NAME : ____________________________________________________

NETID: ______________

• The exam is closed book and closed notes. Do not begin until instructed. You have 90 minutes. Good luck!

• Start by writing your name and Cornell netid on top! There are 9 numbered pages. Check now that you have all the pages.

• Web, email, etc. may not be used. Calculator with programming capabilities are not permitted—no calculators should be needed anyway. This exam is individual work.

• We have scrap paper available, so you if you are the kind of programmer who does a lot of crossing out and rewriting, you might want to write code on scrap paper first and then copy it to the exam, just so that we can make sense of what you handed in!

• Write your answers in the space provided. Ambiguous answers will be considered incorrect. You should be able to fit your answers easily into the space we provided. Answers that are not concise might not receive full points.

• In some places, we have abbreviated or condensed code to reduce the number of pages that must be printed for the exam. In others, code has been obfuscated to make the problem more difficult. This does not mean that its good style.

POINTS:

Classes, Interfaces, Types, and Stuff ______ / 13
Recursion ______ / 18
Trees ______ / 16
Asymptotic Complexity ______ / 17
Sorting ______ / 14
Lists ______ / 17

=========

Total ______ / 95
1. Answer the following questions with either true or false. No explanation necessary. 9 pts.

- Java interfaces do not allow static method definitions.
- All types in Java are subtypes of Object.
- All classes in Java implicitly extend the Object class.
- A cast can change the dynamic type of a variable.
- A subclass can override a private method of its parent class to make it public.
- Upcasts can produce runtime errors.
- The dynamic type of an argument to an overloaded method determines which of the methods is selected.
- Java interfaces can not contain variable definitions.
- The dynamic type of a variable must always be a subtype of the static type.

2. What is printed by `System.out.println(new Bar("A"));` for the following two classes? 4 pts.

```java
class Foo {
    String s;

    Foo(String t) {
        s = "C" + t;
    }

    public String toString() {
        return s;
    }
}

class Bar extends Foo {
    Bar(String r) {
        super("B" + r);
    }
}
```
2 Recursion

1. What is the output of `goforit(false, false)`?

   ```java
   public static void goforit(boolean a, boolean b) {
       if (!a & !b) {
           goforit(a, !b);
           System.out.println("KABOOM!");
       }
       else {
           if (a & !b) {
               goforit(a, !b);
           }
           else if (!a & b) {
               goforit(!a, !b);
           }
           System.out.println(a + " " + b);
       }
   }
   ```

2. Write a method with the signature `public static int sumOfSquares(int[] x)` that returns the sum of all the array elements' squared values. Do this without using any loops but use recursion instead. You can create a helper method, but you may not create any static fields in the class.

   ```java
   ```
3 Trees

1. Given the sequence of integers (4, 1, 10, 5, 2, 14), consider a binary search tree (BST) constructed by inserting the sequence of integers at the next available location (using the usual increasing numerical ordering, with lower values on the left, and larger values on the right). Draw a diagram of the binary search tree that you would obtain.

7 pts.

2. What sequence of elements would you obtain if you traversed this binary search tree (BST) using (i) Preorder traversal, (ii) Inorder traversal, and (iii) Postorder traversal?

9 pts.

Preorder:

Inorder:

Postorder:
4 Asymptotic Complexity

1. Answer the following questions with either true or false. No explanation necessary. 8 pts.

   - $n^2 = O(n^n)$  
   - $\sqrt{n} = O(\log(n))$  
   - $\sqrt{n} = O(2^{2^n})$  
   - $n^{\log(n)} = O(2^{2^{1000}})$  
   - Inserting an element into a sorted linked list with $n$ elements can be done in worst-case time $O(\log(n))$.
   - The worst-case time complexity of MergeSort is the same as QuickSort.
   - SelectionSort has expected-case time complexity of $O(n \log(n))$.
   - InsertionSort has worst-case time complexity of $O(n \log(n))$.

2. Using the definition of big $O$ notation, prove that $f(n) = \frac{1}{n} + n \log(n) + n^2$ is $O(n^2)$ by finding a suitable witness pair $(c, N)$. 9 pts.
5 Sorting

1. Given the disguised sorting method below, what would be printed in the console with the input [3,5,2,6,1,4]?

```java
public int crimeSort(int[] lineup){

    int n = lineup.length;
    int i,j;
    int suspect;
    int crimes = 0;

    for (j = 0; j < n-1; j++) {

        suspect = j;
        for ( i = j+1; i < n; i++) {
            if (lineup[i] < lineup[suspect]) {
                suspect = i;
            }
        }
        if ( suspect != j ) {
            int accomplice = lineup[j];
            lineup[j] = lineup[suspect];
            lineup[suspect] = accomplice;
            crimes++;
        }

        // Print out "lineup":
        String s = "";
        for (int j = 0; j < n; j++){
            s = s + lineup[j] + " ";
        }
        System.out.println(s);
    }

    return crimes;
}
```
2. Give an array of length 6 that would minimize the number returned (i.e., \texttt{crimes}) by crimeSort. Also, state the value of \texttt{crimes}. 

3 pts.

3. Give an array of length 6 that would maximize the number returned (i.e., \texttt{crimes}) by crimeSort. Also, state the value of \texttt{crimes}. 

3 pts.

4. Answer with “Yes” or “No” or “Maybe” or “Sometimes”: Is the sorting algorithm from above stable? 
No explanation necessary. 

3 pts.
6 Lists

1. Assume that the following class List implements a singly-linked list comprised of ListNode objects. Write a List method “int getSumOfSquares()” that computes the sum of squares of the list’s values.

```
class ListNode {
    public ListNode next;
    public int value;

    public ListNode() {}
}

public class List {
    public ListNode start;
    public List() {
        // other methods of singly-linked list implementation are not shown
    }
```
2. Add a method \texttt{void removeOddEntries()\;} to the \texttt{List} class from above. This method should remove any \texttt{ListNode} objects corresponding to odd-valued entries. If the list does not contain any odd entries, then the list should remain unchanged. Note: Do NOT use other methods in \texttt{List}, but write the method from scratch.

9 pts.