



# CS 3110

## Abstraction Functions and Representation Invariants

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Today's music: *Never Change* by JAY-Z

# Review

## **Previously in 3110:**

- Specifying functions

## **Today:**

- Specifying data abstractions

# Back to: Audience of specification

- **Clients**

- Spec informs what they must guarantee (preconditions)
- Spec informs what they can assume (postconditions)

- **Implementers**

- Spec informs what they can assume (preconditions)
- Spec informs what they must guarantee (postconditions)

But the spec isn't **enough** for implementers...

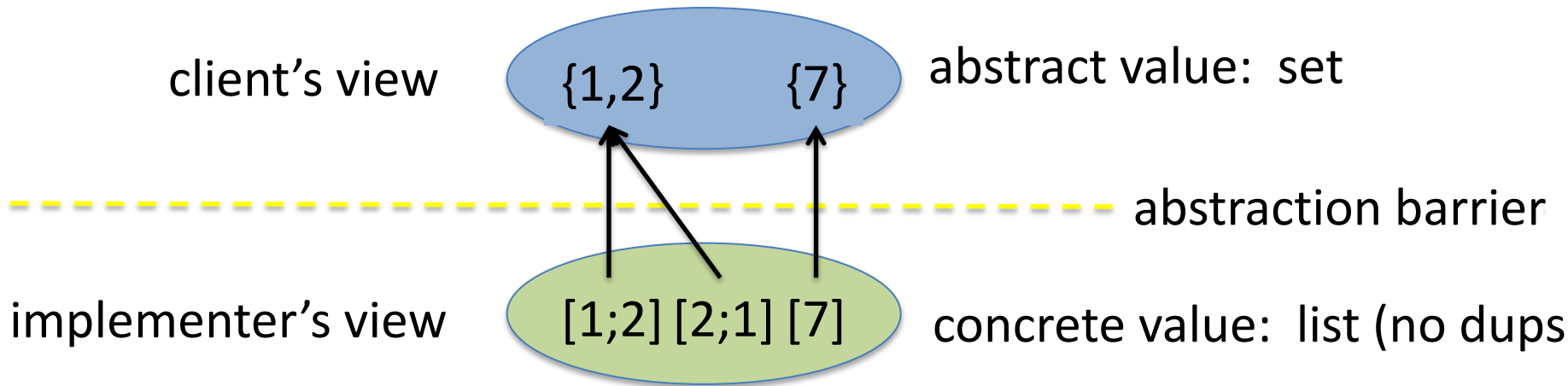
# REPRESENTATION TYPES

# Representation types

- **Q:** How to **interpret** the representation type as the data abstraction?
- **A:** Abstraction function
- **Q:** How to determine which values of representation type are **meaningful**?
- **A:** Representation invariant

# **ABSTRACTION FUNCTIONS**

# Abstraction function



the black arrows are the abstraction function

# Abstraction function

maps

valid concrete values

to

abstract values



# Documenting the AF

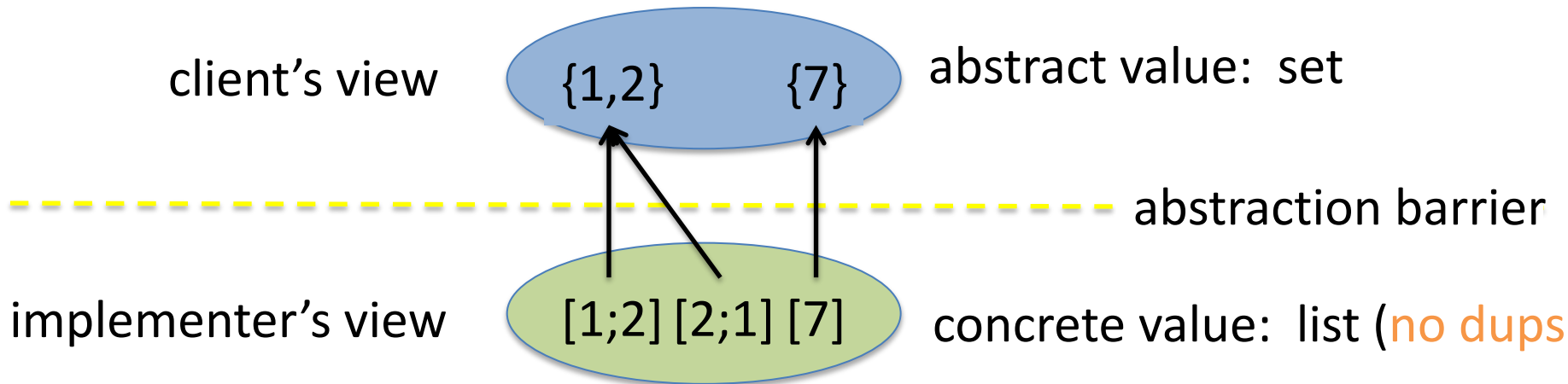
- Above rep type in implementation you write:  
`(* AF: comment *)`
- Write it **first** before implementing operations

# Representation types

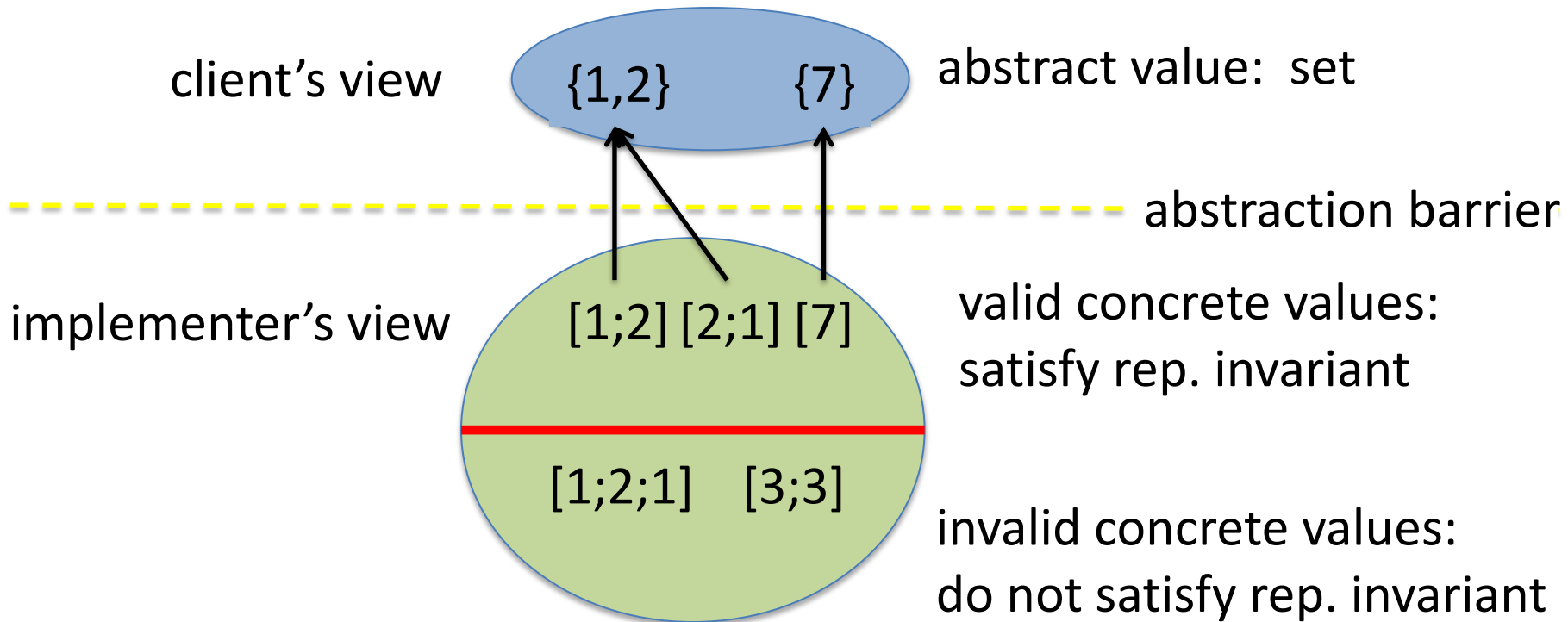
- **Q:** How to **interpret** the representation type as the data abstraction?
- **A:** Abstraction function
- **Q:** How to determine which values of representation type are **meaningful**?
- **A:** Representation invariant

# **REPRESENTATION INVARIANTS**

# Abstraction function



# Representation invariant



the thick red line is the rep. invariant

# Rep. invariant

distinguishes

valid concrete values

from

invalid concrete values

# Documenting the RI

- Above rep type in implementation you write:  
`(* RI: comment *)`
- Write it **first** before implementing operations

Rep. invariant  
implicitly part of  
every precondition and  
every postcondition  
in abstraction



# Invariant may temporarily be violated

concrete  
input



concrete  
operation



concrete  
output



RI holds



RI holds



RI maybe violated

# Discussion

When and how would you implement a RI as part of a data abstraction?

# Implementing the RI

**Idiom:** if RI fails then raise exception,  
otherwise return concrete value

# Recap

- **Q:** How to **interpret** the representation type as the data abstraction?
- **A:** Abstraction function
- **Q:** How to determine which values of representation type are **meaningful**?
- **A:** Representation invariant

# Upcoming events

- [Today] Foster Office Hours 1:15-2:15pm

*This is invariant.*

**THIS IS 3110**