This 150-minute exam has 9 questions worth a total of 117 points. You may separate the pages while working on the exam; we have a stapler available.

The second page of this exam gives you the specifications for some useful functions and methods.

You will be expected to write Python code on this exam. We recommend that you draw vertical lines to make your indentation clear, as follows:

```python
def foo():
    if something:
        do something
        do more things
    do something last
```

It is a violation of the Academic Integrity Code to look at any exam other than your own, to look at any other reference material, or to otherwise give or receive unauthorized help.

We also ask that you not discuss this exam with students who are scheduled to take a later makeup.

Academic Integrity is expected of all students of Cornell University at all times, whether in the presence or absence of members of the faculty. Understanding this, I declare I shall not give, use or receive unauthorized aid in this examination.

Signature: ___________________________ Date ____________
<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
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</thead>
<tbody>
<tr>
<td><code>s.find(substr)</code></td>
<td>Returns: starting index of first occurrence of string <code>substr</code> in string <code>s</code> (-1 if not found)</td>
</tr>
<tr>
<td><code>s.strip()</code></td>
<td>Returns: copy of string <code>s</code> where all whitespace has been removed from the beginning and the end of <code>s</code>. Whitespace not at the ends is preserved.</td>
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<tr>
<td><code>s.split(sep)</code></td>
<td>Returns: a list of the “words” in string <code>s</code>, using <code>sep</code> as the word delimiter (whitespace if <code>sep</code> not given)</td>
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<tr>
<td><code>s.join(slist)</code></td>
<td>Returns: a string that is the concatenation of the strings in list <code>slist</code> separated by string <code>s</code></td>
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<tr>
<td><code>lt.append(item)</code></td>
<td>Adds <code>item</code> to the end of list <code>lt</code></td>
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<tr>
<td><code>range(n)</code></td>
<td>Returns: the list <code>[0 .. n-1]</code></td>
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<tr>
<td><code>lt.remove(item)</code></td>
<td>Removes the first occurrence of <code>item</code> from list <code>lt</code>; raises an error if <code>item</code> is not found.</td>
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<tr>
<td><code>lt.index(item)</code></td>
<td>Returns: index of first occurrence of <code>item</code> in list <code>lt</code>; raises an error if <code>item</code> is not found. (There’s no “find” for lists.)</td>
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<tr>
<td><code>lt[i:j]</code></td>
<td>Returns: A new list <code>[lt[i], lt[i+1], ..., lt[j-1]]</code> under ordinary circumstances. Returns <code>[]</code> if <code>i</code> and <code>j</code> are not both sensible indices</td>
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<tr>
<td><code>lt.pop(i)</code></td>
<td>Returns: element of list <code>lt</code> at index <code>i</code> and also removes that element from the list <code>lt</code>.</td>
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<tr>
<td><code>map(func, lt)</code></td>
<td>Returns: A list obtained by applying function <code>func</code> to each element in list <code>lt</code> and concatenating the results of each application.</td>
</tr>
<tr>
<td><code>isinstance(o, c)</code></td>
<td>Returns: True if <code>o</code> is an instance of class <code>c</code>, False otherwise.</td>
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<table>
<thead>
<tr>
<th>Question</th>
<th>Points</th>
<th>Score</th>
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<tbody>
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<td>1</td>
<td>11</td>
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<td>2</td>
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<td>Total:</td>
<td>117</td>
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</tbody>
</table>
1. [11 points] Implement the following function according to its specification.

   def putSideBySide(two_line_strings):
       """Returns: a string with two lines. The first line of the return string
       should contain, in order, the first line of each string in two_line_strings,
       separated by a space. The second line of the return string should contain,
       in order, the second line of each string in two_line_strings, separated by a space.

       Input: two_line_strings, which is a non-empty list of two-line strings.
       Each string has exactly this form: xx
       xx, where x is a character
       in [a..z or A..Z or 0..9]. There will always be exactly two characters
       before and after the new line character \n.

       Remember that \n is a SINGLE special character indicating a new line
       (which causes the string to print over multiple lines).

       For example:
       putSideBySide(["AB\nCD", "EF\nGH"]) should return "AB EF\nCD GH".

       This corresponds to arranging strings that print as:

       AB
       CD

       and:

       EF
       GH

       into the following:

       AB EF
       CD GH

       Note: should NOT add a space before the first string or after the last string.
       This would be wrong because there is a space before the first AB\nCD:

       AB EF
       CD GH

       Another example:
       putSideBySide(["AB\nCD", "EF\nGH", "IJ\nKL"]) returns "AB EF IJ\nCD GH KL".
       """
# Put your code for function putSidebySide below.
2. [21 points] Consider the following code to solve the "Towers of Hanoi" problem. We guarantee there are no errors.

class Tower(object):
    def __init__(self, name, disks):
        self.disks = disks
        self.name = name

    def topDisk(self):
        if self.disks == []:
            return None
        else:
            return self.disks[len(self.disks) - 1]

    def popTopDisk(self):
        return self.disks.pop(len(self.disks) - 1)

    def move(self, to):
        if self.topDisk() is not None:
            isEmpty = to.topDisk() is None
            if isEmpty or to.topDisk() > self.topDisk():
                to.disks.append(self.popTopDisk())

def plan(source, target, other, num_disks):
    if num_disks == 1:
        source.move(target)
    else:
        plan(source, other, target, num_disks-1)
        print "move disk"
        source.move(target)
        plan(other, target, source, num_disks-1)

left = Tower("left", [2, 1])
middle = Tower("middle", [])
right = Tower("right", [])
plan(left, right, middle, len(left.disks))

In the space above, draw the function call frames for plan, global variables, and object folders that result by running this code.

Do NOT draw class folders or folders for functions. You do NOT need to draw function call frames for any function other than plan.

Remember that lists are objects.
3. For debugging purposes, Professor Andersen wants to count how many moves it takes to complete the Towers of Hanoi puzzle in the previous example. He added a print statement on line 27 to print “move disk” whenever a “disk” is moved. This may have been a poor choice.

(a) [1 point] How many times will “move disk” get printed when the code is run?

(b) [1 point] How many moves were actually made (i.e., line 20 was actually executed)?

(c) [3 points] Suggest how Prof. Andersen can change the code so that “move disk” is printed each time a move is made. Refer to specific line numbers on which print statements should be inserted or deleted, and also be clear about the level of indentation of any added prints.

4. Consider the following subclass Loutcome of class Outcome. It has almost the same class invariant as Outcome. The differences are shown in orange below, so you should be to just skim the orange parts.

```python
class Loutcome(Outcome):
    """ An instance is a loser-annotated outcome in a tournament tree. """
    """ Attributes:
    winner [nonempty str]: name of the winner in this Loutcome
        Must be the same as the name of *exactly one* of attributes input1 or
        input2, defined next.
    loser [nonempty str]: name of the loser in this Loutcome
    input1 [Loutcome or nonempty string]:
        If a nonempty string, the name of a competitor in the tournament, and
        we say that the name of input1 is that string.
        If a Loutcome, then the name of input1 is its winner attribute.
    input2 [Loutcome or nonempty string]:
        If a nonempty string, the name of a competitor in the tournament, and
        we say that the name of input2 is that string
        If a Loutcome, then the name of input2 is its winner attribute.
    Note that the constraints (invariants) on winner imply that the names of
    input1 and input2 must be different. """
```
(a) [12 points] Implement the \_\_init\_\_ method of Loutcome below.

\[
def \_\_init\_\_(self, in1, in2, one\_won=True):
    
    
    
    If one\_won is True, loser is the name of in2's winner
    (if in2 is an Loutcome) or in2 itself (if in2 is a string)
    
    Otherwise, loser is in1's winner (if in1 is an Loutcome) or
    in1 itself (if in1 is a string)

    Preconditions: same as for the \_\_init\_\_ for Outcome, except substitute
    the word "Loutcome" for "Outcome" ""

    ### You MUST effectively call the \_\_init\_\_ method of Outcome.
    ### Its header is: def \_\_init\_\_(self, in1, in2, one\_won=True)
    ### You are allowed to use \_extract\_name (see below for specification).
\]

Specification for \_extract\_name(). It is not a method of Outcome.

def \_extract\_name(x):

    
    
    
    Returns: string that is the name of x, defined as follows:
    If x is an Outcome, then the name is x's winner; otherwise, the name is x itself.

    Precondition: x is either a non-empty string or an Outcome.""
(b) [17 points] Implement the following method of **Loutcome** according to its specification.

```python
def winsAndLosses(self, team):
    """Returns: a two-item list where the item at index 0 is the number of
games that team won, and the item at index 1 is the number of games
that team lost.

Precondition: team [str] is a team that played in this Loutcome.

Example: for the Loutcome below:

Here's the desired output for various teams:

| D beat B        | "A" --> [1,1] |
| D beat A        | "B" --> [1,2] |
| A beat B        | "C" --> [0,2] |
| A               | "D" --> [3,0] |
| B               |               |
| C               |               |
| D               |               |
| B beat C        |               |
| B               |               |
| C               |               |

"""

### Hint: We are dealing with Loutcomes, so you don't need _extract_name.
```
5. [12 points] Implement the following function according to its specification.

```python
def merge_records(d1, d2):
    """Input: d1 and d2 are (possibly empty) dictionaries representing win-loss records:
    Each key is a non-empty string representing a team name.
    The value for each key is a two-item list of ints, where the first is
    the number of wins and the second is the number of losses for that
    team in some tournament/outcome tree.

    This function adds the win-loss records of d2 into d1.

    WARNINGS: It does NOT return anything; it changes d1 but not d2.
    And, the values in the altered d1 should be different list objects than the
    list objects that are values in d2, even if they have the same numbers in them.

    For example:

    if d1 is
        {"Cornell": [10,1],  {"Cornell": [2,0],  {"Cornell": [12,1],
        "Harvard": [4,3]}   "Stanford": [0,3]}   "Harvard": [4,3],
    and d2 is
        {"Cornell": [2,0],  {"Cornell": [12,1],
        "Harvard": [4,3]}   "Stanford": [0,3]}
    then d1 becomes
        {"Cornell": [12,1],  {"Cornell": [12,1],
        "Harvard": [4,3]}   "Stanford": [0,3]}

    where the new d1's "Stanford" list [0,3] is a DIFFERENT list object
    than d2's "Stanford" list object ""

    ### HINT: for a list mylist, list(mylist) or mylist[:] returns a copy of mylist.
```
6. A progression is a sequence of integers that are separated by the same distance; for instance, 5, 10, 15, 20 is a progression with 3 steps of step-size 5, and -15, -12, -9 is a progression with 2 steps of step-size 3.

We would like to use a while-loop to write a function `has_progression(x, step, n)` that returns the starting index `start` in list of ints `x` for a progression of step-size `step` that has at least `n` steps. (It should return -1 if there is no such `start`, and we require that `n>=1`).

For example, suppose that `x` is [1, 2, 14, 16, 18, 20, 22]. Then,

`has_progression(x, 2, 4) --> 2 b/c the step-2 progression 14,16,18,20,22
starts at x[2] and has 4 steps.`
`has_progression(x, 2, 5) --> -1`
`has_progression(x, 1, 1) --> 0`

We give you the following invariant, documenting variables `start`, `m`, and `i`.

<table>
<thead>
<tr>
<th>start</th>
<th>i</th>
</tr>
</thead>
<tbody>
<tr>
<td>x</td>
<td>the progression can’t start here</td>
</tr>
</tbody>
</table>

In words, `x[start..i-1]` forms a progression with `m` steps; `x[..start-1]` does not contain an `n`-step progression, and if `start-1` is a valid index, then `x[start-1] != x[start] - step`.

(a) [4 points] We initialize `i` to be 1, because there is necessarily a progression in `x[0..0]`, albeit one with 0 steps.

What should we then initialize `m` and `start` to be, **according to the invariant**?

(b) [3 points] Is the following a correct while-loop condition **according to the invariant**? If yes, write the word “YES” below it; otherwise, cross it out and write a correct while-loop condition below it.

`while m < n and i < len(x) - 1:`
(e) [5 points] Suppose the invariant is true, and \( m \) is much less than \( n \) and \( i \) is much less than the length of \( x \).

Now, suppose we find out that \( x[i] = x[i-1] + \text{step} \). *According to the invariant...*

...should \( m \) and/or \( i \) be updated? If so, give Python code making the update(s); if not, write “No changes”.

...and, should \( \text{start} \) be updated? If so, give Python code making the update; if not, write “No change to \( \text{start} \)”.

Helper function for question on next page.

```python
def swap(b, h, k):
    """ Swaps element h and k in list b ""
    tmp = b[h]
    b[h] = b[k]
    b[k] = tmp
```
7. [15 points] Implement string_list_sort according to its specification.

```python
def string_list_sort(b, h, k):
    """Swaps items in the PORTION of list b from index h up to and including
    index k so that strings are in front and lists are in back.
    Returns: index i such that b[h..i] are strings and b[i+1..k] are lists.
   "
    Example: if b = [['Prospero', 'and', 'Ariel'], 'how', ['are', 'you']]
    string_list_sort(b, 0, 2) returns 0,
    and could change b to:
    ['how', ['are', 'you'], ['Prospero', 'and', 'Ariel']]
    or
    ['how', ['Prospero', 'and', 'Ariel'], ['are', 'you']]

    Your solution MUST use a while loop, MUST NOT create a copy of the list,
    and MUST satisfy the invariants set out in the code below.

    Precondition: b is a nonempty list containing only lists and strings; h and k
    are integers that are valid indices in list b"
    # INVARIANT: b[h..i] are strings, b[t..k] are lists
    # PRECONDITION: no strings or lists yet identified (b[h..i] and b[t..k] both empty)

    # FIRST, FIX THESE INITIALIZATIONS
    i = None
    t = None

    # Hint: you may use the swap function from the previous page

    return i
    #POSTCONDITION: b[h..i] are strings, b[i+1..k] are lists
```
8. (a) [3 points] Consider the following class definition:

```python
1 class Bird(object):
2     def __init__(self, n):
3         self.name = n
4     def tweet(self, punc):
5         output = self.name + " says tweet"
6         return output + str(punc)
```

Write a Python assignment statement that stores in variable `x` the ID of a new Bird object whose name is the string “Caliban”.

(b) [8 points] Consider the following objects and global variables:

```
  b1  id1
  b2  id2
```

Draw the call frame that results from the call `b2.tweet('?')`, stopping execution just before line 6 is executed. Include any crossed-off variable contents or line numbers.

9. [1 point] Fill in your last name, first name, and Cornell NetID at the top of each page.

Did you write your name and netID on each page, and re-read all specs, and check that your code works against test cases? Then have a great summer!