

Module 28

Generators

Recall: The Range Iterable

range(x)

Example

- Creates an *iterable*
 - Can be used in a for-loop
 - Makes ints (0, 1, ... x-1)
- But it is not a tuple!
 - A **black-box** for numbers
 - Entirely used in for-loop
 - Contents of folder hidden

```
>>> range(3)
range(0,3)
>>> for x in range(3)
...     print(x)
0
1
2
```

Recall: The Range Iterable

range(x)

Example

- Creates an *iterable*

```
>>> range(3)
```

- Can be used in a for-loop

- Makes it possible to iterate over a range of values

- But it is not a list

- A **black** box

- Entirely used in for-loop

- Contents of folder hidden

**Iterable: Anything that
can be used in a for-loop**

```
1
```

```
2
```

```
range(3)
```

Iterators: Iterables Outside of For-Loops

- Iterators can *manually* extract elements
 - Get each element with the `next()` function
 - Keep going until you reach the end
 - Ends with a `StopIteration` (Why?)
- Can create iterators with `iter()` function

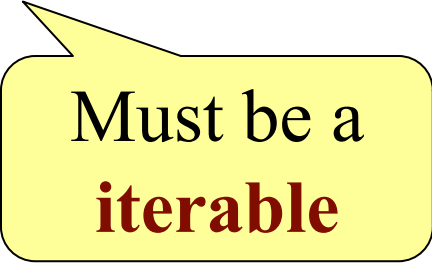
```
>>> a = iter([1,5,3])
```

```
>>> next(a)
```

```
1
```

```
>>> next(a)
```

```
5
```



Must be a
iterable

Iterators Can Be Used in For-Loops

```
>>> a = iter([1,2])
```

```
>>> for x in a:
```

```
...     print(x)
```

```
...
```

```
1
```

```
2
```

```
>>> for x in a:
```

```
...     print(x)
```

```
...
```

```
>>>
```

Technically, iterators
are also iterable

But they are
one-use only!

Iterators are Classes

```
class range2iter(object):
    """Iterator class for squares of a range"""
    # Attribute _limit: end of range
    # Attribute _pos: current spot of iterator
    ...
    def __next__(self):
        """Returns the next element"""
        if self._pos >= self._limit:
            raise StopIteration()
        else:
            value = self._pos*self._pos
            self._pos += 1
            return value
```

Iterators are Classes

```
class range2iter(object):
```

```
    """Iterator class for squares of a range"""
```

```
    # Attribute _limit: end of range
```

```
    # Attribute _pos: current square
```

```
    ...
```

```
    def __next__(self):
```

```
        """Returns the next element"""
```

```
        if self._pos >= self._limit:
```

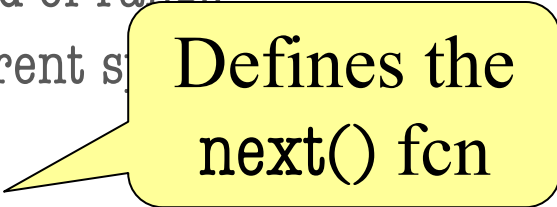
```
            raise StopIteration()
```

```
        else:
```

```
            value = self._pos * self._pos
```

```
            self._pos += 1
```

```
            return value
```



Defines the
next() fcn

Iterators are Classes

```
class range2iter(object):
```

```
    """Iterator class for squares of a range"""
```

```
    # Attribute _limit: end of range
```

```
    # Attribute _pos: current spot of iterator
```

```
    ...
```

```
    def __next__(self):
```

```
        """Returns the next element"""
```

```
        if self._pos >= self._limit:
```

```
            raise StopIteration()
```

```
        else:
```

```
            value = self._pos * self._pos
```

```
            self._pos += 1
```

```
            return value
```

How far to go

How far we are

Raise error when
gone too far

Iterators are Classes

```
class range2iter(object):  
    """Iterator class for squares of a range"""  
    # Attribute _limit: end of range  
    # Attribute _pos: current spot of iterator  
    ...  
    def __next__(self):  
        """Returns the next element"""  
        if self._pos >= self._limit:  
            raise StopIteration()  
        else:  
            value = self._pos*self._pos  
            self._pos += 1  
            return value
```

Update “loop” after
doing computation

Essentially a
loop variable

Iterables are Also Classes

```
class range2(object):
```

```
    """Iterable class for squares of a range"""
```

```
    def __init__(self,n):
```

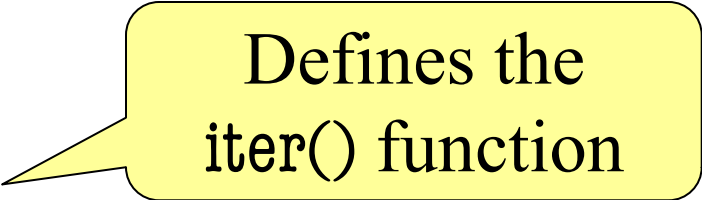
```
        """Initializes a squares iterable"""
```

```
        self._limit = n
```

```
    def __iter__(self):
```

```
        """Returns a new iterator"""
```

```
        return range2iter(self._limit)
```



Defines the
iter() function

Iterables are Also Classes

```
class range2(object):  
    """Iterable class for squares of a range"""  
  
    def __init__(self,n):  
        """Initializes a squares iter  
        self._limit = n  
  
    def __iter__(self):  
        """Returns a new iterator"""  
        return range2iter(self._limit)
```

**Iterables are objects
that generate
iterators on demand**

Iterators are Hard to Write!

- Has the same problem as GUI applications
 - We have a hidden loop
 - All loop variables are now attributes
 - Similar to inter-frame/intra-frame reasoning
- Would be easier if loop were **not** hidden
 - **Idea:** Write this as a function definition
 - Function makes loop/loop variables visible
- But iterators “return” multiple values
 - So how would this work?

The Wrong Way

```
def range2iter(n):
```

```
    """
```

```
    Iterator for the squares of numbers 0 to n-1
```

```
    Precondition: n is an int  $\geq 0$ 
```

```
    """
```

```
    for x in range(n):
```

```
        return x*x
```



Stops at the
first value

The **yield** Statement

- **Format:** `yield <expression>`
 - Used to produce a value
 - But it **does not stop** the “function”
 - Useful for making iterators
- **But:** These are not normal functions
 - Presence of a yield makes a **generator**
 - Function that returns an iterator

The **yield** Statement

- **Format:** `yield <expression>`
 - Used to produce a value
 - But it **does not stop** the “function”
 - Useful for making iterators
- **But:** These are not normal functions
 - Pr
 - Fu

More on this distinction in a bit

The Generator approach

```
def range2iter(n):
```

```
    """
```

```
    Generator for the squares  
    of numbers 0 to n-1
```

```
    Precon: n is an int >= 0
```

```
    """
```

```
    for x in range(n):
```

```
        yield x*x
```

```
>>> a = range2iter(3)
```

```
>>> a
```

```
<generator object>
```

```
>>> next(a)
```

```
0
```

```
>>> next(a)
```

```
1
```

```
>>> next(a)
```

```
4
```


The Generator approach

```
def range2iter(n):
```

```
    """
```

```
    Generator for the squares  
    of numbers 0 to n-1
```

```
    Precon: n is an int >= 0
```

```
    """
```

```
    for x in range(n):
```

```
        yield x*x
```

```
>>> a = range2iter(3)
```

```
>>> a
```

```
<generator object
```

```
>>> next(a)
```

```
0
```

```
>>> next(a)
```

```
1
```

```
>>> next(a)
```

```
4
```

Essentially
a constructor

What Happens on a Function Call?

Visualize Execute Code Edit Code Heap primitives Use an

```
1 def range2iter(n):
2     """Generator for a range of squares"""
3     for x in range(n):
4         yield x*x
5         print('Ended loop for '+str(x))
6
7 → a = range2iter(3)
8
9 → x = next(a)
10 y = next(a)
11 z = next(a)
12 w = next(a)
```

Global

global	
range2iter	id1
a	id2

Frames

id2:generator
range2iter(3)

Creates a generator

No call frame

<< First < Back Step 3 of 20 Forward > Last >>

→ line that has just executed
→ next line to execute

next() Initiates a Function Call

Visualize

Execute Code

Edit Code

Heap primitives Use arrows

```
1 def range2iter(n):
2     """Generator for a range of squares"""
3     for x in range(n):
4         yield x*x
5         print('Ended loop for '+str(x))
6
7 a = range2iter(3)
8
9 x = next(a)
10 y = next(a)
11 z = next(a)
12 w = next(a)
```



<< First

< Back

Step 4 of 20

Forward >

Last >>

→ line that has just executed

→ next line to execute

Globals

Objects

global

range2iter

id1

a

id2

id1:function

Comes from original call

Frames

range2iter

n

3

Frame for next()

Call Finishes at the yield

Visualize

Execute Code

Edit Code

Heap primitives Use arrows

```
1 def range2iter(n):
2     """Generator for a range of squares"""
3     for x in range(n):
4         yield x*x
5         print('Ended loop for '+str(x))
6
7 a = range2iter(3)
8
9 x = next(a)
10 y = next(a)
11 z = next(a)
12 w = next(a)
```

Globals

```
global
range2iter | id1
a          | id2
```

Objects

```
id1:function
range2iter(n)

id2:generator
range2iter(3)
```

Frames

```
range2iter
n | 3
x | 0
Return value | 0
```

<< First

< Back

Step 6 of 20

Forward >

Last >>

→ line that has just executed

→ next line to execute

**yield is return
for next()**

Later Calls Resume After the yield

Visualize

Execute Code

Edit Code

Heap primitives Use arrows

```
1 def range2iter(n):
2     """Generator for a range of squares"""
3     for x in range(n):
4         yield x*x
5         print('Ended loop for '+str(x))
6
7 a = range2iter(3)
8
9 x = next(a)
10 y = next(a)
11 z = next(a)
12 w = next(a)
```



<< First

< Back

Step 8 of 20

Forward >

Last >>

→ line that has just executed

→ next line to execute

Globals

global	
range2iter	id1
a	id2
x	0

Objects

id1: function
range2iter(n)
id2: generator
range2iter(3)

Frames

range2iter	
n	3
x	0

From last time

Next call returns to where it left off

Exception is Made Automatically

Visualize

Execute Code

Edit Code

Heap primitives Use arrows

```
1 def range2iter(n):  
2     """Generator for a range of squares"""  
3     for x in range(n):  
4         yield x*x  
5         print('Ended loop for '+str(x))  
6  
7 a = range2iter(3)  
8  
9 x = next(a)  
10 y = next(a)  
11 z = next(a)  
12 w = next(a)
```

Globals

Objects

global	
range2iter	id1
x	0
y	1
z	4

id1: function
range2iter(n)

Frames

<< First

< Back

Program terminated

Forward >

Last >>

StopIteration:

Exception when
generator is done

Return Statements Make Exceptions

Visualize

Execute Code

Edit Code

Heap primitives Use arrows

```
1 def range2iter(n):
2     """Generator for a range of squares"""
3     for x in range(n):
4         yield x*x
5         print('Ended loop for '+str(x))
6     return x # The final x
7
8 a = range2iter(3)
9
10 x = next(a)
11 y = next(a)
12 z = next(a)
13 w = next(a)
```

Globals

Objects

global	
range2iter	id1
x	0
y	1
z	4

id1: function
range2iter(n)

Frames

<< First

< Back

Program terminated

Forward >

Last >>

StopIteration: 2

Return Value

Exception when
generator is done

Iterator Parameters

- The initial call is essentially a constructor
 - Creates a generator object
 - Parameters used to initialize the object
- **Pattern:** Use an iterable parameter
 - Iterator loops over this iterable
 - Iterator transforms contents of the iterable
 - Iterator yields the transformed data
- Generators often replace **accumulator pattern**

Accumulators: The Old Way

```
def add_one(lst):  
    """Returns copy with 1 added to every element  
    Precond: lst is a list of all numbers"""  
    copy = [] # accumulator  
    for x in lst:  
        x = x + 1  
        copy.append(x)  
    return copy
```

Generators: The New Way

```
def add_one(input)
```

```
    """Generates 1 added to each element of input
```

```
    Precond: input is a iterable of all numbers"""
```

```
    for x in input :
```

```
        yield x + 1
```

Much
Simpler!

**yield eliminates
the accumulator**

Accumulators: The Old Way

```
def evens(lst):  
    """Returns a copy with even elements only  
    Precond: lst is a list of all numbers"""  
    copy = [] # accumulator  
    for x in lst:  
        if x % 2 == 0:  
            copy.append(x)  
    return copy
```

Generators: The New Way

```
def evens(input):
```

```
    """Generates only the even elements of input
```

```
    Precond: input is a iterable of all numbers"""
```

```
    for x in input:
```

```
        if x % 2 == 0:
```

```
            yield x
```

Accumulators: The Old Way

```
def average(lst):
```

```
    """Returns a running average of lst (elt n is average of lst[0:n])
```

```
    Ex: average([1, 3, 5, 7]) returns [1.0, 2.0, 3.0, 4.0]
```

```
    Precond: lst is a list of all numbers"""
```

```
    result = []           # actual accumulator
```

```
    sum = 0; count = 0   # accumulator "helpers"
```

```
    for x in lst:
```

```
        sum = sum+x; count = count+1
```

```
        result.append(sum/count)
```

```
    return result
```

Accumulators: The Old Way

```
def average(lst):
```

```
    """Returns a running average of lst (elt n is average of lst[0:n])
```

```
    Ex: average([1, 3, 5, 7]) returns [1.0, 2.0, 3.0, 4.0]
```

```
    Precond: lst is a list of all numbers"""
```

```
    result = []
```

```
    sum = 0; count = 0
```

```
    for x in lst:
```

```
        sum = sum+x; count = count+1
```

```
        result.append(sum/count)
```

```
    return result
```



Allows multiple assignments per line

Generators: The New Way

```
def average(input):
```

```
    """Generates a running average of input
```

```
    Ex: input 1, 3, 5, 7 yields 1.0, 2.0, 3.0, 4.0
```

```
    Precond: input is a iterable of all numbers"""
```

```
    sum = 0      # accumulator "helper"
```

```
    count = 0   # accumulator "helper"
```

```
    for x in lst:
```

```
        sum = sum+x
```

```
        count = count+1
```

```
        yield sum/count
```

Advanced Data Processing

- Previous lesson saw functions as variables
 - Seemed like a weird but useless trick
- It is very useful in **large data processing**
 - Start with a function on a single piece of data
 - Have a large set (list/tuple) of this data
 - Want to apply function to every data in set
- We can process this data with a *for-loop*
 - But write a new for-loop for each function?

Example: map()

```
def map(f,data)
```

```
    """Returns a copy of data, f applied to each entry
```

```
    Precond: f is a function taking exactly one argument
```

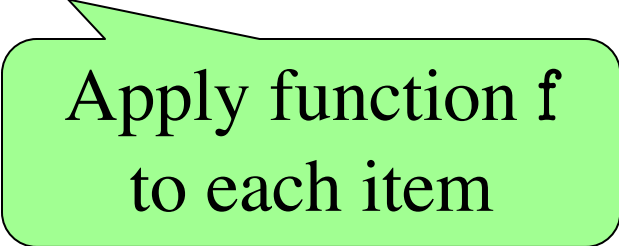
```
    Precond: data iterable, each elt satisfying precond of f"""
```

```
    accum = []
```

```
    for item in data:
```

```
        accum.append( f(item) )
```

```
    return accum
```



Apply function f
to each item

Example: `map()`

```
def plus1(x)
```

```
    """Returns x+1"""
```

```
    return x+1
```

```
def negate(x):
```

```
    """Returns -x"""
```

```
    return -x
```

```
>>> a = [1,2,3]
```

```
>>> b = map(plus1, a)
```

```
>>> b
```

```
[2,3,4]
```

```
>>> c = map(negate, a)
```

```
>>> c
```

```
[-1,-2,-3]
```

The Generator Version

```
def map(f,data)
```

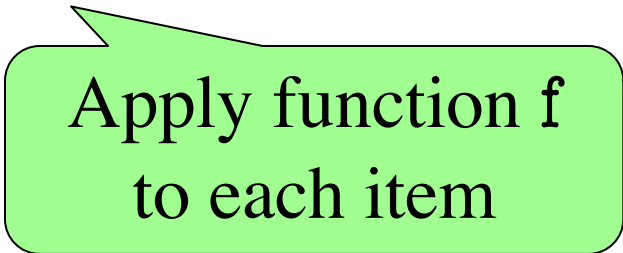
```
    """Generates f applied to each element
```

```
    Precond: f is a function taking exactly one argument
```

```
    Precond: data iterable, each elt satisfying precond of f"""
```

```
    for item in data:
```

```
        yield f(item)
```



Apply function f
to each item

Example: filter()

```
def filter(f,data)
```

```
    """Returns a copy of data, removing anything f is False on
```

```
    Precond: f is a boolean function taking exactly one argument
```

```
    Precond: data iterable, each elt satisfying precondition of f"""
```

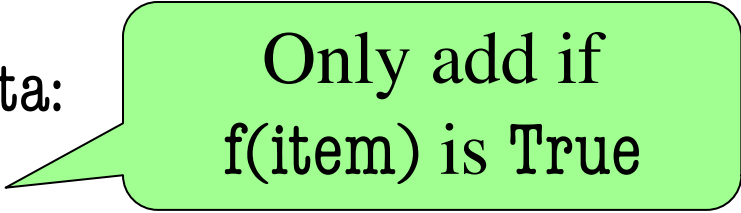
```
    accum = []
```

```
    for item in data:
```

```
        if f(item):
```

```
            accum.append( item)
```

```
    return accum
```



Only add if
f(item) is True

Example: filter()

```
def iseven(x)
    """Rets True if x even"""
    return x % 2 == 0
```

```
def ispos(x):
    """Rets True if x > 0"""
    return x > 0
```

```
>>> a = [-2,1,4]
>>> b = filter(iseven, a)
>>> b
[-2,4]
>>> c = filter(ispos, a)
>>> c
[1,4]
```

The Generator Version

```
def filter(f,data)
```

```
    """Generates all elements of data where f is True
```

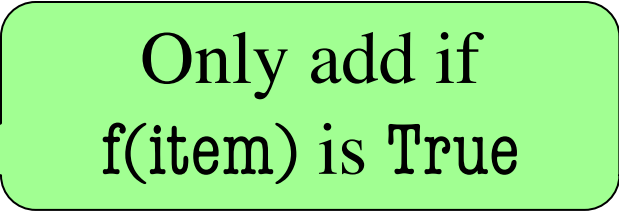
```
    Precond: f is a boolean function taking exactly one argument
```

```
    Precond: data iterable, each elt satisfying precondition of f"""
```

```
    for item in data:
```

```
        if f(item):
```

```
            yield accum
```



Only add if
f(item) is True

These Are Famously Powerful

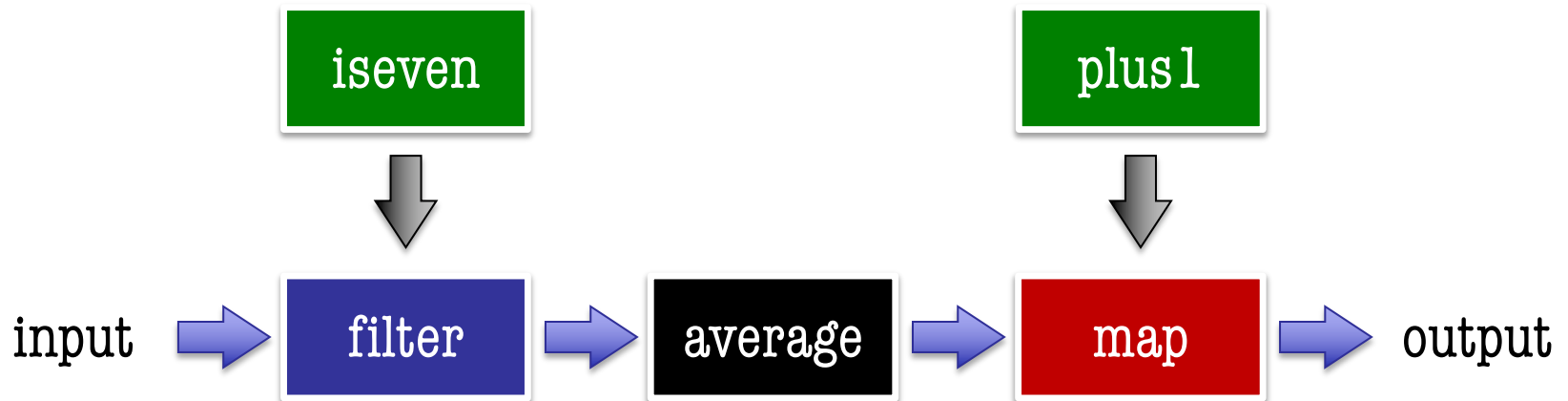
- Functions `map` and `filter` are very powerful tools
 - Focus of study in advanced language courses
 - Form the basis of data processing infrastructure
- They are building blocks to combine together
 - The generators take iterables/iterators as input
 - And the output is a iterator itself
 - So you can chain these generators together
- **Benefit:** Python needs *much* less memory
 - Only looks at one element at a time

Simple Chaining



```
>>> a = [1, 2, 3, 4] # Start w/ any iterable
>>> b = add_one(average(evens(a))) # Apply right to left
>>> c = list(b) # Convert to list/tuple
>>> c
[3.0, 4.0]
```


Chaining with Map and Filter



```
>>> a = [1, 2, 3, 4]
```

```
>>> b = average(filter(iseven,a))
```

```
>>> b = map(plus1,b)
```

```
>>> c = list(b)
```

```
# Start w/ any iterable
```

```
# Apply first funcs
```

```
# Add map to chain
```

```
# Convert to list/tuple
```

Python Encourages This Approach

- This is a natural way to process data
 - Don't write complex programs
 - Just download functions and string together
 - Will see this again if go on to 3110
- Python has a lot of these tools for you
 - Generators map and filter are **built-in!**
 - Other tools in the [itertools](#) module
- Worth exploring on your own

Module `itertools`

Infinite iterators:

Iterator	Arguments	Results	Example
<code>count()</code>	start, [step]	start, start+step, start+2*step, ...	<code>count(10) --> 10 11 12 13 14 ...</code>
<code>cycle()</code>	p	p0, p1, ... plast, p0, p1, ...	<code>cycle('ABCD') --> A B C D A B C D ...</code>
<code>repeat()</code>	elem [,n]	elem, elem, elem, ... endlessly or up to n times	<code>repeat(10, 3) --> 10 10 10</code>

Iterators terminating on the shortest input sequence:

Iterator	Arguments	Results	Example
<code>accumulate()</code>	p [,func]	p0, p0+p1, p0+p1+p2, ...	<code>accumulate([1,2,3,4,5]) --> 1 3 6 10 15</code>
<code>chain()</code>	p, q, ...	p0, p1, ... plast, q0, q1, ...	<code>chain('ABC', 'DEF') --> A B C D E F</code>
<code>chain.from_iterable()</code>	iterable	p0, p1, ... plast, q0, q1, ...	<code>chain.from_iterable(['ABC', 'DEF']) --> A B C D E F</code>
<code>compress()</code>	data, selectors	(d[0] if s[0]), (d[1] if s[1]), ...	<code>compress('ABCDEF', [1,0,1,0,1,1]) --> A C E F</code>

Module `itertools`

Infinite iterators:

Iterator	Arguments	Results	Example
<code>count()</code>	start, [step]	start, start+step, start+2*step, ...	<code>count(10) --> 10 11 12 13 14 ...</code>
<code>cycle()</code>	p	p0, p1, ... plast, p0, p1, ...	<code>cycle('ABCD') --> A B C D A B C D ...</code>
<code>repeat()</code>	elem [,n]	elem, elem, elem, ... endlessly or up to n times	<code>repeat(10, 3) --> 10 10 10</code>

Iterators terminating on the shortest input sequence:

Iterator	Arguments	Results	Example
<code>accumulate()</code>	p [,func]	p0, p0+p1, p0+p1+p2, ...	<code>accumulate([1,2,3,4,5]) --> 1 3 6 10 15</code>
<code>chain()</code>	p, q, ...	p0, p1, ... plast, q0, q1, ...	<code>chain('ABC', 'DEF') --> A B C D E F</code>
<code>chain.from_iterable()</code>			<code>chain.from_iterable(['ABC', 'DEF']) --> A B C D E F</code>
<code>compress()</code>	selectors	s[1], ...	<code>compress('ABCDEF', [1,0,1,0,1,1]) --> A C E F</code>

Cumulative map

+ for iterables

Final Step of Chaining

- The last step of a chain is to convert “back”
 - Data less useful as a generator
 - Would like a list/tuple; easier to manipulate
 - Called **materializing** the computation
- Are there alternatives to list/tuple function?
 - What if we could add code at materialization?
 - We can, but only for lists (not tuples)
 - Called **list comprehension**

List Comprehension

- Basic Format:

[<expression> for <var> in <iterable>]

- Looks like a backwards for-loop
- That because this is an expression

- Similar to conditional expressions:

<expression> if <boolean-exp> else <expression>

- Example: [x for x in iterable]

- This is the same as list(iterable)

Only Works for Lists

Contents of parens is a
generator expression

```
>>> ( x for x in lst ) # Not a tuple  
<generator object <genexpr>>
```

Traditional For-Loops

```
def add_one(lst):
```

```
    """Returns copy with 1 added to every element
```

```
    Precond: lst is a list of all numbers"""
```

```
    copy = [] # accumulator
```

```
    for x in lst:
```

```
        x = x + 1
```

```
        copy.append(x)
```

```
    return copy
```


List Comprehension

```
def add_one(lst):
```

```
    """Returns copy with 1 added to every element
```

```
    Precond: lst is a list of all numbers"""
```

```
    return [x+1 for x in lst]
```

For-Loops with Conditionals

```
def evens(lst):  
    """Returns a copy with even elements only  
    Precond: lst is a list of all numbers"""  
    copy = [] # accumulator  
    for x in lst:  
        if x % 2 == 0:  
            copy.append(x)  
    return copy
```

List Comprehension

```
def evens(lst):
```

```
    """Returns a copy with even elements only
```

```
    Precond: lst is a list of all numbers"""
```

```
    return [ x for x in lst if x % 2 == 0]
```

Comprehension
Filter

```
    # THIS IS VERY DIFFERENT
```

```
    # return [ (x if x % 2 == 0 else None) for x in lst]
```

Conditional
Expression

Nested For-Loops

```
def transpose(table):
```

```
    """Returns: copy of table with rows and columns swapped
```

```
    Precondition: table is a (non-ragged) 2d List"""
```

```
    numcols = len(table[0]) # All rows have same no. cols
```

```
    result = [] # Result (new table) accumulator
```

```
    for m in range(numcols):
```

```
        newrow = [] # Single row accumulator
```

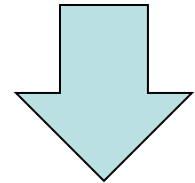
```
        for row in table:
```

```
            newrow.append(row[m]) # Create a new row list
```

```
        result.append(newrow) # Add result to table
```

```
    return result
```

1	2
3	4
5	6



1	3	5
2	4	6

Nested For-Loops

```
def transpose(table):
```

```
    """Returns: copy of table with rows and columns swapped
```

```
    Precondition: table is a (non-ragged) 2d List"""
```

```
    numcols = len(table[0]) # All rows have same no. cols
```

```
    return [[row[i] for row in table] for i in range(numcols)]
```

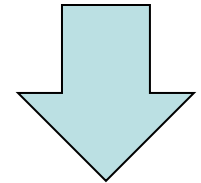


Comprehension



Comprehension

1	2
3	4
5	6



1	3	5
2	4	6

Recall: Dictionaries are Iterable

- Start with a dictionary `d = {'a':1, 'b':2}`
- **Key Iterator:** `d.keys()`
`>>> list(d.keys())`
`['a','b']`
- **Value Iterator:** `d.values()`
`>>> list(d.values())`
`[1,2]`
- **Pair Iterator:** `d.items()`
`>>> list(d.items())`
`[('a',1),('b',2)]`

Dictionary Comprehension

- Basic Format:

```
{ <exp1>:<exp2> for <var> in <iterable> }
```

- <exp1> is the key
 - <exp2> is the value
 - Pairs together form the dictionary
- Otherwise, just like list comprehension
 - Can filter it (with an if at then end)
 - Can nest it with other comprehension

Traditional For-Loops

```
def halve_grades(grades):
```

```
    """Returns a copy cutting all exam grades in half.
```

```
    Precondition: grades has netids as keys, ints as values"""
```

```
    result = { }
```

```
    for k in grades:
```

```
        | result[k] = grades[k]//2
```

```
    return result
```


Traditional For-Loops

```
def halve_grades(grades):
```

```
    """Returns a copy cutting all exam grades in half.
```

```
    Precondition: grades has netids as keys, ints as values"""
```

```
    return { k:grades[k]//2 for k in grades }
```

Traditional For-Loops

```
def extra_credit(grades,students,bonus):
```

```
    """Returns a copy of grades with extra credit assigned
```

```
    Precond: grades has netids as keys, ints as values.
```

```
    netids is a list of valid (string) netids, bonus an int"""
```

```
    result = { }
```

```
    for k in grades:
```

```
        if k in students:
```

```
            result[k] = grades[k]+bonus
```

```
        else:
```

```
            result[k] = grades[k]
```

```
    return result
```

Traditional For-Loops

```
def extra_credit(grades,students,bonus):
```

```
    """Returns a copy of grades with extra credit assigned
```

```
    Precond: grades has netids as keys, ints as values.
```

```
    netids is a list of valid (string) netids, bonus an int"""
```

```
    return { k:(grades[k]+bonus if k in students else grades[k])
            for k in grades }
```

Final Words on Comprehension

Advantages

- Code very compact/concise
- Python can optimize heavily (no wasteful accumulators)

Disadvantages

- Harder to read/understand
- Much harder to debug (more stuff on one line)

Use this technique sparingly