



CS 3110

Variables and Scope

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Fall 2015

Today's music: "Let It Go" from Frozen

Review

Previously in 3110:

- Aspects of a PL: syntax, semantics, idioms, libraries, tools
- **if** expressions
- Functions (recursive, anonymous)
- Lab: higher-order functions, operators, labeled arguments

Today:

- **let** expressions
- scope: in expressions, in modules
- logistics of course assignments

LET EXPRESSIONS

Let expressions

Syntax:

let **x** = **e1** **in** **e2**

x is an *identifier*

e1 is the *binding expression*

e2 is the *body expression*

let x = e1 in e2 is itself an expression

x = e1 is a *binding*

e.g.

```
let x = 2 in x+x
```

```
let inc x = x+1 in inc 10
```

```
let y = "catch" in (let z = "22" in y^z)
```

let expressions

let **x** = **e1** **in** **e2**

Evaluation:

- Evaluate **e1** to a value **v1**
- Substitute **v1** for **x** in **e2**, yielding a new expression **e2'**
- Evaluate **e2'** to **v**
- Result of evaluation is **v**

Let expressions

let x = e1 in e2

Type-checking:

If **e1 : t1**,

and if **e2 : t2** (assuming that **x : t1**),

then **(let x = e1 in e2) : t2**

Let expressions

let x = 1+4 in x*3

--> Evaluate **e1** to a value **v1**

let x = 5 in x*3

--> Substitute **v1** for **x** in **e2**, yielding a new expression **e2'**

5*3

--> Evaluate **e2'** to **v**

15

Result of evaluation is **v**

Anonymous functions

These two expressions are **syntactically different** but **semantically equivalent**:

```
let x = 7 in x+1
```

```
(fun x -> x+1) 7
```

Let expressions in REPL

Syntax:

let **x** = **e**

Implicitly, “**in** *rest of what you type*”

E.g., you type:

```
let a="catch";;  
let b="22";;  
let c=a^b;;
```

OCaml understands as

```
let a="catch" in  
let b="22" in  
let c=a^b in...
```

SCOPE: EXPRESSIONS

Scope

Bindings are in effect only in the *scope* (the “block”) in which they occur.

```
let x=42 in  
  (* y is not in scope here *)  
x + (let y="3110" in  
    (* y is in scope here *)  
    int_of_string y)
```

Exactly what you're used to from (e.g.) Java

Overlapping scope

Overlapping bindings of the same name is usually bad **idiom** (and darn confusing)

```
let x = 5 in ((let x = 6 in x) + x)
```

Question

```
let x = 5 in ((let x = 6 in x) + x)
```

To what value does the above expression evaluate?

- A. 10
- B. 11
- C. 12
- D. None of the above

How to substitute

```
let x = 5 in ((let x = 6 in x) + x)
```

-->

???

Not a choice: (why? semantics says to evaluate binding expr first)

```
let x = 5 in (6 + 6)
```

Two choices:

i. ((let x = 6 in x) + 5)

ii. ((let x = 6 in 5) + 5)

How to substitute

`let x = 5 in ((let x = 6 in x) + x)`

-->

???

Not a choice:

`let x = 5 in (6 + 6)`

Two choices:

i. `((let x = 6 in x) + 5)`

ii. ~~`((let x = 6 in 5) + 5)`~~

Why?

Principle of Name Irrelevance

The name of a variable should not matter.

In math, these are the same functions:

$$f(x) = x^2$$

$$f(y) = y^2$$

So in programming, these should be the same functions:

```
let f x = x*x
```

```
let f y = y*y
```

This principle is also called *alpha equivalence*

Principle of Name Irrelevance

Likewise, these should be the same expressions:

```
(let x = 6 in x)
```

```
(let y = 6 in y)
```

So these should also be the same:

```
let x = 5 in ((let x = 6 in x) + x)
```

```
let x = 5 in ((let y = 6 in y) + x)
```

But if we substitute inside inner **let** expression, they will not be the same:

```
(let x = 6 in 5) + 5 ==> 10
```

```
(let y = 6 in y) + 5 ==> 11
```

Back to substitution

`let x = 5 in ((let x = 6 in x) + x)`

-->

???

Not a choice:

`let x = 5 in (6 + 6)`

Two choices:

A. `((let x = 6 in x) + 5)`

B. ~~`((let x = 6 in 5) + 5)`~~ Name irrelevance is why!

Shadowing

A new binding *shadows* an older binding of the same name

```
let x = 5 in ((let x = 6 in x) + x)
```

Think of the second binding as a binding of an **entirely different variable** that just happens to have the same name as the old variable

Shadowing

A new binding *shadows* an older binding of the same name

```
let x = 5 in (  + x )
```

Think of the second binding as a binding of an **entirely different variable** that just happens to have the same name as the old variable

Shadowing is not assignment

```
let x = 5 in ((let x = 6 in x) + x)  
-----> 11
```

```
let x = 5 in (x + (let x = 6 in x))  
-----> 11
```

Shadowing is not assignment

Q: So how is this not assignment?!

```
# let x=42;;  
val x : int = 42  
# let x=22;;  
val x : int = 22
```

(@13 on Piazza)

A: The second **let** binds an entirely different variable that just happens to have the same name

Shadowing is not assignment

```
# let x=42;;  
val x : int = 42  
# let f y = x+y;;  
val f : int -> int = <fun>  
# f 0;;  
- : int = 42  
# let x=22;;  
val x : int = 22  
# f 0;;  
- : int = 42   x did not mutate!
```

Shadowing is not assignment

First: recall it's one big **let**

```
let x=42 in
let f y = x+y in
let x=22 in
f 0
```

Shadowing is not assignment

First: recall it's one big **let**

```
let x=42 in
  let f y = x+y in
    let x=22 in
      f 0
```

Shadowing is not assignment

Second: recall semantics

```
let f y = 42+y in
  let x=22 in
    f 0
```

Shadowing is not assignment

Third: recall substitution and name irrelevance

```
let f y = 42+y in
  let z=22 in
    f 0
```

Shadowing is not assignment

What have we learned?

- Each **let** binding binds an entirely new variable
- If that new variable happens to have the same name as an old variable, the new variable temporarily shadows the old
- But the old variable is still around
- And its value is immutable: **never ever changes**

Bottom line: let expressions look superficially like assignment statements from imperative languages, but are actually quite different

Let expressions (summary)

- **Syntax:**

let **x** = **e1** **in** **e2**

- **Type-checking:**

If **e1** : **t1**, and if **e2** : **t2** under the assumption that **x** : **t1**, then **let x = e1 in e2** : **t2**

- **Evaluation:**

- Evaluate **e1** to **v1**

- Substitute **v1** for **x** in **e2** yielding new expression **e2'**

- Evaluate **e2'** to **v**

- Result of evaluation is **v**

SCOPE: MODULES

Modules

- A **module** is a namespace with a collection of definitions
- E.g., the [Char module](#), the [Random module](#)
- Provides another kind of scoping: name is bound inside the module but not outside
- Access the names with dot notation, like in many languages, e.g., **Char.lowercase**
- Modules can do much more, but that will have to wait...

ASSIGNMENT LOGISTICS

A1

- Out now on course website, due in about 9 days
- Implement the Enigma encryption machine from WWII
- Needs lists: will see in lecture on Thursday
- Suggestion: in the next two days, write no code; just figure out the Enigma cipher algorithm



A1

- Individual assignment: work on your own
- (Re)read the [CS 1110 Explanation of Academic Integrity](#):
 - Fraudulently represent someone else's work as your own: punishable under AI code
 - Truthfully document that what you are submitted is mostly not your own work: grade penalty, but not an AI violation
 - Collaborate lightly with other students, getting an idea or two from them, and documenting that, but never actually designing/writing code with them: fine!!!

A1

- Soft deadline and hard deadline:
 - Submit before soft deadline, you're great!
 - Submit between soft deadline and hard deadline, 25% penalty
 - perfectly fine to do this once or twice a semester as a way to get a little extra time to finish assignment
 - doing it for every assignment will probably reduce your final course grade by about 1 letter grade
 - No submissions after hard deadline
- Note: **no grace period in CMS**. (Otherwise you'd never be able to tell whether 1-minute late submission was before or after the soft deadline)

Upcoming events

- [this week] No Clarkson office hours: at FOSAD (Foundations of Security Analysis and Design)
- [Thursday] guest lecture by Dean of CIS, Greg Morrisett

This is in scope

THIS IS 3110