This 90-minute exam has 6 questions worth a total of 100 points. Read over the whole test before starting. Budget your time wisely. Use the back of the pages if you need more space. You may tear the pages apart; we have a stapler at the front of the room.

It is a violation of the Academic Integrity Code to look at any exam other than your own, to look at any other reference material, or to otherwise give or receive unauthorized help.

You will be expected to write Python code on this exam. We recommend that you draw vertical lines to make your indentation clear, as follows:

```python
def foo():
    if something:
        do something
        do more things
    do something last
```

You should not use loops or recursion on this exam. Beyond that, you may use any Python feature that you have learned in class (if-statements, try-except, lists), unless directed otherwise.

<table>
<thead>
<tr>
<th>Question</th>
<th>Points</th>
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<tbody>
<tr>
<td>1</td>
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</table>

The Important First Question:

1. [2 points] Write your last name, first name, and netid, at the top of each page.
## Reference Sheet

Throughout this exam you will be asked questions about strings and lists. You are expected to understand how slicing works. In addition, the following functions and methods may be useful.

### String Functions and Methods

<table>
<thead>
<tr>
<th>Expression or Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>len(s)</code></td>
<td>Returns: number of characters in <code>s</code>; it can be 0.</td>
</tr>
<tr>
<td><code>a in s</code></td>
<td>Returns: True if the substring <code>a</code> is in <code>s</code>; False otherwise.</td>
</tr>
<tr>
<td><code>s.count(s1)</code></td>
<td>Returns: the number of times <code>s1</code> occurs in <code>s</code></td>
</tr>
<tr>
<td><code>s.find(s1)</code></td>
<td>Returns: index of the first character of the FIRST occurrence of <code>s1</code> in <code>s</code> (-1 if <code>s1</code> does not occur in <code>s</code>).</td>
</tr>
<tr>
<td><code>s.find(s1,n)</code></td>
<td>Returns: index of the first character of the first occurrence of <code>s1</code> in <code>s</code> STARTING at position <code>n</code> (-1 if <code>s1</code> does not occur in <code>s</code> from this position).</td>
</tr>
<tr>
<td><code>s.rfind(s1)</code></td>
<td>Returns: index of the first character of the LAST occurrence of <code>s1</code> in <code>s</code> (-1 if <code>s1</code> does not occur in <code>s</code>).</td>
</tr>
<tr>
<td><code>s.isalpha()</code></td>
<td>Returns: True if <code>s</code> is <code>not empty</code> and its elements are all letters; it returns False otherwise.</td>
</tr>
<tr>
<td><code>s.isdigit()</code></td>
<td>Returns: True if <code>s</code> is <code>not empty</code> and its elements are all numbers; it returns False otherwise.</td>
</tr>
<tr>
<td><code>s.isalnum()</code></td>
<td>Returns: True if <code>s</code> is <code>not empty</code> and its elements are all letters or numbers; it returns False otherwise.</td>
</tr>
<tr>
<td><code>s.islower()</code></td>
<td>Returns: True if <code>s</code> is <code>has at least one letter</code> and all letters are lower case; it returns False otherwise (e.g. <code>'a123'</code> is True but <code>'123'</code> is False).</td>
</tr>
<tr>
<td><code>s.isupper()</code></td>
<td>Returns: True if <code>s</code> is <code>has at least one letter</code> and all letters are upper case; it returns False otherwise (e.g. <code>'A123'</code> is True but <code>'123'</code> is False).</td>
</tr>
<tr>
<td><code>s.lower()</code></td>
<td>Returns: A copy of <code>s</code> with all letters lower case.</td>
</tr>
<tr>
<td><code>s.upper()</code></td>
<td>Returns: A copy of <code>s</code> with all letters upper case.</td>
</tr>
</tbody>
</table>

### List Functions and Methods

<table>
<thead>
<tr>
<th>Expression or Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>len(x)</code></td>
<td>Returns: number of elements in list <code>x</code>; it can be 0.</td>
</tr>
<tr>
<td><code>y in x</code></td>
<td>Returns: True if <code>y</code> is in list <code>x</code>; False otherwise.</td>
</tr>
<tr>
<td><code>x.count(y)</code></td>
<td>Returns: the number of times <code>y</code> occurs in <code>x</code></td>
</tr>
<tr>
<td><code>x.index(y)</code></td>
<td>Returns: index of the FIRST occurrence of <code>y</code> in <code>x</code> (an error occurs if <code>y</code> does not occur in <code>x</code>).</td>
</tr>
<tr>
<td><code>x.index(y,n)</code></td>
<td>Returns: index of the first occurrence of <code>y</code> in <code>x</code> STARTING at position <code>n</code> (an error occurs if <code>y</code> does not occur in <code>x</code>).</td>
</tr>
<tr>
<td><code>x.append(y)</code></td>
<td>Adds <code>y</code> to the end of list <code>x</code>.</td>
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<tr>
<td><code>x.insert(i,y)</code></td>
<td>Inserts <code>y</code> at position <code>i</code> in list <code>x</code>, shifting later elements to the right.</td>
</tr>
<tr>
<td><code>x.remove(y)</code></td>
<td>Removes the first item from the list whose value is <code>y</code> (an error occurs if <code>y</code> does not occur in <code>x</code>).</td>
</tr>
</tbody>
</table>

The last three list methods are all procedures. They return the value `None`. 

Page 2
2. [12 points total] **Short Answer Questions.**

   (a) [4 points] What is an *expression*? What is a *statement*? Give an example of each.

   (b) [4 points] Consider the following two assignment statements

   ```python
   >>> a = 3//2
   >>> b = 3.0//2
   ```

   What are the values in the variables `a` and `b`? Explain your answers.

   (c) [4 points] What is the difference between a *mutable* and an *immutable* type? Give an example of each shown in class.

3. [21 points total] **Objects and Functions.**

   One of the most popular classes in Python is the `Date` class, which represents a month, day, and year. For this problem, all objects of this class have the following attributes:

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Meaning</th>
<th>Invariant</th>
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<tbody>
<tr>
<td>month</td>
<td>the month as number</td>
<td>int value between 1 and 12 (inclusive)</td>
</tr>
<tr>
<td>day</td>
<td>the day of the month</td>
<td>int value between 1 and <code>d.daysInMonth()</code> (inclusive)</td>
</tr>
<tr>
<td>year</td>
<td>the year</td>
<td>int value greater than 0</td>
</tr>
</tbody>
</table>

   In addition, all `Date` objects have the following method:

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>d.daysInMonth()</code></td>
<td><strong>Returns</strong>: number of days in the current month of <code>d</code>.</td>
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</table>

   To create a new `Date` object, the constructor function is `Date(month, day, year).`
(a) [6 points] Implement the function below according to the specification.

```python
def last_day(date):
    """Returns the date of the last day of the current month
    
    Example: if d is Date(2,12,2000), last_day(d) returns Date(2,29,2000)
    
    Precondition: date is a Date object"
```

(b) [15 points] Implement the function below according to the specification.

```python
def next_day(date):
    """MODIFIES date to be the next calendar day
    
    Example: if d is Date(2,12,2000), next_day(d) modifies d to Date(2,13,2000)
    if d is Date(2,29,2000), next_day(d) modifies d to Date(3,1,2000)
    if d is Date(12,31,2000), next_day(d) modifies d to Date(1,1,2001)
    
    Precondition: date is a Date object"
```
4. [21 points] **Call Frames.**

Consider the following function definitions.

```python
1 def mixup(a):
2     """Returns a mixed up copy of a
3     Pre: a is a nonempty list of ints"
4     b = a[:1]
5     c = merge(b, a[1:])
6     return c

7 def merge(a, b):
8     """Returns merging of a, b
9     Pre: a, b are nonempty lists of ints"
10    b[a[0]] = a[0]
11    return b+a
```

Assume `a = [1, 2, 3]` is a global variable referencing a list in the heap, as shown below.

On the next two pages, diagram the evolution of the call

```python
a = mixup(a)
```

Diagram the state of the *entire call stack* for the function `mixup` when it starts, for each line executed, and when the frame is erased. If any other functions are called, you should do this for them as well (at the appropriate time). This will require a total of **eight** diagrams, not including the (pre-call) diagram shown.

You should draw also the state of global space and the heap at each step. You can ignore the folders for the function definitions. Only draw folders for lists or objects. You are also allowed to write “unchanged” if no changes were made to either global space or the heap.
<table>
<thead>
<tr>
<th>Call Stack</th>
<th>Global Space</th>
<th>The Heap</th>
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<tbody>
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<td>Call Stack</td>
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5. [21 points total] **Testing and Debugging.**

(a) [9 points] The function `ordinalize` is very similar to the function `anglicize` demonstrated in class. Instead of the normal word for a number, it produces the *ordinal* word. So 1 becomes 'first', 23 becomes 'twenty third', and so on.

There are **at least three bugs** in the code below. These bugs are potentially spread across multiple functions. We have added several print statements throughout the code, and shown the results on the next page. Using this information as a guide, identify and fix the three bugs on the next page. Remember that specifications are always correct, and any deviation between code and a specification is a bug. You **must** explain your fixes.

```python
def ordinalize(n):
    # Small numbers are simple
    if n < 20:
        print('If < 20')  # TRACE
        word = ord1to19(n)
        print('word: ' + word)  # WATCH
    # Big numbers may need 2 words
    if n > 10:
        # Get the first word
        print('If > 10')  # TRACE
        part1 = tens(n // 10)
        print('part1: ' + part1)  # WATCH
        # Check if we need 2nd word
        if n % 10 == 0:
            print('No 2nd word')  # TRACE
            part1 = ithify(part1)
            print('part1: ' + part1)  # WATCH
        else:
            print('Has 2nd word')  # TRACE
            part2 = ' ' + ord1to19(n % 10)
            print('part2: ' + part2)  # WATCH
    word = part1+part2
    print('word: ' + word)  # WATCH
    return word

def ithify(word):
    # Returns word with 'ieth' at end
    result = word[:-1]+'ieth'
    return result

def tens(n):
    # Returns: tens-word for n
    words = ['twenty', 'thirty', 'forty', 'fifty',
             'sixty', 'eighty', 'ninety']
    result = words[n-2]
    return result

def ord1to19(n):
    # Returns: Ordinal word for n.
    words = ['first', 'second', 'third', 'fourth',
             'fifth', 'sixth', 'seventh', 'eighth',
             'ninth', 'tenth', 'eleventh', 'twelfth',
             'thirteenth', 'fourteenth', 'fifteenth',
             'sixteenth', 'seventeenth',
             'eighteenth', 'nineteenth']
    result = words[n-1]
    return result
```

---

Page 8
Tests:

>>> ordinalize(12)  # 'twelfth'
If < 20
ord1to19: 12
result: twelfth
word: twelfth
If > 10
tens: 1
result: ninety
part1: ninety
Has 2nd word
ord1to19: 2
result: second
part2: second
word: ninety second
'twelfth'

>>> ordinalize(30)  # 'thirtieth'
If > 10
tens: 3
result: thirty
part1: thirty
No 2nd word
ithify: thirty
result: thirtieth
part1: thirtieth
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
  File "debug.py", line 29, in ordinalize
    word = part1+part2
UnboundError: 'part2' ref before assignment

>>> ordinalize(99)  # 'ninty ninth'
If > 10
tens: 9
Traceback (most recent call last):
  File "<stdin>", line 1, in <module>
  File "debug.py", line 16, in ordinalize
    part1 = tens(n // 10)
  File "debug.py", line 52, in tens
    result = words[n-2]
IndexError: list index out of range

First Bug:
Second Bug:
Third Bug:
(b) [8 points] Consider the following function specification:

```python
def unique(lst):
    """Returns: The number of unique elements in the list.
Example: unique([1, 5, 5]) returns 2.
Precondition: lst is a list. Any value in lst must be an int.""
```

**Do not implement this function.** Instead, we want you to write at least four test cases below. By a test case, we just mean an input and an expected output; you do not need to write an `assert_equal` statement. For each test case, you should explain why it is substantially different from the others.

(c) [4 points] **Do not implement the function specified below.** Instead, use assert statements to enforce the precondition. You do not need to provide error messages.

```python
def xpand(s):
    """Returns a copy of s with all 'x' replaced by 'xxx'
Example: xpand('extra') returns 'exxxtra'
Precond: s is a string with at least one 'x'. There are no adjacent 'x' characters in s.""
```
Implement the function below. You **may not use a for-loop to implement this function** (and a for-loop is not necessary). Simply use the functions and methods provided on the reference page. Pay close attention to the examples to better understand the function.

```python
def replace_ab(s, a, b, c):
    """Returns copy of s with the FIRST occurrence of a or b replaced by c

    Only the substring (a or b) that occurs FIRST will be replaced by c. If
    neither a nor b is a substring of s, then the string is unchanged.

    Examples:
    replace_ab('abba', 'a', 'b', 'c') returns 'cbba'
    replace_ab('abba', 'b', 'a', 'c') returns 'cbba'
    replace_ab('acaba', 'ca', 'ab', 'd') returns 'adba'
    replace_ab('adda', 'a', 'b', 'c') returns 'cdda'
    replace_ab('xyz', 'a', 'b', 'c') returns 'xyz'

    Preconditions: s, a, b, and c are all strings of lowercase letters.
    a and b are nonempty and start with different letters.""
```