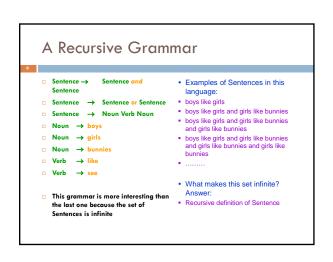


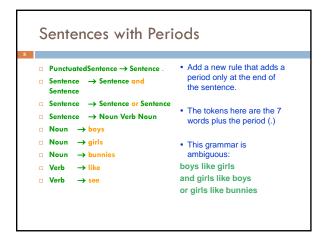
Application of Recursion So far, we have discussed recursion on integers Factorial, fibonacci, an, combinatorials Let us now consider a new application that shows off the full power of recursion: parsing Parsing has numerous applications: compilers, data retrieval, data mining,...



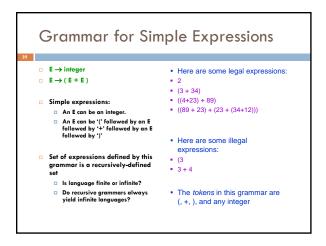




Defour What if we want to add a period at the end of every sentence? Sentence → Sentence and Sentence. Sentence → Sentence or Sentence. Sentence → Noun Verb Noun. Noun → ... Does this work? No! This produces sentences like: girls like boys . and boys like bunnies . . Sentence Sentence Sentence



Uses of Grammars Grammar describes every possible legal expression You could use the grammar for Java to list every possible Java program. (It would take forever) Grammar tells the Java compiler how to understand a Java program



```
□ Grammars can be used in two ways
□ A grammar defines a language (i.e., the set of properly structured sentences)
□ A grammar can be used to parse a sentence (thus, checking if the sentence is in the language)
□ To parse a sentence is to build a parse tree
□ This is much like diagramming a sentence
```

```
Recursive Descent Parsing

| Idea: Use the grammar to design a recursive program to check if a sentence is in the language
| To parse an expression E, for instance
| We look for each terminal (i.e., each token)
| Each nonterminal (e.q., E) can handle itself by using a recursive call
| The grammar tells how to write the programl
| Doolean parseE() {
| if (first token is an integer) return true;
| if (first token is '(') {
| parseE();
| Make sure there is a '+' token;
| parseE();
| Make sure there is a ')' token;
| return true;
| }
| return false;
| }
```

Java Code for Parsing E

```
public static Node parseE(scanner scanner) {
    if (scanner.hasNextInt()) {
        int data = scanner.nextInt();
        return new Node(data);
    }
    check(scanner, '(');
    left = parseE(scanner);
    check(scanner, '+');
    right = parseE(scanner);
    check(scanner, ')');
    return new Node(left, right);
}
```

Detour: Error Handling with Exceptions

- Parsing does two things:
 - □ It returns useful data (a parse tree)
 - □ It checks for validity (i.e., is the input a valid sentence?)
 - □ How should we respond to invalid input?
 - □ Exceptions allow us to do this without complicating our code unnecessarily

Exceptions

- 15
 - Exceptions are usually thrown to indicate that something bad has happened
 - IOException on failure to open or read a file
 - ClassCastException if attempted to cast an object to a type that is not a supertype of the dynamic type of the object
 - NullPointerException if tried to dereference null
 - \blacksquare ArrayIndexOutOfBoundsException if tried to access an array element at index i < 0 or ϵ $\,$ the length of the array
 - ☐ In our case (parsing), we should throw an exception when the input cannot be parsed

Handling Exceptions

- Exceptions can be caught by the program using a try-catch block
 - □ catch clauses are called exception handlers

```
Integer x = null;
try {
    x = (Integer)y;
    System.out.println(x.intValue());
} catch (ClassCastException e) {
    System.out.println("y was not an Integer");
} catch (NullPointerException e) {
    System.out.println("y was null");
}
```

Defining Your Own Exceptions

- An exception is an object (like everything else in Java)
 - □ You can define your own exceptions and throw them

```
class MyOwnException extends Exception {}
...
if (input == null) {
    throw new MyOwnException();
}
```

Declaring Exceptions

 In general, any exception that could be thrown must be either declared in the method header or caught

```
void foo(int input) throws MyOwnException {
  if (input == null) {
    throw new MyOwnException();
  }
  ...
}
```

- □ Note: throws means "can throw", not "does throw"
- □ Subtypes of RuntimeException do not have to be declared (e.g., NullPointerException, ClassCastException)
 - □ These represent exceptions that can occur during "normal operation of the Java Virtual Machine"

How Exceptions are Handled

- - $\ \square$ If the exception is thrown from inside the try clause of a try-catch block with a handler for that exception (or a superclass of the exception), then that handler is executed
 - Otherwise, the method terminates abruptly and control is passed back to the calling method
 - □ If the calling method can handle the exception (i.e., if the call occurred within a try-catch block with a handler for that exception) then that handler is executed
 - Otherwise, the calling method terminates abruptly, etc.
 - ☐ If none of the calling methods handle the exception, the entire program terminates with an error message

Using a Parser to Generate Code

- ■We can modify the parser so that it generates stack expressions:
 - STOP
 - (2 + 3)PUSH 2 PLISH 3 ADD STOP
- □Goal: Method parseE should return a string containing stack code for expression it has parsed
- Method parseE can generate code in a recursive way:
- code to evaluate arithmetic For integer i, it returns string "PUSH"
 - For (E1 + E2).
 - Recursive calls for E1 and E2 return code strings c1 and c2
 - Then to compile (E1 + E2), return
 - Top-level method should tack on a STOP command after code received from parseE

Does Recursive Descent Always Work?

descent is hard to use

not in this course)

technique (there are several, but

- $lue{}$ There are some grammars $lue{}$ For some constructs, recursive that cannot be used as the basis for recursive descent • Can use a more powerful parsing
 - A trivial example (causes infinite
 - S → b
 - S → Sq
- □Can rewrite grammar

 - A → a
 - A → αA

Syntactic Ambiguity

- Sometimes a sentence has

 - □ The string aaxbb can be parsed in two ways
 - This kind of ambiguity sometimes shows up in programming languages
 - □if E1 then if E2 then S1 else S2
- □Which then does the else go
- This ambiguity actually affects the program's meaning
- How do we resolve this? Provide an extra non-grammar rule (e.g., the else goes with the closest if)
- Modify the language (e.g., an if-statement must end with a 'fi')
- Operator precedence (e.g.
 1 + 2 * 3 should be parsed as
- Other methods (e.g., Python uses amount of indentation)

Conclusion

- - □ Recursion is a very powerful technique for writing compact programs that do complex things
 - □ Common mistakes:
 - □ Incorrect or missing base cases
 - □ Subproblems must be simpler than top-level problem
 - □ Try to write description of recursive algorithm and reason about base cases before writing code
 - - Syntactic junk such as type declarations, etc. can create mental fog that obscures the underlying recursive algorithm
 - Best to separate the logic of the program from coding details

Exercises

- □ Think about recursive calls made to parse and generate code for simple expressions
 - **2 (2 + 3)**
 - **((2 + 45) + (34 + -9))**
- Derive an expression for the total number of calls made to parseE for parsing an expression
 - Hint: think inductively
- □ Derive an expression for the maximum number of recursive calls that are active at any time during the parsing of an expression (i.e. max depth of call stack)

Exercises

- Write a grammar and recursive program for sentence palindromes that ignores white spaces & punctuation
 - Was it Eliot's toilet I saw?
 - No trace; not one carton
 - □ Go deliver a dare, vile dog!
 - □ Madam, in Eden I'm Adam
- $\hfill\Box$ Write a grammar and recursive program for strings A^nB^n

 - AB AABB
- Write a grammar and recursive program for Java identifiers
 <a