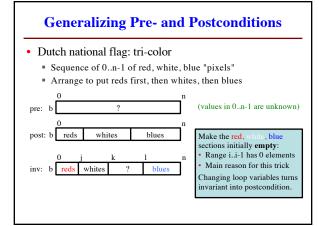
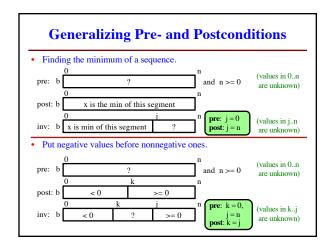
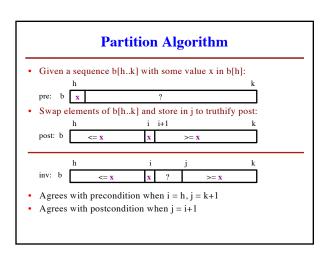


Developing Algorithms on Sequences

- Specify the algorithm by giving its precondition and postcondition as pictures.
- Draw the invariant by drawing another picture that "generalizes" the precondition and postcondition
 - The invariant is true at the beginning and at the end
- The four loop design questions
 - 1. How does loop start (how to make the invariant true)?
 - 2. How does it stop (is the postcondition true)?
 - 3. How does the body make progress toward termination?
 - 4. How does the body keep the invariant true?







Partition Algorithm Implementation $\textcolor{red}{\textbf{def}} \hspace{0.1cm} \textbf{partition(b, h, k):}$ """Partition list b[h..k] around a pivot x = b[h]""" i = h; j = k+1; x = b[h]# invariant: b[h..i-1] < x, b[i] = x, b[j..k] >= x while i < j-1: if b[i+1] >= x;partition(b,h,k), not partition(b[h:k+1]) # Move to end of block. Remember, slicing always copies the list! $_{\text{swap}(b,i+1,j-1)}$ j=j-1 We want to partition the original list else: # b[i+1] < x _swap(b,i,i+1) i = i + 1# post: b[h..i-1] < x, b[i] is x, and b[i+1..k] >= xreturn i

