real_v a, Real_v b)  => (Real_v (a+b),   Real_t)
    | (Plus, _, _)                => err "type error(+)"
    ...
  )
and evaluateDeclare (dlist: decl list, en: env): env = ...
315 end

```