# Prelim 1, Solution

CS 2110, 12 March 2019, 7:30 PM

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<tr>
<th>Question</th>
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The exam is closed book and closed notes. Do not begin until instructed.

You have **90 minutes**. Good luck!

Write your name and Cornell **NetID**, **legibly**, at the top of the first page, and your Cornell ID Number (7 digits) at the top of pages 2-8! There are 6 questions on 8 numbered pages, front and back. Check that you have all the pages. When you hand in your exam, make sure your pages are still stapled together. If not, please use our stapler to reattach all your pages!

We have scrap paper available. If you do a lot of crossing out and rewriting, you might want to write code on scrap paper first and then copy it to the exam so that we can make sense of what you handed in.

Write your answers in the space provided. Ambiguous answers will be considered incorrect. You should be able to fit your answers easily into the space provided.

In some places, we have abbreviated or condensed code to reduce the number of pages that must be printed for the exam. In others, code has been obfuscated to make the problem more difficult. This does not mean that it’s good style.

**Academic Integrity Statement:** I pledge that I have neither given nor received any unauthorized aid on this exam. I will not talk about the exam with anyone in this course who has not yet taken prelim 1.

__________________________

(signature)

## 1. Name (1 point)

Write your name and NetID, **legibly**, at the top of page 1. Write your Student ID Number (the 7 digits on your student ID) at the top of pages 2-8 (so each page has identification).
2. Short Answer (32 points)

(a) 6 points. Below are three expressions. To the right of each, write its value.
1. (char) ('G' - 2) 'E' char is numerical type.
2. new Integer(6) == new Integer(6) false These are two separate objects.
3. (int) (9.2/2) == (int) (9.2/2) true

(b) 7 points. Circle T or F in the table below.

<table>
<thead>
<tr>
<th></th>
<th>T</th>
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<tbody>
<tr>
<td>(a)</td>
<td></td>
<td></td>
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<tr>
<td></td>
<td>if (0) { return &quot;Fail&quot;; } is not valid Java. true 0 is not of type boolean</td>
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<tr>
<td>(b)</td>
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<td></td>
<td>Selection sort is stable. false Each iteration swaps the first value in a section with the min in that section; this is inherently unstable.</td>
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<td>(c)</td>
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<td>The tightest worst-case bound for Mergesort is $O(n \times \log n)$ because its depth of recursion may be proportional to the log of the length n of the array. true The depth of recursion of Mergesort is $O(\log n)$.</td>
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<td>(d)</td>
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<td></td>
<td>This declaration overrides method toString(): public String toString(int x) { return &quot;&quot; + x; }. false To override toString(), it should have no parameters.</td>
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<td>(e)</td>
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<td>We know that List is an interface. Therefore, this declaration is illegal: List c; false It is legal; it is just a declaration of a variable with a type.</td>
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<tr>
<td>(f)</td>
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<td>Because List is an interface, this statement is illegal: List c = new List(); true The new-expression is illegal since List is an interface.</td>
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<td>(g)</td>
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<td>Two versions of an overloaded method can have different numbers of parameters. true For example, String has two substring functions, one with 1 parameter and the other with two.</td>
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</table>

(c) 4 points. Write the 4-step algorithm for executing the procedure call z(8.1, 6).
1. Push a frame for the call onto the call stack. (It contains space for the parameters and local variables.)
2. Assign argument values 8.1 and 6 to the parameters.
3. Execute the method body (using the frame for the call for the local vars and pars).
4. Pop the frame for the call from the call stack. (There is no need to talk about putting the returned value on the stack because p is a procedure.)

(d) 3 points. Binary search. The precondition of binary search is that array $b$ is sorted. The postcondition is given below. If $v$ is in $b$ it indicates that the rightmost occurrence of $v$ will be found. Complete the loop invariant, which appears below the postcondition. There is no need to mention that $b$ is sorted, since that is always true.

Postcondition: $b$

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<tr>
<td></td>
<td>$0$</td>
<td>$h$</td>
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<td>$\leq v$</td>
<td>$&gt; v$</td>
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Answer: $b$

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<td>$\leq v$</td>
<td>$?$</td>
<td>$&gt; v$</td>
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(e) 6 points. Complexity
1. Suppose a method calls a procedure that requires \(300 \times n\) operations once and then calls another procedure \(\log n\) times, and this second procedure requires \(n/2\) operations. Below, circle the tightest (smallest) asymptotic time complexity of this method.

\[
O(n) \quad O(n \log n) \quad O(n^2) \\
O(n \log n) \quad \text{The total operations executed in all calls of the second procedure is } \log n \times n/2.
\]

2. To the right of the code below, write the tightest (smallest) asymptotic time complexity (in terms of \(n\)) of the code. It is known that \(n > 5\). \(O(n)\). The outer loop iterates \(n\) times. The inner loop iterates at most 6 times because each iteration adds \(n/5\) to \(j\). Each iteration takes constant time, so the inner loop takes constant time.

```java
double s = 0;
for (int h = 1; h <= n; h = h + 1) {
    for (int j = 1; j < n; j = j + n/5) {
        s = s + h/j;
    }
}
```

(f) 6 points. Testing. Below is the signature for function findFurthest.

```java
/** Return the value in b that is furthest from zero.
 * Note: -3 is further from zero than 2.
 * If several array values are the same distance from zero,
 * return the one with smallest index.
 * If b is null or empty, return 0. */
public static int findFurthest(int[] b)
```

Write six (6) distinct test cases in the space below. We don’t need formal `assertEquals` calls. Instead, say what is in `b` (or give its values as a list).

One should be convinced the function works as specified if it passes all six of these test cases. Testing nearly identical cases 6 times does not count.

We’re looking for some combination of

1. \(b\) is null.
2. \(b\) is empty.
3. \(b\) contains only 0.
4. \(b\) contains all positive values.
5. \(b\) contains all negative values.
6. \(b\) contains a mix of positive and negative values.
7. \(b\) contains multiple values the same distance from 0, e.g 2, -2.
8. \(b\) contains `Integer.MAX_VALUE` or `Integer.MIN_VALUE`.
3. **Object-Oriented Programming** (23 points)

Below and on the next page are three classes, Plane, PassengerPlane, and Trip. Unnecessary parts of classes are omitted. There is no need for assert statements for preconditions.

(a) 3 points Implement Plane’s constructor.

(b) 3 points Implement Plane’s method compareTo.

(c) 7 points Implement Plane’s method equals.

(d) 6 points Implement PassengerPlane’s constructor.

(e) 4 points Implement PassengerPlane’s method equals.

```java
/** An instance contains the serial number of a Plane and its Trips. */
class Plane implements Comparable<Plane> {
  private String serialNum; // Plane's serial number (not null)
  private ArrayList<Trip> trips; // list of Trips this Plane took

  /** Constructor: a Plane with serial number serialNum and no Trips.
   * Precondition: serialNum is not null. */
  public Plane(String serialNum) {
    this.serialNum= serialNum;
    trips= new ArrayList<>();
    // The assignment to trips is necessary. null is not an empty list.
  }

  /** Return the number of Trips this Plane has taken. */
  public int numTrips() {
    // ... implementation omitted ...
  }

  /** Compare total number of trips of the two planes
   * as per specification in interface Comparable. */
  @Override public int compareTo(Plane p) {
    return numTrips() - p.numTrips();
    // you can use if-statements or conditional expression instead,
    // and -1, 0, or 1 can be returned.
  }

  /** Return true iff this Plane and ob are of the same class and
   * have the same serial number. */
  @Override public boolean equals(Object ob) {
    if (ob == null || getClass() != ob.getClass()) return false;
    Plane p= (Plane) ob;
    return serialNum.equals(p.serialNum);
  }
}
```
PASSengerPlane has seats and passengers on the plane. */
class PassengerPlane extends Plane {
    int numSeats; // Number of seats
    ArrayList<String> passengers; // List of passengers on the plane (not null)

    /** Constr.: instance with serial number s, number of seats seats, no passengers. */
    public PassengerPlane(String s, int seats) {
        super(s);
        numSeats = seats;
        passengers = new ArrayList<>();
        // Not assigning an empty list to passengers is wrong;
        // null is not an empty list
    }

    /** Return true iff this object and ob are of the same class, they have */
    // the same name, and they have the same number of seats. */
    public boolean equals(Object ob) {
        if (!super.equals(ob)) return false;
        PassengerPlane pp = (PassengerPlane) ob;
        return numSeats == pp.numSeats;
        // This must start off with the call on super.equals. Just as in
        // in a subclass constructor the superclass fields are filled in
        // first, in the OO way, check the superclass equals first.
        // Checking getClasses in this method is redundant since they
        // are checked in super.equals.
    }
}

/** A Trip between two airports. */
class Trip {
    // We omit the implementation of this class.
}

4. Recursion (19 Points)
(a) 4 points  The Hofstadter F and M sequences are defined recursively as follows:

    public static int F(int n) {
        if (n == 0) return 1;
        return n - M(F(n - 1));
    }
    public static int M(int n) {
        if (n == 0) return 0;
        return n - F(M(n - 1));
    }

Write the calls made in evaluating the call M(2) in the order they are called, starting with M(2).

    M(2)  M(1)  M(0)  F(0)  F(0)
Class Road, below, maintains information about roads leaving Rome. A road either starts at Rome or forks from another road. A road may end or fork into one or two other roads.

(b) 7 points. Complete the body of function timeFromRome(). Use recursion; do not use loops.

(c) 8 points. Complete the body of function isTradeRoute(). Use recursion; do not use loops.

---

```java
public class Road {
    private Road source; // Road that leads to this road (null if it starts at Rome)
    private Road leftFork; // left fork of road, null if none
    private Road rightFork; // right fork of road, null if none
    private int travelTime; // time it takes to travel along this road in hours.
    private boolean hasTradePost; // true if this road has a trading post.

    /** Return the time it takes to travel from Rome to the end of this road */
    public int timeFromRome() {
        if (source == null) return travelTime;
        return travelTime + source.timeFromRome();
    }

    /** Return true if this road is part of a trade route.
     * A road is part of a trade route if it has a trading post
     * or either of its forks are part of a trade route. */
    public boolean isTradeRoute() {
        if (hasTradePost) return true;
        if (leftFork != null && leftFork.isTradeRoute()) return true;
        return rightFork != null && rightFork.isTradeRoute();
        // It's alright to start off with the base case
        // if leftFork == null && rightFork == null) return hasTradePost.
        // Our solution is shorter.
    }
}
```

---

Example:

```
ROME
 |  A
A starts at Rome. o
A forks into B, C. / \
B, C's source is A. / \
B has no forks. / B \ C
C forks into D, E. / \
D, E's source is C. o
D, E have no forks. / \
      D / \ E
```
5. **Loop Invariants** (13 points)

(a) **3 points** Consider the assertion

\[ b[0..k] \text{ are prime} \quad \& \quad k \leq j \quad \& \quad b[j+1...b.length-1] \text{ are composite (non-prime)} \]

Draw it as an array diagram below:

When the loop terminates k and j are equal.  
Don’t draw k or j directly above a line; that is ambiguous.  
The section \( b[k+1..j] \) must be there because of the term \( k \leq j \).  
It doesn’t matter what you put in it —? or unknown or leave it blank.

(b) **10 points** Below are the precondition, postcondition, and invariant of a loop that sorts an array \( b \) of Students based on the operating system on their laptops (Windows, OSX, Linux):

1. Write the initialization code that truthifies \( P: h = -1; m = b.length - 1; t = b.length - 1; \)

2. Write a while-loop condition that makes the loop terminate when \( R \) is true: \( h \neq m \) or use this alternative: \( h < m \)

3. Write the repetend. Use \( \text{swap}(b, i, j) \) to swap \( b[i] \) and \( b[j] \). Instances of class Student have three functions \( \text{usesWindows()} \) (true if the student’s operating system is Windows), \( \text{usesOSX()} \) (true if the student’s os is OSX), and \( \text{usesLinux()} \) (true if the student’s os is Linux).

\[
\begin{align*}
\text{if (b[m].usesLinux())} \quad \{ \text{swap}(b, t, m); \quad m = m-1; \quad t = t-1; \} \\
\text{else if (b[m].usesWindows())} \quad \{ \text{h = h+1; swap}(b, h, m); \} \\
\text{else m = m-1;}
\end{align*}
\]

// When we look at the repetend, we do not take into account what the initialization is. We look only at whether this Hoare triple is true:

\[
\{ \text{invariant AND h < m} \} \text{ repetend} \{ \text{invariant} \}
\]

// and whether the repetend makes progress toward termination.

// Don’t look at your initialization when writing the repetend.
6. Exception handling (12 Points)

In method `foo` to the right, `S0`, `S1`, `S3`, `S5`, `S7`, and `S9` are statements. Below, method `p` calls `foo`.

```java
public static void foo() {
    S0
    try { S1 }
    catch (Error e) { S3 }
    catch (ArithmeticException e) { S5 }
    catch (Throwable e) { S7 }
    S9
}
```

Below are four situations that could happen when the call on `foo` in method `p` is executed. Answer the question for each of these situations.

(a) 3 points Suppose `S1` throws a `Throwable`. Is it caught by the third catch clause, and if not, what happens to that `Throwable` object?
Yes, it is caught by the third catch clause.

(b) 3 points Suppose `S0` throws an `ArithmeticException`. Is it caught by the second catch clause, and if not, what happens to that `ArithmeticException` object?
It is not caught because `S0` is not within the try-block. It is thrown out to the call of `foo` in `p`.

(c) 3 points Suppose `S3` is executed and it does not throw anything. What is executed next?
`S9` is executed next.

(d) 3 points Suppose `S5` throws an `Error`. Is it caught by the third catch clause, and if not, what happens to that `Error` object?
It is not caught because `S5` is not within the try-block. It is thrown out to the call of `foo` in `p`.