CS211 Spring 2005
Prelim 1
March 10, 2005

Name_________________________ NetId________________

Instructions

Write your name and Cornell netid above. There are 6 questions on 9 numbered
pages. Check now that you have all the pages. Write your answers in the boxes
provided. Use the back of the pages for workspace. Ambiguous answers will be
considered incorrect. The exam is closed book and closed notes. Do not begin until
instructed. You have 90 minutes. Good luck!

<table>
<thead>
<tr>
<th>Score</th>
<th>1/15</th>
<th>2/24</th>
<th>3/10</th>
<th>4/15</th>
<th>5/21</th>
<th>6/15</th>
<th>Σ/100</th>
</tr>
</thead>
<tbody>
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<td></td>
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<td></td>
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</tr>
</tbody>
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1. (15 points) Prove by induction that for all \( n \geq 0 \),

\[
\sum_{i=0}^{n-1} i(i + 1) = \frac{n^3 - n}{3}.
\]

Label clearly the parts of your proof. In the induction step, state the induction hypothesis and indicate exactly where in your argument it is used. Make sure your argument is perfectly clear—any ambiguity whatsoever will result in loss of points.
2. (24 points) Say what is printed by the following Java programs.

(a) class Xp {
    public static void main(String[] args) {
        System.out.println(new Xp().ff());
    }
    String ff() {
        char[][] a = {{'a','b','c'},{'d','e'}};
        StringBuilder s = new StringBuilder();
        for (char[] t : a) {
            for (char u : t) {
                s.append(u);
            }
        }
        return s.toString();
    }
}

(b) class Enum {
    enum Season { WINTER, SPRING, SUMMER, FALL }
    public static void main(String[] args) {
        System.out.println(new Enum().pf());
    }
    String pf() {
        if (Season.WINTER.equals("WINTER")) return "equal";
        else return "not equal";
    }
}
(c) class Fs {
    static String s = "hello";
    public static void main(String[] args) {
        new Fs().foo();
        System.out.println(s);
    }
    void foo() {
        String s = "world";
    }
}

(d) class Wg {
    static int x = 0;
    int y;
    Wg() { y = x++; }
    public String toString() {
        return String.valueOf(y);
    }
    public static void main(String[] args) {
        String s = new Wg().toString();
        s += new Wg().toString();
        s += new Wg().toString();
        System.out.println(s);
    }
}
(e) class Rts {
    public static void main(String[] args) {
        System.out.println(zorg(new RtsC()));
    }
    static int zorg(RtsA x) {
        return x.f() * 10 + x.a;
    }
}
abstract class RtsA {
    int a = 2;
    int f() { return a; }
}
class RtsB extends RtsA {
    int a = 3;
    int f() { return a; }
}
class RtsC extends RtsB {
    int a = 4;
}

(f) class Yfk {
    public static void main(String[] args) {
        System.out.println(new YfkC().x);
    }
}
abstract class YfkA {
    int x = 3;
    YfkA() { x++; }
}
class YfkB extends YfkA {}
class YfkC extends YfkB {"}
(g) class Vbn {
    public static void main(String[] args) {
        System.out.println(new VbnC().zorg());
    }
}
class VbnB {
    String zorg(VbnB x) { return x.f(); }
    String f() { return "VbnB"; }
}
class VbnC extends VbnB {
    String zorg() { return super.zorg(this); }
    String f() { return "VbnC"; }
}

(h) class MyInteger {
    int value;
    MyInteger(int v) { value = v; }
}
class Tvm {
    public static void main(String[] args) {
        MyInteger s = new MyInteger(13);
        int t = 13;
        foo(s, t);
        System.out.println(s.value + " " + t);
    }
    static void foo(MyInteger u, int v) {
        u.value = 12;
        v = 12;
    }
}
3. (10 points)

(a) Explain, in at most 50 words, the difference between *reference types* and *primitive types* in Java.

(b) Explain, in at most 50 words, the difference between *static types* and *dynamic types* in Java.
4. (15 points) Binary trees and lists were defined in class in terms of TreeCell and ListCell. Lists are terminated by null, and one or both children of a TreeCell may be null.

```java
class TreeCell {
    Object datum;
    TreeCell left, right;
    ...
}

class ListCell {
    Object datum;
    ListCell next;
    ListCell(Object obj, ListCell c) {
        datum = obj;
        next = c;
    }
    ListCell(Object obj) {
        this(obj, null);
    }
}
```

Write a recursive method `tree2List` that, for a given binary tree, creates a list of the elements in preorder. For each TreeCell in the input tree, there should be exactly one ListCell with the same datum in the output list, and the order of elements in the list from front to back should be the same as preorder in the original tree. (*Hint.* Create the list from back to front. Use the second argument of the helper function to pass the accumulated list so far.)

```java
static ListCell tree2List(TreeCell t) {return tree2List(t,null);}
static ListCell tree2List(TreeCell t, ListCell c) {
```
5. (21 points) True or false?

(a) T  F A downcast can change the dynamic type of an object.
(b) T  F An upcast can change the dynamic type of an object.
(c) T  F A private field can only be accessed by methods in the same class.
(d) T  F Java supports multiple inheritance.
(e) T  F A class that implements an interface I must also implement all superinterfaces of I.
(f) T  F A call to super or this in a constructor must occur first.
(g) T  F "211".equals(211)
(h) T  F "211" instanceof Integer
(i) T  F The static type of an expression is determined by whether the variables in it have been declared static.
(j) T  F The static type of the expression (Integer)x is Integer.
(k) T  F A static field is shared by all objects of the class.
(l) T  F A non-abstract subclass of an abstract class A must implement all methods declared abstract in A.
(m) T  F Subclasses and subtypes are the same thing.
(n) T  F Abstract classes and interfaces cannot be instantiated.
(o) T  F int[] is a reference type.
(p) T  F Local variables of a method can be declared static provided the method is declared static.

Questions (q)–(u) refer to the following grammar for well-parenthesized Boolean expressions with operators & (and), | (or), and ! (not), constants true and false, and variables V (not defined in the grammar). Spaces are not significant.

\[
\begin{align*}
E & \rightarrow V \\
E & \rightarrow (E & E) \\
E & \rightarrow true \\
E & \rightarrow (E | E) \\
E & \rightarrow false \\
E & \rightarrow !$E
\end{align*}
\]

(q) T  F The following is a sentence: !!!( true | true )
(r) T  F The following is a sentence: ((true))
(s) T  F The following is a sentence: ( !true & ( false | true ))
(t) T  F All sentences are of finite length.
(u) T  F The number of possible sentences is infinite.
6. (15 points) Write an equals method for String. You may use the following methods from the String class:

```java
char charAt(int index)  // returns the char value at the specified index
int length()           // returns the length of this string
```

Indexing starts at 0. Your method should return a value even if the argument is not a String.

```java
public boolean equals(Object obj) {

```