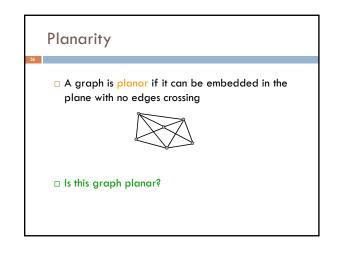
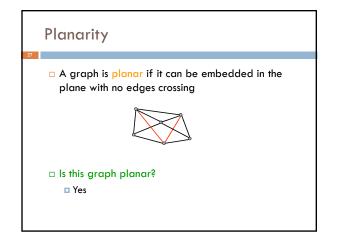


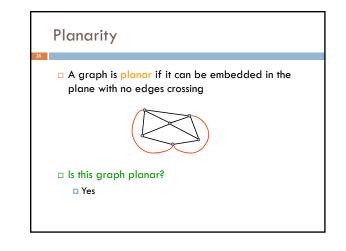
An Application of Coloring

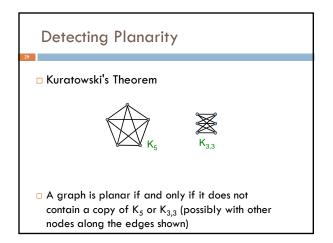
- Vertices are jobs
- Edge (u,v) is present if jobs u and v each require access to the same shared resource, and thus cannot execute simultaneously
- Colors are time slots to schedule the jobs
- Minimum number of colors needed to color the graph = minimum number of time slots required

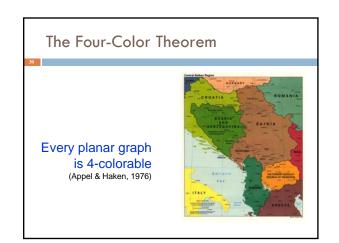




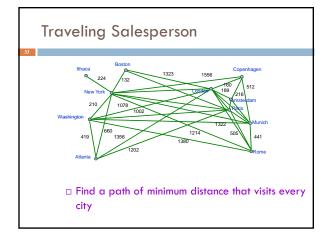


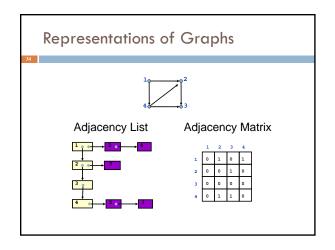


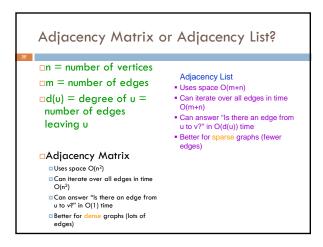


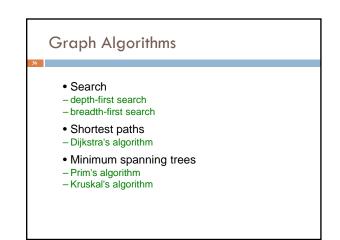


Bipartite Graphs • A directed or undirected graph is bipartite if the vertices can be partitioned into two sets such that all edges go between the two sets • The following are equivalent • G is bipartite • G is 2-colorable • G has no cycles of odd length • J



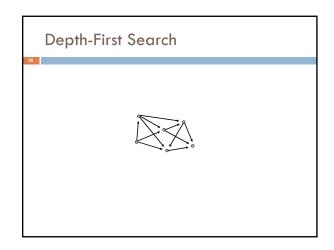


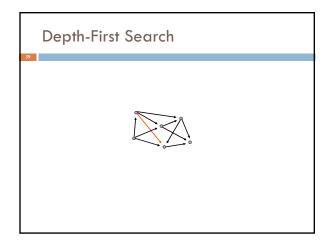


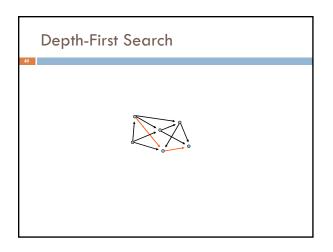


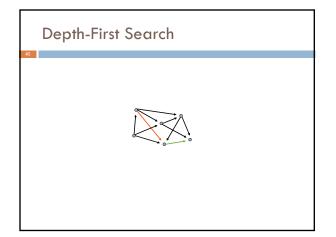
Depth-First Search

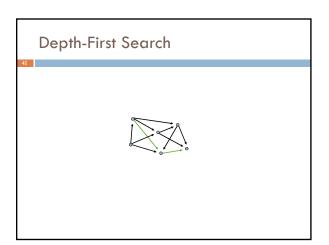
- Follow edges depth-first starting from an arbitrary vertex r, using a stack to remember where you came from
- When you encounter a vertex previously visited, or there are no outgoing edges, retreat and try another path
- Eventually visit all vertices reachable from r
- If there are still unvisited vertices, repeat
- O(m) time

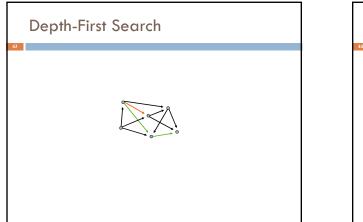


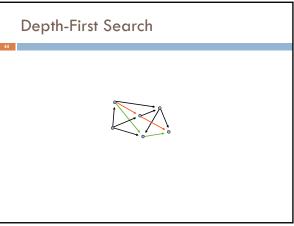


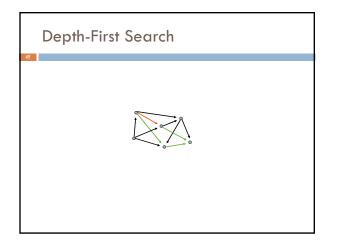


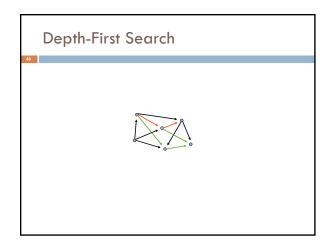


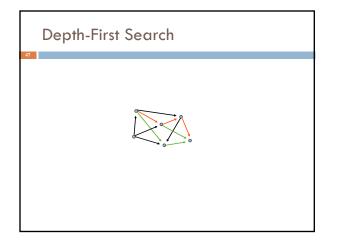


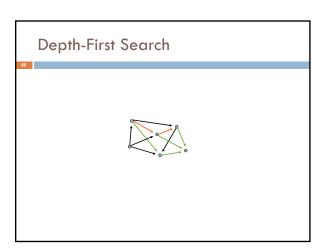


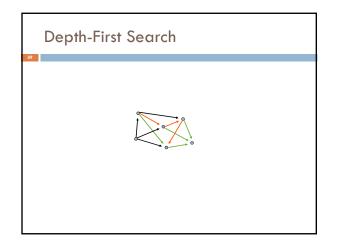


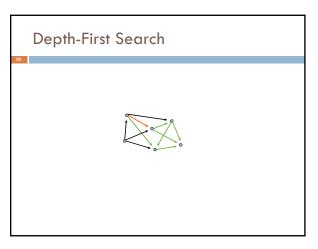


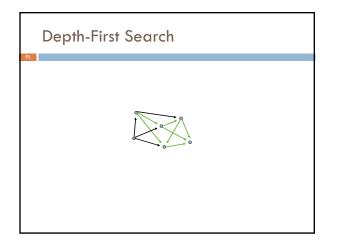


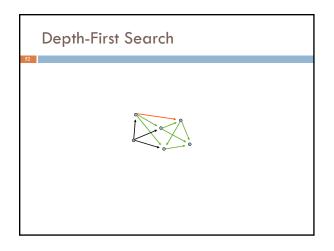


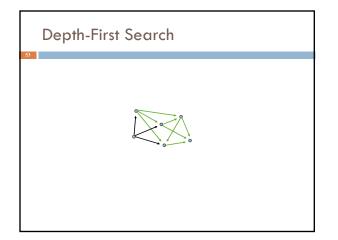


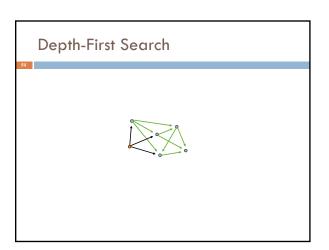


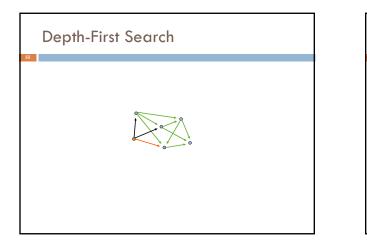


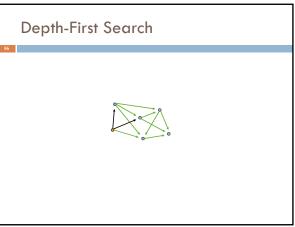


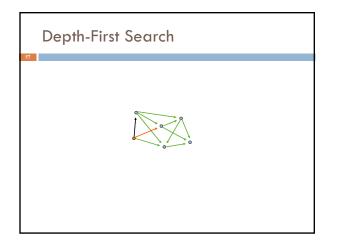


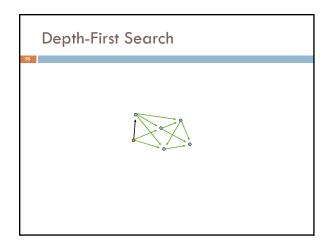


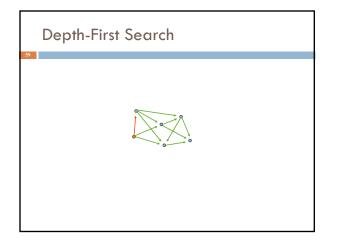


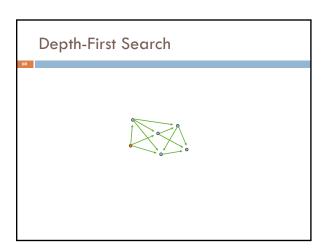


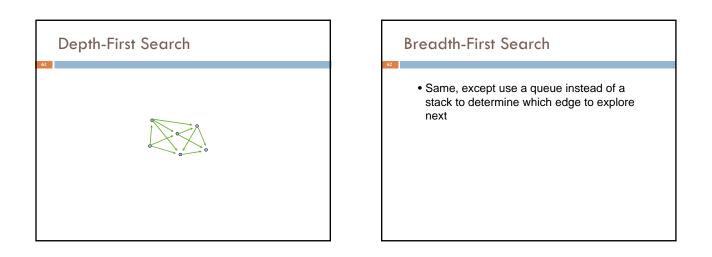


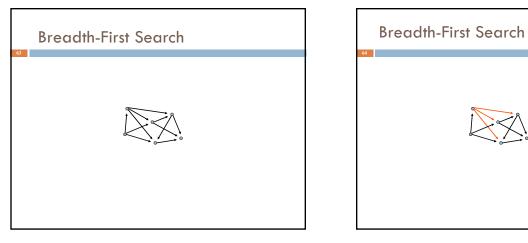


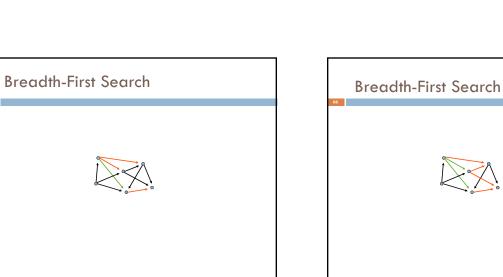




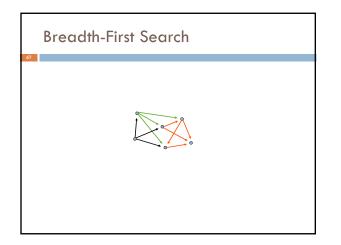


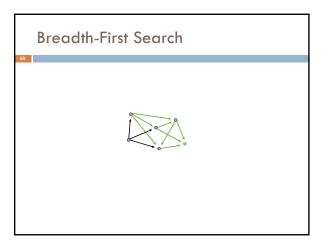


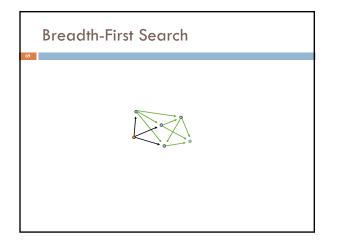


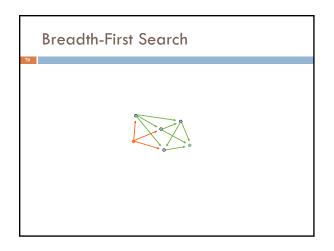


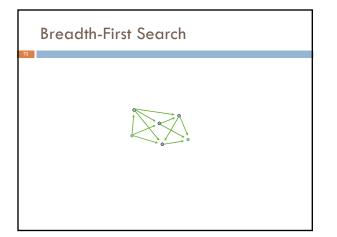


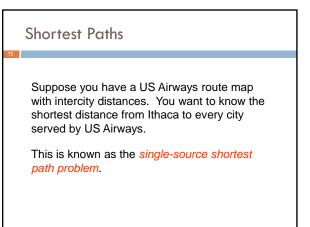


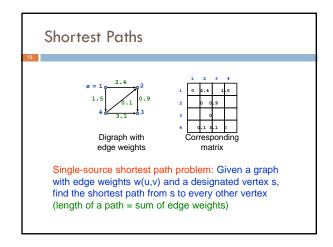


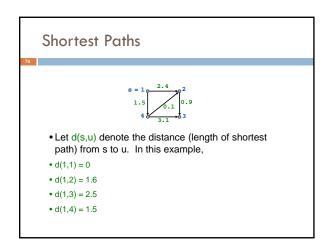


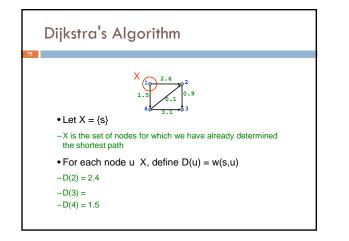


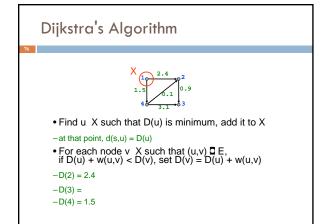


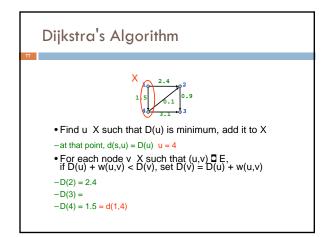


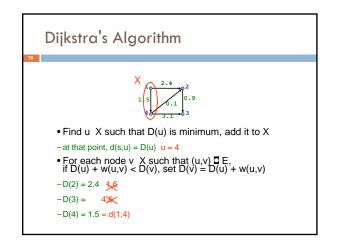


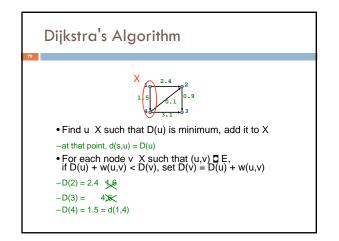


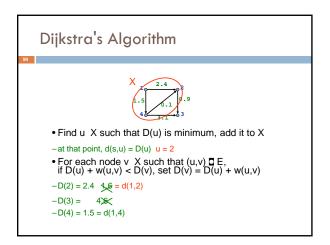


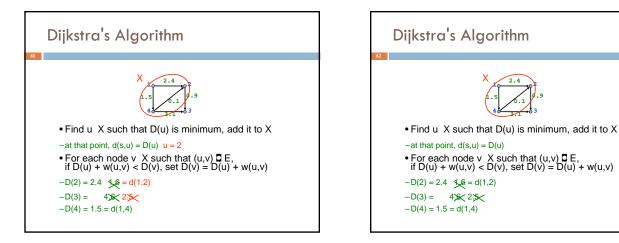


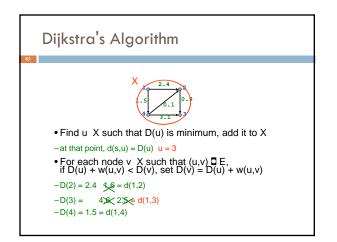


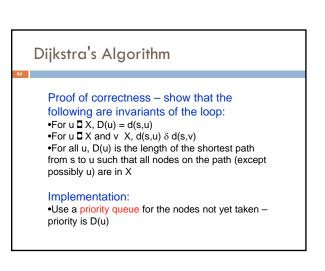












Complexity

- Every edge is examined once when its source is taken into \boldsymbol{X}
- A vertex may be placed in the priority queue multiple times, but at most once for each incoming edge
- Number of insertions and deletions into priority queue = m + 1, where m = |E|
- Total complexity = O(m log m)

Conclusion

- There are faster but much more complicated algorithms for single-source, shortest-path problem that run in time O(n log n + m) using something called *Fibonacci heaps*
- It is important that all edge weights be nonnegative

 Dijkstra's algorithm does not work otherwise, we
 need a more complicated algorithm called
 Warshall's algorithm
- Learn about this and more in CS4820