



CS 3110

Functors

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Today's music: "Uptown Funk"
by Mark Ronson feat. Bruno Mars

Review

Previously in 3110:

- modules, structures, signatures, abstract types
- aspects of modularity: namespaces, abstraction

Today:

- higher-order usage of modules: functors
- another aspect: code reuse

Review

Structure: a group of related *definitions*

```
struct  
  type 'a t = 'a list  
  let push x s = x::s  
end
```

Signature: a group of related *declarations* aka *type specifications*

```
sig  
  type 'a t  
  val push : 'a -> 'a t -> 'a t  
end
```

Signatures are the types of structures

Review

Module and module types: bind structures and signatures to names

```
module type Stack = sig  
  type 'a t  
  val push : 'a -> 'a t -> 'a t  
end
```

```
module ListStack : Stack = struct  
  type 'a t = 'a list  
  let push x s = x::s  
end
```

Review

Encapsulation: hide parts of module from clients

```
module type Stack = sig  
  type 'a t  
  val push : 'a -> 'a t -> 'a t  
end
```

```
module ListStack : Stack = struct  
  type 'a t = 'a list  
  let push x s = x::s  
end
```

Review

Encapsulation: hide parts of module from clients

```
module type Stack = sig
  type 'a t
  val push : 'a -> 'a t -> 'a t
end
```

type constructor t is *abstract*:
clients of this signature know the
type exists but not what it is

```
module ListStack : Stack = struct
  type 'a t = 'a list
  let push x s = x::s
end
```

Review

Encapsulation: hide parts of module from clients

```
module type Stack = sig
  type 'a t
  val push : 'a -> 'a t -> 'a t
end
```

```
module ListStack : Stack = struct
  type 'a t = 'a list
  let push x s = x::s
end
```

module is *sealed*: all definitions in it except those given in signature **Stack** are hidden from clients

Question

Consider this code:

```
module type Stack =  
sig  
  type 'a t  
  val empty : 'a t  
  val push : 'a -> 'a t -> 'a t  
end
```

```
module ListStack : Stack =  
struct  
  type 'a t = 'a list  
  let empty = []  
  let push x s = x::s  
end
```

Which of the following expressions will type check?

- A. `Stack.empty`
- B. `ListStack.push 1 []`
- C. `fun (s:ListStack) -> ListStack.push 1 s`
- D. All of the above
- E. None of the above

Question

Consider this code:

```
module type Stack =  
sig  
  type 'a t  
  val empty : 'a t  
  val push : 'a -> 'a t -> 'a t  
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Which of the following expressions will type check?

- A. `Stack.empty`
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INCLUDES

Include a signature

Interface inheritance: reuse code from other signatures

```
module type Ring = sig
  type t
  val zero : t
  val one   : t
  val add   : t -> t -> t
  val mult  : t -> t -> t
  val neg   : t -> t
end
```

```
module type Field = sig
  include Ring
  val div : t -> t -> t
end
```

Include a module

Implementation inheritance: reuse code from other structures

```
module FloatRing = struct  
  type t = float  
  let zero = 0.  
  let one  = 1.  
  let add  = (+.)  
  let mult = (*.)  
  let neg  = (~-.)  
end
```

```
module FloatField = struct  
  include FloatRing  
  let div = (/.)  
end
```

Code reuse from includes

- Implementer of one module can rely on code from another module: no need to copy code
- Solves a similar problem as class inheritance in Java
 - but without creating subtype relationships
 - decouples inheritance from subtyping



FUNCTIONORS

(funk you up?)

<https://www.youtube.com/watch?v=Au56Ah92UIk>

Structures are higher order

- You can write "functions" that manipulate structures
 - take structures as input, return structure as output
 - syntax is a bit different than functions we've seen so far
- These "functions" are called *functors*
 - One of the most advanced features in OCaml
 - A *higher-order module system*
 - Time for some **funky higher-order fun...**

Simple functor

```
module type X = sig val x : int end
```

```
module IncX (M : X) = struct
```

```
  let x = M.x + 1
```

```
end
```

functor: takes structure of type **X** as input,
uses **M** as the name of that structure in its
own body, returns a structure

```
module A = struct let x = 0 end
```

```
module B = IncX(A) (* B.x is 1 *)
```

```
module C = IncX(B) (* C.x is 2 *)
```


Alternative functor syntax

Instead of:

```
module IncX (M : X) = struct  
  let x = M.x + 1  
end
```

Could write:

```
module IncX = functor (M : X) -> struct  
  let x = M.x + 1  
end
```

Parallels syntax for anonymous functions

STANDARD LIBRARY: MAP

Map

```
(* maps over totally ordered keys *)  
module Map : sig  
  (* the input type of Make *)  
  module type OrderedType = sig type t ... end  
  
  (* the output type of Make *)  
  module type S = sig type key ... end  
  
  (* functor that makes a module *)  
  module Make (Ord : OrderedType)  
    : S with type key = Ord.t  
end
```

Map

```
module type S =  
sig  
  type key  
  type 'a t  
  val empty : 'a t  
  val mem : key -> 'a t -> bool  
  val add : key -> 'a -> 'a t -> 'a t  
  ...  
end
```

Map

```
module type OrderedType = sig
  type t
  val compare : t -> t -> int
end
```

Must return 0 if equal,
-1 if first argument is lesser,
1 if second argument is lesser

Map

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(* maps over totally ordered keys *)  
module Map : sig  
  (* the input type of Make *)  
  module type OrderedType = sig type t ... end  
  
  (* the output type of Make *)  
  module type S = sig type key ... end  
  
  (* functor that makes a module *)  
  module Make (Ord : OrderedType)  
    : S with type key = Ord.t  
end
```

sharing constraint: the output of Make additionally knows that the **key** type and the **OrderedType** are the same

Map

```
module type S with type key = Ord.t =
sig
  type key = Ord.t
  type 'a t
  val empty : 'a t
  val mem : key -> 'a t -> bool
  val add : key -> 'a -> 'a t -> 'a t
  ...
end
```

Map

Why does this work? The String module already provides a type `t` and a function `compare`.

```
# module StringMap = Map.Make(String) ;;  
module StringMap : sig  
  type key = string  
  ...  
end  
  
# let sm = StringMap.(  
  empty |> add "Alice" 4.0 |> add "Bob" 3.7)  
  
# StringMap.find "Bob" sm  
- : float = 3.7
```


Map

- What if we wanted a map with keys that are int's?
- There's no standard library module that gives us a type **t** and function **compare** for ints.
- So we build our own...

```
module Int = struct  
  type t = int  
  let compare = Pervasives.compare  
end
```

```
module IntMap = Map.Make(Int)  
let im = IntMap.(  
  empty |> add 1 "one" |> add 2 "two")
```

Question

Why didn't we write:

```
module Int : Map.OrderedType = struct  
  type t = int  
  let compare = Pervasives.compare  
end  
module IntMap = Map.Make(Int)
```

- A. Actually we should have; without it the code before doesn't compile
- B. We didn't need to; the compiler infers that module type for us
- C. It's incorrect; that's not a valid module type for Int
- D. None of the above; I'm fucked up

Question

Why didn't we write:

```
module Int : Map.OrderedType = struct  
  type t = int  
  let compare = Pervasives.compare  
end  
module IntMap = Map.Make(Int)
```

- A. Actually we should have; without it the code before doesn't compile
- B. We didn't need to; the compiler infers that module type for us
- C. It's incorrect; that's not a valid module type for Int
- D. None of the above; I'm fucked up**

Answer

```
# module IntMap = Map.Make(Int);;
module IntMap : sig
  type key = Int.t (* t is abstract! *)
  ...
end
```

```
# IntMap.(empty |> add 1 "one");;
```

Error: This expression has **type int** but
an expression was expected **of type key**

Map

- What if we wanted a map over records that sorts in a custom order?
- Again, build our own module...

```
type name = {first:string; last:string}
```

```
module Name = struct
```

```
  type t = name
```

```
  let compare {first=first1;last=last1}  
            {first=first2;last=last2} =
```

```
    match Pervasives.compare last1 last2 with  
    | 0 -> Pervasives.compare first1 first2  
    | c  -> c
```

```
end
```

```
module NameMap = Map.Make(Name)
```

Sort by last name then by first name

Map

```
let k1 =  
  {last="Kardashian"; first="Kourtney"}  
let k2 =  
  {last="Kardashian"; first="Kimberly"}  
let k3 =  
  {last="Kardashian"; first="Khloe"}  
let k4 =  
  {last="West"; first="Kanye"}  
  
let nm = NameMap.  
  empty |> add k1 1979 |> add k2 1980  
        |> add k3 1984 |> add k4 1977)
```

Map

```
let print_entry {first;last} v
    = print_string (first ^ " " ^ last ^ ": ");
    print_int v;
    print_newline ();
```

```
let () = NameMap.iter print_entry nm
```

Khloe Kardashian: 1984

Kimberly Kardashian: 1980

Kourtney Kardashian: 1979

Kanye West: 1977

Code reuse with Map

- The Map implementer built all the tricky parts of maps: adding keys and values, iterating over them, etc.
- As clients, all we have to provide is a description of our keys and how to sort them; then we get to reuse everything the implementer already built
- Solves a similar problem as Java does with interfaces +subtyping: see Java's [TreeMap](#) constructor that takes a Comparator
- OCaml's Set module is quite similar to Map in its *functorial interface*

Recap

- Functors are "functions" from structures to structures
- Functors make the OCaml module system higher-order
- Functors enable code reuse

Upcoming events

- [Wednesday] A2 due

This is higher-order funk.

THIS IS 3110