The exam is closed book and closed notes. Do not begin until instructed.

You have **90 minutes**. Good luck!

Write your name and Cornell **NetID** at the top of **every** page! There are 5 questions on 9 numbered pages, front and back. Check that you have all the pages. When you hand in your exam, make sure your booklet is still stapled together. If not, please use our stapler to reattach all your pages!

We have scrap paper available. If you do a lot of crossing out and rewriting, you might want to write code on scrap paper first and then copy it to the exam, so that we can make sense of what you handed in.

Write your answers in the space provided. Ambiguous answers will be considered incorrect. You should be able to fit your answers easily into the space provided.

In some places, we have abbreviated or condensed code to reduce the number of pages that must be printed for the exam. In others, code has been obfuscated to make the problem more difficult. This does not mean that its good style.

0. **Name** 1 point

Ensure that your name and NetID is written on **every** page of this exam.
### 1. True / False (20 points)

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2. Short Answer (36 points)

(a) (4 points) Consider the following code segment, note that (int)'a' is 97, (int)'b' is 98, and (char)99 is 'c'. Execute the segment, writing each value printed to the right of the corresponding println statement.

    String a= "a"; //SOLUTION. You must know: (1) + is evaluated left to right,
    char b= 'b'; //SOLUTION. (2) if one op of + is a String, the other is
    int c= 99; //SOLUTION. converted to a String, and
            //SOLUTION. it is converted to an int, its internal repr.
    System.out.println(a + b + c); //SOLUTION: ab99
    System.out.println(a + b + (char) c); //SOLUTION: abc
    System.out.println(c + b + a); //SOLUTION: 197a
    System.out.println(b + c + a); //SOLUTION: 197a

(b) (8 points) A program segment that is supposed to store into s the product of values in b[m..n] has the following precondition and postcondition:

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<td>s = product of these</td>
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<td>Postcondition:</td>
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A loop with initialization will be written for this problem, using this loop invariant: s is the product of b[i + 1..n] —as shown as the the diagram below.

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<td>Invariant:</td>
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<td>s = product of these</td>
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</table>

Answer the following four questions, which gives you all the parts of the loop. Be extremely careful! Do not simply write the loop you are thinking of; use the invariant shown above.

(i) What initial assignment to s and i makes the invariant true?
   i = n; s = 1; —The sum of an empty set is 0, the product is 1

(ii) What condition along with the invariant implies the postcondition?
   i == m - 1

(iii) In writing the body of the loop, how do you make progress toward termination?
   i = i - 1;

(iv) In writing the body of the loop, how do you keep the invariant true while making progress toward termination?
   s = s * b[i] —put before the decrement of i
(c) (6 points) Indicate which of the following three statements about linked lists are true. Assume you have direct access only to the head of a singly linked list or the head and tail of a doubly linked list. Circle all that are true.

(i) Finding the smallest element in a sorted singly linked list takes constant time.
(ii) Inserting a value in the middle of a doubly linked list takes constant time. Starting with the head, you have to use succ fields to reach the middle. That takes time proportional to the length of the list.
(iii) Inserting a value after the third element of a doubly linked list takes time proportional to the length of the list. Use head.succ.succ to get the third element. Constant time.

(d) (6 points) Consider class A, below. Write down the statements S1, S2, S3, S4, S5, and S6 that are executed, in the order they are executed, for the following procedure calls:
1. first(7); Statements executed: S5 S4
2. first(0); Statements executed: S5 S2 S1 S6
3. first(3); Statements executed: S5 S4 S3 S1 S6

```java
class A {
    public static void first(int i) {
        second(i);
        S6;
    }

    public static void second(int i) {
        S5;
        try {
            int b = 5/i;
            S4;
            if (i == 7) throw new Exception();
            S3;
        } catch (ArithmeticException e) {
            S2;
        }
        S1
    }
}
```

(e) (4 points) Write down the steps in executing a procedure call. It's important to memorize this. Only then do you really understand method calls.

- Push a frame for the call on the stack
- Assign argument values to parameters
- Execute method
- Pop frame from stack, leaving return value on the top of the stack
(f) (4 points) Consider the following classes.

```java
class D {
    public String toString() {
        return "I'm a D";
    }
}
class B extends D {
    public String toString() {
        return "I'm a B";
    }
    public static void main(String[] args) {
        B b= new B(); // Suppose the value stored in b is B@20
        Object ob= b;
        D d= b;
        System.out.println(b.toString());
        System.out.println(ob.toString());
        System.out.println(d.toString());
    }
}
```

What is printed to the console when running class B as an application? The overriding or bottom-up rule gives you the answers.

I'm a B
I'm a B
I'm a B

(g) (4 points) Consider the following class.

```java
public class {
    public static final Suit CLUBS= new Suit();
    public static final Suit SPADES= new Suit();
    public static final Suit HEARTS= new Suit();
    public static final Suit DIAMONDS= new Suit();
    private Suit() {} 
}
```

Is there a better way to represent Suits in Java? If so, rewrite class Suit below in that way. If not, explain briefly why the above class is the best way to represent Suits.

Solution

```java
public enum Suit {CLUBS, SPADES, HEARTS, DIAMONDS}
```
3. Testing (16 points)

(a) 8 points Consider the following code, which computes the median of an array of ints. Recall that the median of a collection is the “middle” value if the collection has an odd number of elements or the arithmetic mean of two “middle” values otherwise.

```java
/** Return the median value in b.
 * Precondition: b is not null and b.length >= 1. */
public static double median(int[] b) {
    int n = b.length;
    if (n % 2 != 0) // b has an odd number of elements
        return b[n/2];
    else // b has an even number of elements
        return (b[n/2-1] + b[n/2]) / 2.0;
}
```

• Unfortunately this code has a serious bug. Write a test to illustrate the bug:
  **Solution** Try small cases first.

```java
@Test
public void testMedian() {
    assertEquals(2, median(new int[] {2, 1, 3}));
}
```

• Modify the precondition so the method meets its specification.
  **Precondition:** b is not null, b.length >= 1, and b is sorted
(b) 8 points  The following method is supposed to compute \( c \) raised to the power \( n \).

```java
/** Return \( c^n \).
 * Precondition: \( n \geq 0 \). */
public static double power(double c, int n) {
    if (n == 0) return 1;
    // n > 0
    return power(c * c, n / 2);
}
```

• Unfortunately this code also has a serious bug. Write a test to illustrate the bug:

  Solution

```java
@Test
gpublic void testPower() {
    assertEquals(125.0, power(5.0, 3));
}
```

• Modify the code so the method meets its specification:

  Solution

```java
/** Return \( c^n \).
 * Precondition: \( n \geq 0 \). */
gpublic static int power(double c, int n) {
    if (n == 0) return 1;
    // n > 0
    if (n % 2 == 0) return power(c * c, n / 2);
    return c * power(c * c, n / 2);
}
```
Reference: Java Collections

Following is a reference to selected classes (unshaded) and interfaces (shaded) from the Collections library, as well as the most important methods defined in the interfaces. This information may be useful in completing the exercise on the opposite page.

interface Collection<E> {
    boolean add(E);
    void clear();
    boolean contains(Object);
    boolean equals(Object);
    boolean isEmpty();
    boolean remove(Object);
    int size();
    ...
}

interface Set<E> extends Collection<E> {
    ...
}

interface List<E> extends Collection<E> {
    boolean add(int, E);
    E get(int);
    E remove(int);
    E set(int, E);
    ...
}

To iterate over a collection, use a for loop:

Collection<E> c = ...;
for(E e : c) {
    ...
}
4. Strings and Collections (15 points)

(a) 7 points  Suppose we have a method areAnagrams (you wrote such a method in A2):

```java
/** Return true iff s and t are anagrams of each other. */
public static boolean areAnagrams(String s, String t) { ... }
```

Complete method anagramSet below according to its specification. Note that Set is an interface, so you will have to use an implementing class to construct the actual set.

**Solution**

```java
/** Return a set of Strings in l that are anagrams of s.
 * Precondition: l != null, s != null. */
public static Set<String> anagramSet(ArrayList<String> l, String s) {
    HashSet<String> anagrams= new HashSet<String>();
    for (String e : l) {
        if (areAnagrams(e, s)) {
            anagrams.add(e);
        }
    }
    return anagrams;
}
```

(b) 8 points  Complete method getChars below according to its specification.

**Solution**

```java
/** Return a list of the characters is, in the same order, but with
 * blanks ' ' removed. Example:
 * getChars(['a', ' ', ' ', 'b', 'c', ' ', 'c', ' ']) is ['a', 'b', 'c', 'c'] */
public static ArrayList<Character> getChars(char[] b) {
    ArrayList<Character> chars= new ArrayList<Character>();
    for (char c : b) {
        if (c != ' ') {
            chars.add(c);
        }
    }
    return chars;
}
```
5. Recursion (12 Points)

(a) 6 points Define the fosterial function \( f(n, k) \) as follows:

- \( f(1, k) = f(0, k) = 1 \)
- If \( n > 1 \) and \( n \) is not divisible by \( k \), \( f(n, k) \) is the product of \( f(n - 1, k) \) and \( f(n - 2, k) \).
- If \( n > 1 \) and \( n \) is divisible by \( k \), \( f(n, k) \) is the product of \( f(n - 1, k) \), and \( n \).

Complete function fosterial below according to its specification.

Solution

```java
/** Return the fosterial value f(n,k).
 * Precondition: n >= 0, k > 0 */
public static int fosterial(int n, int k) {
    if (n <= 1) {
        return 1;
    }
    if (n % k != 0) {
        return fosterial(n-1, k) * fosterial(n-2, k);
    }
    return n * fosterial(n-1, k);
}
```

(b) 6 points Complete the following function body. Do not change \( n \) into a String or other char-valued thing. Work only with type int.

Solution 1

```java
/** Return true iff the decimal representation of n has only 5’s in it.
 * Example hasOnly5(515) is false, hasOnly5(5555) is true.
 * Precondition: n >= 0. */
public static boolean hasOnly5(int n) {
    if (n == 0) return false;
    if (n == 5) return true;
    return n % 10 == 5 && hasOnly5(n / 10);
}
```

Solution 2

```java
/** Return true iff the decimal representation of n has only 5’s in it.
 * Example hasOnly5(515) is false, hasOnly5(5555) is true.
 * Precondition: n >= 0. */
public static boolean hasOnly5(int n) {
    return n > 0 && (n == 5 || (n%10 == 5 && hasOnly5(n/10)));
}
```