

# CS 3110

## Logic in Coq

Prof. Clarkson

Fall 2018

Today's music: *Autologic* by Rage Against The Machine

# Attendance question

Is every logical proposition either true or false?

- A. Yes
- B. No
- C. Mu

# Review

## Previously in 3110:

- Functional programming in Coq
- Proofs about simple programs

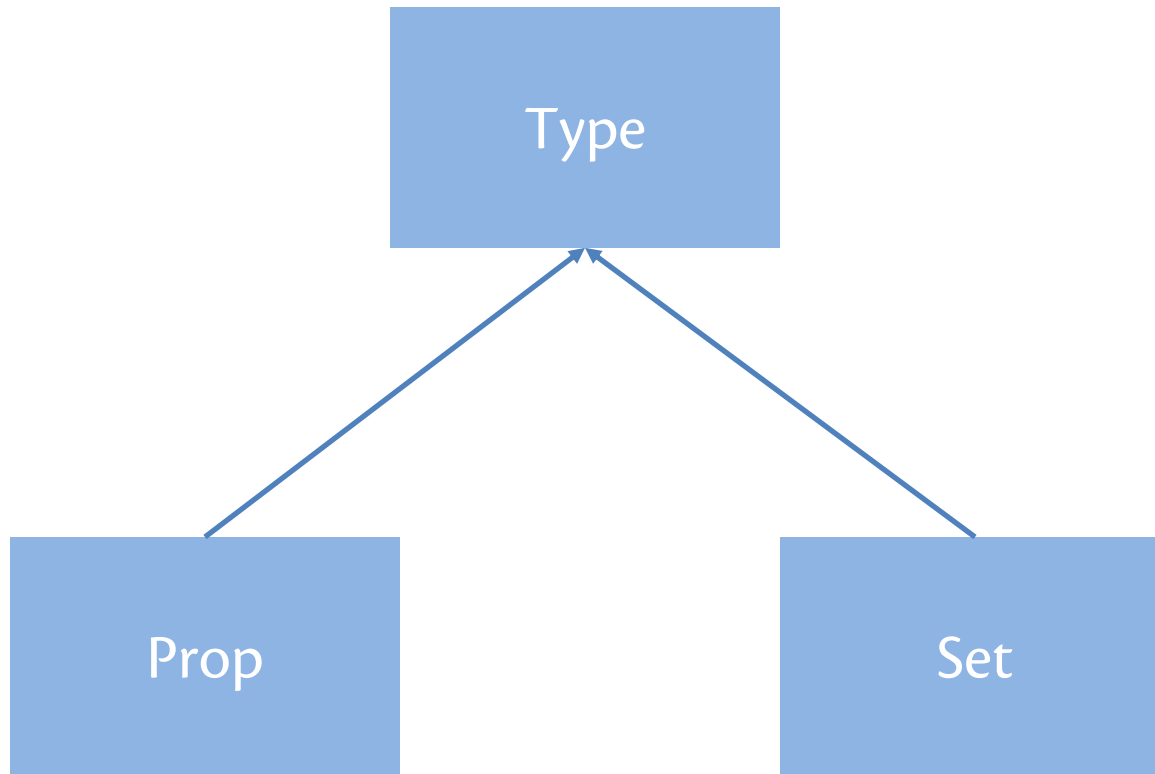
## Today:

- Logic in Coq, at the CS 2800 level

**TYPES**

Demo

# Type hierarchy



Propositions: specify assertions

Programs: specify computations

# PROPOSITIONAL LOGIC

# Logical connectives

- Implication:  $p \rightarrow p$
- Conjunction:  $p \wedge p$
- Disjunction:  $p \vee p$
- Negation:  $\sim p$

# Implication

Print `p_implies_p`.

```
p_implies_p =
```

```
fun (P : Prop) (P_assumed : P) => P_assumed  
  : forall P : Prop, P -> P
```

`p_implies_p`  
is a function

first input is a  
proposition

second input is  
proof of first input

output is that proof



Coq proofs  
are  
functional programs

# Logical connectives

- Implication:  $p \rightarrow p$
- Conjunction:  $p \wedge p$
- Disjunction:  $p \vee p$
- Negation:  $\sim p$

# Upcoming events

- A9 GIST: today, 8pm, Gates 122

*This is logical.*

**THIS IS 3110**