This 90-minute exam has 9 questions worth a total of 104 points. You may tear the pages apart; we have a stapler at the front of the room.

The second page of this exam gives you the specifications for some useful functions and methods.

You will be expected to write Python code on this exam. We recommend that you draw vertical lines to make your indentation clear, as follows:

```python
def foo():
    if something:
        do something
        do more things
    do something last
```

It is a violation of the Academic Integrity Code to look at any exam other than your own, to look at any other reference material, or to otherwise give or receive unauthorized help.

We also ask that you not discuss this exam with students who are scheduled to take a later makeup.

Academic Integrity is expected of all students of Cornell University at all times, whether in the presence or absence of members of the faculty. Understanding this, I declare I shall not give, use or receive unauthorized aid in this examination.

Signature: _____________________________ Date ___________
For reference:

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
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<tbody>
<tr>
<td>s.find(substr)</td>
<td>Returns: index of first occurrence of string \texttt{substr} in string \texttt{s} (-1 if not found)</td>
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<tr>
<td>s.strip()</td>
<td>Returns: copy of string \texttt{s} where all whitespace has been removed from the beginning and the end of \texttt{s}. Whitespace not at the ends is preserved.</td>
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<tr>
<td>s.split(sep)</td>
<td>Returns: a list of the “words” in string \texttt{s}, using \texttt{sep} as the word delimiter (whitespace if \texttt{sep} not given)</td>
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<td>s.join(slist)</td>
<td>Returns: a string that is the concatenation of the strings in list \texttt{slist} separated by string \texttt{s}</td>
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<tr>
<td>\texttt{s[i:j]}</td>
<td>Returns: if \texttt{i} and \texttt{j} are non-negative indices and \texttt{i} ≤ \texttt{j}-1, a new string containing the characters in \texttt{s} from index \texttt{i} to index \texttt{j}-1, or the substring of \texttt{s} starting at \texttt{i} if \texttt{j} ≥ len(\texttt{s})</td>
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<tr>
<td>lt.append(item)</td>
<td>Adds \texttt{item} to the end of list \texttt{lt}.</td>
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<tr>
<td>lt.remove(item)</td>
<td>Removes the first occurrence of \texttt{item} from list \texttt{lt}.</td>
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<tr>
<td>lt.index(item)</td>
<td>Returns: index of first occurrence of \texttt{item} in list \texttt{lt}; raises an error if \texttt{item} is not found. (There's no “find” for lists.)</td>
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<tr>
<td>lt[i:j]</td>
<td>Returns: A new list \texttt{lt[i], lt[i+1], \ldots, lt[j-1]} under ordinary circumstances. Returns [] if \texttt{i} and \texttt{j} are not both sensible indices</td>
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<tr>
<td>lt.pop(i)</td>
<td>Returns: element of list \texttt{lt} at index \texttt{i} and also removes that element from the list.</td>
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<tr>
<td>map(func, lt)</td>
<td>Returns: A list obtained by applying function \texttt{func} to each element in list \texttt{lt} and concatenating all of the results.</td>
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<tr>
<th>Question</th>
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<td><strong>Total:</strong></td>
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1. **Object Diagramming and Terminology.**

(a) [8 points] Suppose there is a class `Acct` defined in file `a2.py` where `Acct` objects have a `balance` attribute. Consider the following code and associated memory diagrams. Eight items in the diagram have been labeled (A) through (H). Match the vocabulary terms below the diagram with a labeled example by writing a letter next to each term.

```python
1 from a2 import *
2 def swap(source, to):
3     """Swap balance of Acct <source> and balance of Acct <to>""
4     tmp = source.balance
5     source.balance = to.balance
6     to.balance = tmp
7
8 a1 = Acct(50)
9 a2 = Acct(25)
10 swap(a1,a2)
```

Local Variable: _____ Global Variable: _____ Parameter: _____ Attribute: _____
Object: _____ Call Frame: _____ Heap Space: _____ Global Space: _____
(b) [9 points] Consider the following 6 lines entered in Python interactive mode. Diagram all variables and objects created at the end of execution. Do not diagram any call frames.

```python
>>> x = 1
>>> y = x
>>> x = 2
>>> p = [1,2]
>>> q = p
>>> p[1] = 5
```
2. **String processing, testing.**

In the US, 10-digit telephone numbers are typically represented in one of the two following styles:

- “Parenthetical”: (555) 666-1110
- “Dashed”: 555-666-1110

There is no whitespace in a Dashed phone number: they are all exactly 12 characters long. There is only one space in a Parenthetical phone number, and it is after the “)”; they are all exactly 14 characters long, counting the space.

(a) [10 points] Implement the following function according to its specification.

```python
def phone_to_paren(s):
    """ Returns: a string representing the phone number s in Parenthetical form.
    """

    Precondition: s is a non-empty string that *would* be a valid Dashed phone number
    EXCEPT that it possibly has spaces around the dashes.

    Examples: '555-666-1110'
              '555 - 666 - 1110'
              '555 - 666-1110'
              ... all yield the same result, '(555) 666-1110' """
(b) [6 points] Consider the following function specification.

```python
def area_code(s):
    """ Returns: an int representing the area code (first three digits)
of a telephone number in string s.
Precondition: s is a non-empty string that *would* be a valid Dashed or Parenthetical phone number, EXCEPT it possibly has spaces around the dashes.""
```

Write **three conceptually distinct test cases** for this function in the table below.

**Test case #1**
Input and expected output:

Rationale:

**Test case #2**
Input and expected output:

Rationale:

**Test case #3**
Input and expected output:

Rationale:
3. [10 points] **Time for Objects!** The Time class is defined so that Time objects have two attributes, `hours` and `minutes`.

Write the body for the function below so that it implements its specification.

You may assume it is being defined in the same file as the definition for Time, so that you can create a new Time object with, say, 1 hour 30 minutes via the call `Time(1,30)`.

```python
def mirror_time(t):
    """Modifies Time object t to be its "mirror image" on the clock.
    Does NOT create a new object; does not return a value.
   "
    To get a "mirror image" time:
    1. If the hours are 12, then the hours should stay the same.
       Otherwise, take 12 and subtract the hours to get the new hours.
    2. If the minutes are 0, then the minutes should stay the same.
       Otherwise, take 60 and subtract the minutes to get the new minutes.
    Examples: 10:10 -> 2:50
              12:00 -> 12:00
              4:30 -> 8:30
    Precondition: t is a Time object with hours <= 12, minutes <= 59 """".
```
4. [16 points] **Banking on objects.** Suppose you are working on a file that defines two classes:

- **Acct:** Acct objects have a float attribute, `balance`
- **Person:** Person objects have two attributes:
  - `partner`, which is either a Person object or `None`
  - `bank_acct`, which is an Acct object.

Inside the same file that defines the classes Acct and Person is also the following function header and specification. Write the body of the function so that it implements its specification.

```python
def groupem(p1, p2):
    """
    1. Creates a new Acct whose balance is the sum of the balances of
       p1 and p2's bank_acct objects;

    2. Changes the balances of both p1's bank_acct and p2's bank_acct to 0

    3. Changes both p1's bank_acct and p2's bank_acct to the new Acct

    4. Makes the partner of p1 be p2 and the partner of p2 be p1.
    
    Preconditions: p1 and p2 are Persons whose partners are both None.""
    
    # hint: if p1 is a Person, p1.bank_acct is an Acct. So you can write
    #       (p1.bank_acct).balance, or even p1.bank_acct.balance
```
5. [7 points] **The import of import.** Suppose file `andersen.py` defines a function `is_the_one` that takes a string as input, performs some computation, and returns a Boolean.

And, suppose file `lee.py` also defines a function `is_the_one` that takes a string as input, but performs some possibly different computation, and returns a Boolean.

Finally, suppose you are writing code in a third file `matrix.py`, which is currently empty.

Write code to be placed in the third file that:

- stores in variable `neo` the result of calling the `andersen.py` version of `is_the_one` on the string "Thomas"; and
- stores in variable `oracle` the result of calling the `lee.py` version of `is_the_one` on the string "Thomas"

6. **For-loop analysis.** Consider the following function header and specification:

```python
def vowel_in_common(s1, s2):
    """Let the vowels be defined as a, e, i, o, u.
    If there is some vowel v contained in both s1 and s2, return a list of the index of the first v in s1 and the index of the first v in s2.
    If there is more than one such vowel v, v = the alphabetically first one.
    If s1 and s2 have no vowel in common, return the list [-1, -1].
    """
    If there is some vowel v contained in both s1 and s2, return a list of the index of the first v in s1 and the index of the first v in s2.
    If there is more than one such vowel v, v = the alphabetically first one.
    If s1 and s2 have no vowel in common, return the list [-1, -1].
```

Preconditions: `s1` and `s2` are non-empty strings.

Examples:

```python
vowel_in_common("brad", "angelina") -> [2, 0]
vowel_in_common("romeo", "romeo") -> [3, 3]
vowel_in_common("dan", "phil") -> [-1, -1]
```

"""
Here is one proposed implementation of *vowel_in_common*. It may or may not be correct.

```python
for v in ['a', 'e', 'i', 'o', 'u']:
    i1 = s1.find(v)
    i2 = s2.find(v)
    if i1 != -1 and i2 != -1:
        return [i1, i2]
    else:
        return [-1, -1]
```

(a) [6 points] Suppose someone makes the call

```
indices = vowel_in_common("brad", "angelina")
```

What is the value of local variable *v* just before the function returns?

What is the return value of the call?

(b) [4 points] Suppose someone makes the call

```
indices = vowel_in_common("romeo", "romeo")
```

What is the value of local variable *v* just before the function returns?

What is the return value of the call?
(c) [7 points] Here is an alternative proposed implementation of `vowel_in_common`. It may or may not be correct.

```python
found = "" # first vowel found in both
for v in ['a', 'e', 'i', 'o', 'u']:
    if v in s1 and v in s2 and found == "":
        found = v

if v == ":
    return [-1, -1]
else:
    return [s1.index(v), s2.index(v)]
```

Suppose someone makes the call
```
indices = vowel_in_common("brad", "angelina")
```

For the alternative implementation, what is the value of local variable `v` just before the function returns?

What is the value of local variable `found` just before the function returns?

What is the return value of the call?
7. [10 points] Lists. The Towers of Hanoi is a famous math puzzle that involves moving circular disks (with a hole in the middle) from one tower to another. There are three towers: “left”, “middle”, and “right”, and each disk has a unique size. The goal is to move all of the disks from the left tower to the right tower without putting a larger disk on top of a smaller disk.

The towers can be represented in Python as lists of integers. Each disk has its own unique associated integer. The first element in the list represents the bottom of the tower, and the last element represents the top. For example, the above setup could be represented as:

```
left = [4, 3, 2, 1]
middle = []
right = []
```

Below is the specification of a function `move` to move disks (integers) from one list to another. For example, after executing the following code:

```
left = [4, 3, 2, 1]
middle = []
move(left, middle)
```

`left` should contain `[4, 3, 2]` and `middle` should contain `[1]`.

```python
def move(from_tower, to_tower):
    '''Tries to move a disk from from_tower to to_tower. More specifically,

    * if to_tower is empty, or if to_tower is not empty and its last element is
      larger than the last element of from_tower, then removes the integer at the
      end of from_tower and appends it to the end of to_tower.

    * otherwise, does nothing.

    Precondition: from_tower and to_tower are lists of integers representing
    disks. from_tower has at least one disk. to_tower may be an empty list.
    Procedure, not a fruitful function, so no return.''
```

Implement this function on the next page.
# Put your code for function move below.
8. [10 points] **String Processing.** Write this function’s body so that it implements its specification.

```python
def glue(name1, stop1, name2, start2):
    """Returns:
    -1 if stop1 is not a valid index for name1 or if
    start2 is not a valid index for name2
    Otherwise, returns a new string formed by concatenating:
    the substring of name1 starting at index 0 and ending at index stop1
    with
    the substring of name2 starting at index start2 and going to the end
    Preconditions:
    name1 and name2 are non-empty strings of lowercase letters
    stop1 and start2 are nonnegative ints
    Examples:
    glue("jules", 1, "vincent", 3) -> "jucent"
    glue("jules", 4, "vincent", 4) -> "julesent"
    glue("jules", 2, "vincent", 0) -> "julvincent",
    glue("jules", 5, "vincent", 4) -> -1
    glue("jules", 1, "vincent", 100) -> -1
    """
```

9. [1 point] Write your last name, first name, and Cornell NetID at the top of each page.

Did you write your name and netID on each page, and re-read all specs, and check your code works against test cases?