This 90-minute exam has 6 questions worth a total of 100 points. Scan the whole test before starting. Budget your time wisely. Use the back of the pages if you need more space. You may tear the pages apart; we have a stapler at the front of the room.

It is a violation of the Academic Integrity Code to look at any exam other than your own, to look at any other reference material, or to otherwise give or receive unauthorized help.

You will be expected to write Python code on this exam. We recommend that you draw vertical lines to make your indentation clear, as follows:

```python
def foo():
    if something:
        do something
        do more things
    do something last
```

You may not use while-loops. Beyond that, you may use any Python feature that you have learned about in class (particularly for-loops and recursion).

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The Important First Question:

1. [2 points] Write your last name, first name, and Cornell NetId at the top of each page.
2. [26 points] **Classes and Subclasses** On the next two pages are the skeletons of two classes. For **Species** complete the two properties and a constructor (not `str`). For **Animal** complete everything. Enforce invariants in setters and enforce preconditions in both constructors. Do not write specifications (e.g. for the properties) beyond what is given.

class Species(object):
    """Instance is an endangered species""
    # IMMUTABLE ATTRIBUTES
    _name = '' # Species name; must be a string
    # MUTABLE ATTRIBUTES
    _year = 0 # Year on endangered list; int >= 1900 (0 if not on list)

    # DEFINE PROPERTY name for FIELD _name (specification not necessary)

    # DEFINE PROPERTY year for FIELD _year (specification not necessary)

def __init__(self):
    """Constructor: species with name s, put on list in year y.
    Precondition: s a string, y an int >= 1900 or == 0.
    y has default of 0.""

    def __str__(self):
        """Returns: Description of this species
        We have completed this method for you. Do not change it.""
        suffix = ''
        if self.year != 0:
            suffix = ' endangered since ' + str(self.year)
        return self.name+suffix
class Animal(Species):
    """Instance is a species of Animal""
    # IMMUTABLE ATTRIBUTES
    _legs = 0 # Number of legs; int >= 0

    # DEFINE PROPERTY legs for FIELD _legs (specifier not necessary)

    def __init__(self,s,x):
        """Constructor: an x-legged animal of species s that is not endangered.
        Precondition: s a string, x an int >= 0.""
        # YOU MUST USE SUPER()

    def __str__(self):
        """Returns: Description of this species
        Format is __str__ from the superclass followed by ' with <legs> legs', where
        you fill in the value for legs.""
        # YOU MUST USE SUPER()

3. [18 points] **Drawing Folders** Suppose you are executing the following sequence of commands at the interactive prompt (and hence in global space).

```python
>>> x = Species('Indiana Bat', 1967)
>>> y = Animal('Red Wolf', 4)
>>> z = x
>>> x.year = 0
```

On the next page (or the back), create two columns: one for global space and another for heap space. Clearly show what is created in each, drawing folders for objects and boxes for variables. If the value of a variable or attribute changes, cross the old one out and write the new value out beside it.
4. [14 points] **Iteration.**
Complete procedure `clamp(seq,vmin,vmax)` below according to the specification. You should use a for-loop. Do not use recursion or a while-loop. Note that it is a procedure that modifies the list. It does not return a new value. You do not need to assert function preconditions.

**Hint:** The function `len` gives the length of a list.

def clamp(seq,vmin,vmax):

    """Clamp the values in list seq (modifies seq, does not return a copy).

    Values less than vmin become vmin; values greater than vmax become vmax
    Example: if a = [2, -5, 7], then clamp(a,-4,4) modifies the list a so that it is now [2, -4, 4].

    Precondition: seq is a list of ints. vmax > vmin are ints."""
5. [22 points total] **Recursion.**

(a) [14 points]

m-RNA (messenger RNA) is a chain or string of “nucleotides.” These nucleotides are typically denoted by the four symbols 'C' (cytosine), 'G' (guanine), 'A' (adenine), and 'U' (uracil). When writing programs to process m-RNA, we typically represent them as a string of these four letters. For example, 'AUUGC' is an m-RNA sequence.

Each nucleotide has a complementary nucleotide with which it bonds; 'C' and 'G' are a complementary pair, as are 'A' and 'U'. We call the RNA sequence 'CGGGCCCG' a perfect hinge because, if the right half is reversed and placed under the left half, the corresponding characters are complementary. This is shown above. From this definition of a perfect hinge, we can deduce that an empty sequence is a perfect hinge and a sequence with an odd number of elements is not a perfect hinge.

Structures similar to perfect hinges play an important role in biology. Hence, we often want to detect whether an m-RNA sequence has this property. Implement the function below with the given specification. Use recursion, not a loop.

**Hint:** You may find this problem easier if you write a helper function to check if two symbols are complimentary pairs. If you do, include a specification docstring. *Do not bother to assert the preconditions, for either `ishinge` or any helper function.*

```python
def ishinge(seq):
    """Returns: True if the m-RNA sequence is a perfect hinge. Returns False otherwise (e.g. not even, does not match).

    Precondition: seq is a string with characters 'C', 'G', 'A', 'U'.""
```

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(more space for part a)

(b) [8 points] One recursive function that we saw in class was `factorial`:

```python
def factorial(n):
    """Returns: n!
    Precondition: n a nonnegative integer"
    if n==0: # Base case
        return 1
    # Recursive case
    return n*factorial(n-1)
```

Evaluate the recursive call `factorial(2)` until the base case completes its return-statement at line 2 (but before the frame is erased and the value is returned). Draw the call stack at this point in time. The stack will have 3-4 call frames.
6. [18 points total] **Short Answer.**
   Answer the following questions. Each answer will require multiple sentences, but should not require more than a paragraph.
   (a) [4 points] What is the difference between `is` and `==`? Give an example of when you would want to use each of these operators.

   (b) [4 points] What is `dispatch-on-type`? How does it apply to error handling in Python?

   (c) [4 points] What is the `bottom-up` rule? How does it relate to `overriding`?
(d) [4 points] Explain the difference between *interface* and *implementation*.

(e) [2 points] Is the following function definition legal? Why or why not?

```python
def absmax(x, y=0, z):
    """Returns: the maximum absolute value of x, y, and z.
    Precondition: x, y, and z are numbers (int or float)"
    return max(abs(x), abs(y), abs(z))
```