

**Topics:** One simple approach to the problem of learning a translation dictionary; this approach illustrates a general method for learning when hidden structure is involved, and echoes an approach we've considered in a different context earlier in the course.

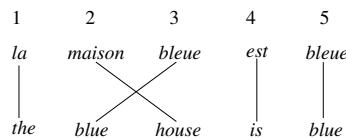
### I. Example translation pair

*Un programme a été mis en application*

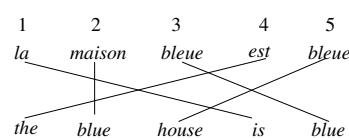
vs.

*And a program has been implemented*

**II. Example alignments** Here is a graphical depiction of two out of the 120 possible alignments<sup>1</sup> for the sentence pair “*la maison bleue est bleue* vs. *the blue house is blue*”, where the French sentence is the source.



[A1]



[A2]

Formally, we would denote [A1] by  $(1 \leftrightarrow 1, 2 \leftrightarrow 3, 3 \leftrightarrow 2, 4 \leftrightarrow 4, 5 \leftrightarrow 5)$ .

### III. Notation

- For a sentence pair  $p$ , let  $\text{Aligns}(p)$  be the set of all possible alignments of the two sentences in  $p$ , and let  $\text{NumAligns}(p)$  be the size of this set.
- Let  $\text{freq}(s \leftrightarrow t, A)$  be the number of times we have the source word  $s$  “matched” to the target word  $t$  in alignment  $A$ . In our example above, we have  $\text{freq}(\text{bleue} \leftrightarrow \text{blue}, [\text{A1}]) = 2$ .

<sup>1</sup>There are only 120 because we only consider “one-to-one and onto” alignments.

#### IV. An iterative learning algorithm for MT

Inspired by IBM's Candide system from the 80s and 90s.

1. *Initialization:* For every sentence pair  $p$ , for every alignment  $A$  of  $p$ , set  $\text{Awt}^{(0)}(A) = 1/(\text{NumAligns}(p))$ .
- Let  $i$  be increasing from 1 on, until the translation weights “converge”:*
2. *Compute temporary translation weights:*  
For every source/target word pair  $(s, t)$ , set  $\text{TempTr}(s \rightarrow t)$  to  $\sum_A \text{freq}(s \leftrightarrow t, A) \text{Awt}^{(i-1)}(A)$ .
3. *Get the translation weights by sum-normalizing the temporary ones:*  
For each source word  $s$ , compute  $\text{norm}_s = \sum_{t'} \text{TempTr}(s \rightarrow t')$ ;  
then, set each  $\text{Tr}^{(i)}(s \rightarrow t)$  to  $\text{TempTr}(s \rightarrow t)/\text{norm}_s$ .
4. *Compute temporary alignment weights:* For every alignment  $A = (1 \leftrightarrow a(1); 2 \leftrightarrow a(2); \dots; \ell \leftrightarrow a(\ell))$ ,  
set  $\text{TempAwt}(A)$  to  $\text{Tr}^{(i)}(s_1 \rightarrow t_{a(1)}) \times \text{Tr}^{(i)}(s_2 \rightarrow t_{a(2)}) \dots \times \text{Tr}^{(i)}(s_\ell \rightarrow t_{a(\ell)})$
5. *Get the alignment weights by sum-normalizing the temporary ones:* For each pair  $p$ ,  
compute  $\text{norm}_p = \sum_{A' \in \text{Aligns}(p)} \text{TempAwt}(A')$ ;  
then, for every  $A$  in  $\text{Aligns}(p)$ , set  $\text{Awt}^{(i)}(A)$  to  $\text{TempAwt}(A)/\text{norm}_p$ .

#### V. Example<sup>2</sup> partial execution

Suppose we have two sentence pairs,  $p_1 = \text{"chat bleu vs. blue cat"}$  and  $p_2 = \text{"chat vs. cat"}$ . This yields three alignments:

$$\begin{aligned} A_1 &= (1 \leftrightarrow 1; 2 \leftrightarrow 2) \quad (\text{so } \textit{chat} \text{ aligned to } \textit{blue} \text{ in } p_1) \\ A'_1 &= (1 \leftrightarrow 2; 2 \leftrightarrow 1) \quad (\text{so } \textit{chat} \text{ aligned to } \textit{cat} \text{ in } p_1) \\ A_2 &= (1 \leftrightarrow 1) \quad (\text{only one possible choice}) \end{aligned}$$

|              | Alignment weights                        |        |       | Translation weights                   |                                      |                                       |                                      |
|--------------|--|--------|-------|---------------------------------------|--------------------------------------|---------------------------------------|--------------------------------------|
|              | $A_1$                                    | $A'_1$ | $A_2$ | $\text{chat} \rightarrow \text{blue}$ | $\text{chat} \rightarrow \text{cat}$ | $\text{bleu} \rightarrow \text{blue}$ | $\text{bleu} \rightarrow \text{cat}$ |
| a. Init      | 1/2                                      | 1/2    | 1     | —                                     | —                                    | —                                     | —                                    |
| b. TempTr's  | “  | “      | “     | 1/2                                   | 3/2                                  | 1/2                                   | 1/2                                  |
|              | (insert normalization computations here) |        |       |                                       |                                      |                                       |                                      |
| c. Tr's      | “  | “      | “     | 1/4                                   | 3/4                                  | 1/2                                   | 1/2                                  |
| d. TempAwt's | 1/8                                      | 3/8    | 3/4   | “                                     | “                                    | “                                     | “                                    |
|              | (insert normalization computations here) |        |       |                                       |                                      |                                       |                                      |
| e. Awt's     | 1/4                                      | 3/4    | 1     | “                                     | “                                    | “                                     | “                                    |
| f. TempTr's  | “  | “      | “     | 1/4                                   | 7/4                                  | 3/4                                   | 1/4                                  |
|              | (insert normalization computations here) |        |       |                                       |                                      |                                       |                                      |
| g. Tr's      | “  | “      | “     | 1/8                                   | 7/8                                  | 3/4                                   | 1/4                                  |

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<sup>2</sup>Adapted from Sections 26 (“Chicken and egg”) and 27 (“Now for the Magic”) of Kevin Knight’s (1999) *A Statistical MT Tutorial Workbook* (<http://www.isi.edu/natural-language/mt/wkbk.rtf>). The tutorial also discusses more advanced models, and is often fairly amusing to boot.