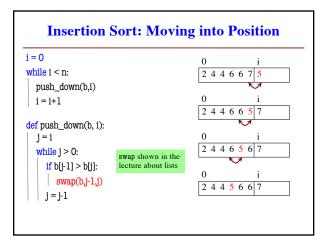
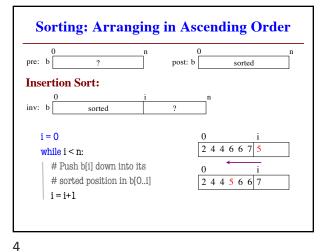


**Binary Search** h k pre: b New statement of the k invariant guarantees post: b that we get leftmost position of v if found k 9 inv: b >= v i=h; j=k+1; while i != j: Looking at b[i] gives linear search from left. Looking at b[j-1] gives linear search from right. Looking at middle: b[(i+j)/2] gives binary search.

3





**Insertion Sort: Performance** def push\_down(b, i): b[0..i-1]: i elements """Push value at position i into • Worst case: sorted position in b[0..i-1]""" ■ i = 0: 0 swaps j = i ■ i = 1: 1 swap while j > 0: • i = 2: 2 swaps **if** b[j-1] > b[j]: Pushdown is in a loop swap(b,j-1,j) Called for i in 0..n j = j-1 Insertion sort is i swaps each time an n<sup>2</sup> algorithm **Total Swaps:**  $0 + 1 + 2 + 3 + \dots (n-1) = (n-1)*n/2$ 

5

Algorithm "Complexity"
• Given: a list of length n and a problem to solve

- Complexity: *rough* number of steps to solve worst case
- Suppose we can compute 1000 operations a second:

Complexity	n=10	n=100	n=1000	
n	0.01 s	0.1 s	1 s	
n log n	0.016 s	0.32 s	4.79 s	
n <sup>2</sup>	0.1 s	10 s	16.7 m	
n <sup>3</sup>	1 s	16.7 m	11.6 d	
2 <sup>n</sup>	1 s	4x10 <sup>19</sup> y	3x10 <sup>290</sup> y	
Major Topic in 2110: Beyond scope of this course				



